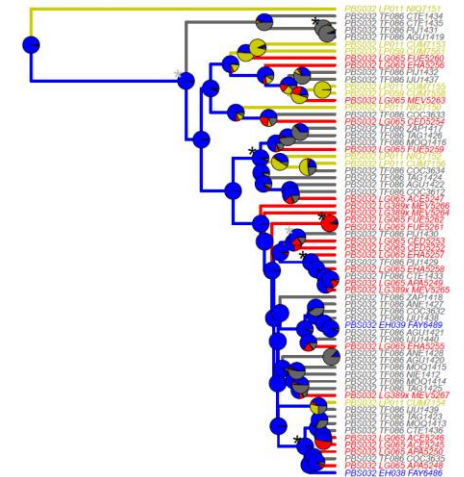
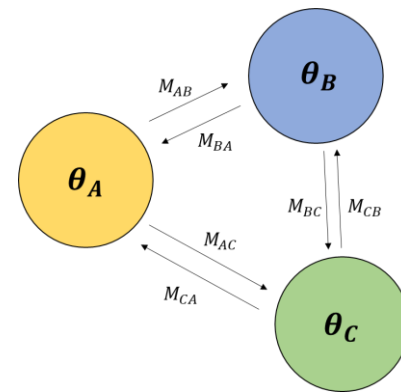
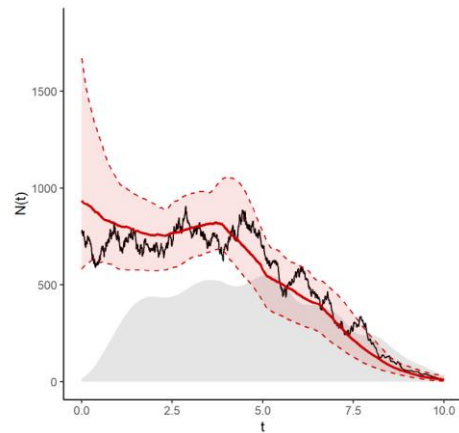
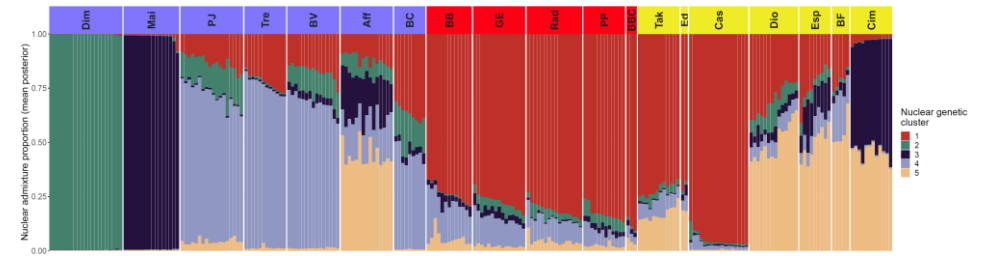
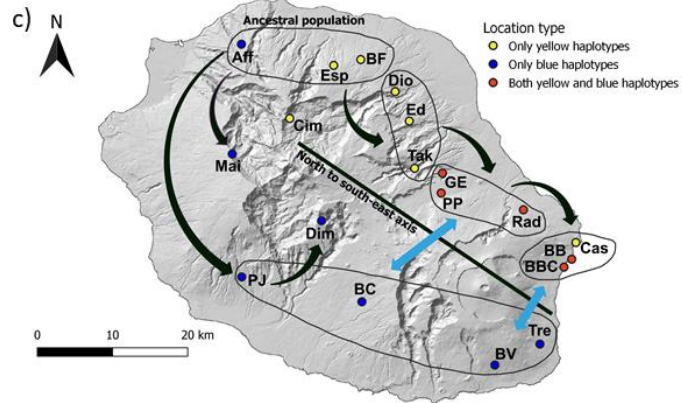
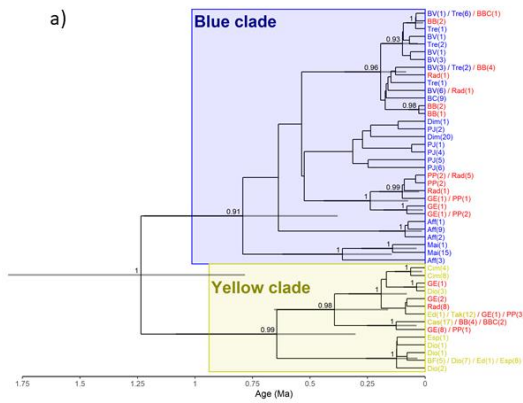


# EMPIRICAL AND METHODOLOGICAL RESEARCH IN BIOGEOGRAPHY, POPULATION GENETICS, AND PHYLOGENETICS

Josselin Cornuault, ISEM, Montpellier

9 janvier 2024



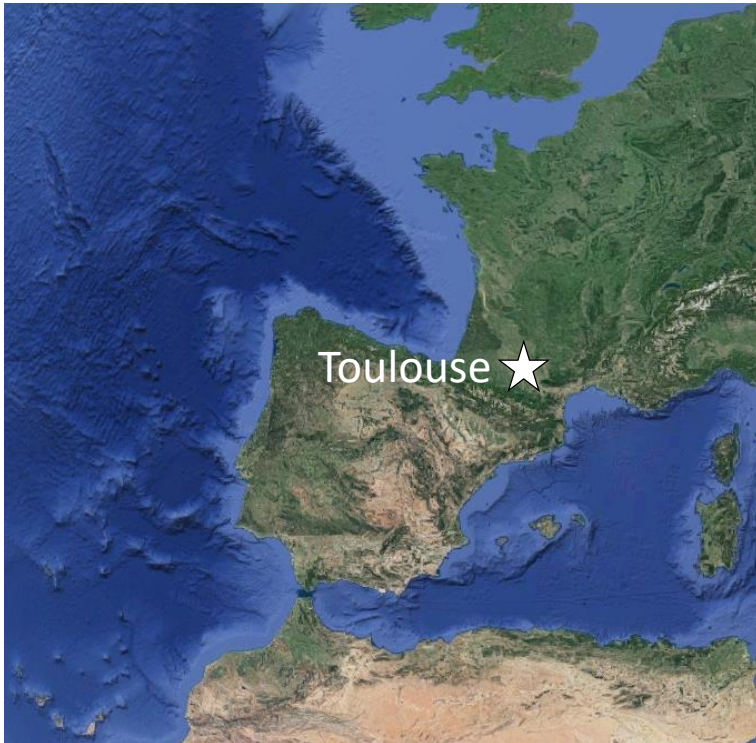
# HEMOSPORIDIAN PARASITES

—

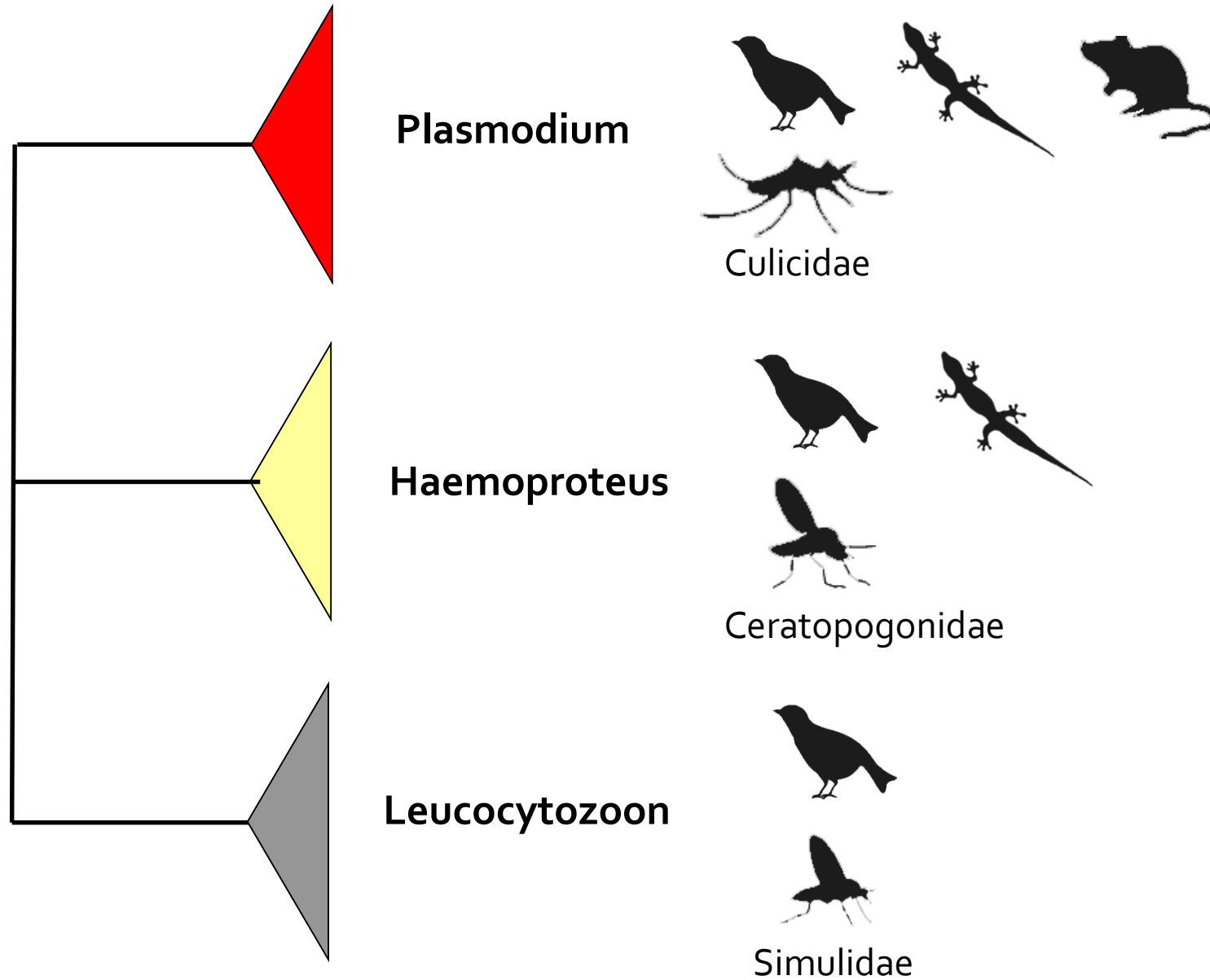
## DIVERSITY IN THE MASCARENES

Josselin Cornuault, Christophe Thébaud, Philippe Heeb, Borja Mila, Ben Warren, Thomas Duval

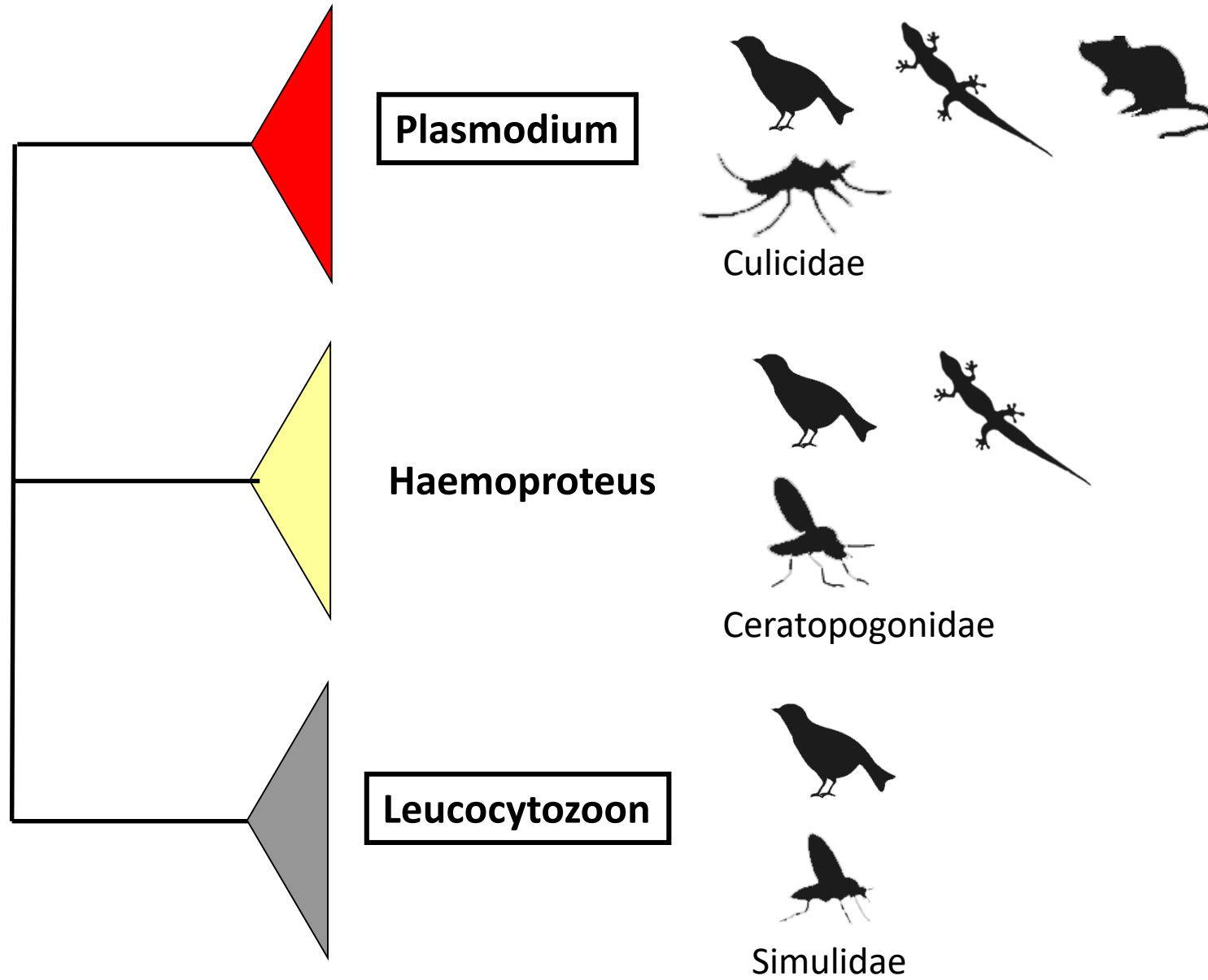
Lab Evolution & Diversité Biologique



# HEMOSPORIDIAN PARASITES – GENERALITIES



# HEMOSPORIDIAN PARASITES – GENERALITIES



**Leucocytozoon**

26 lineages

>

**Plasmodium**

10 lineages

**Leucocytozoon**

26 lineages

>

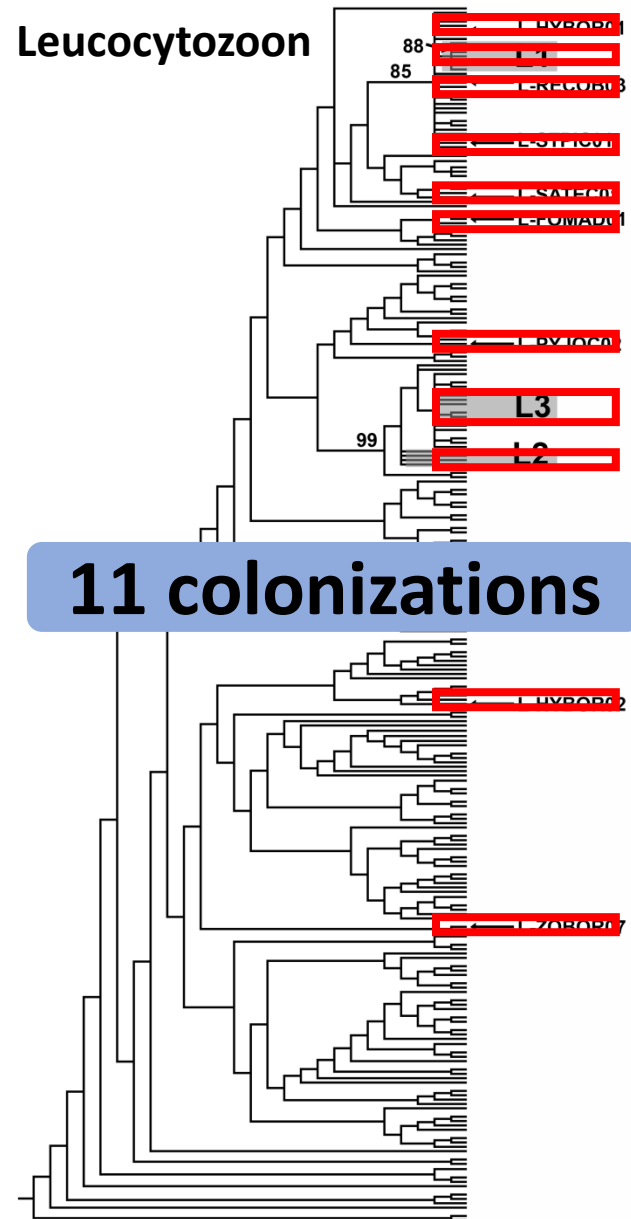
**Plasmodium**

10 lineages

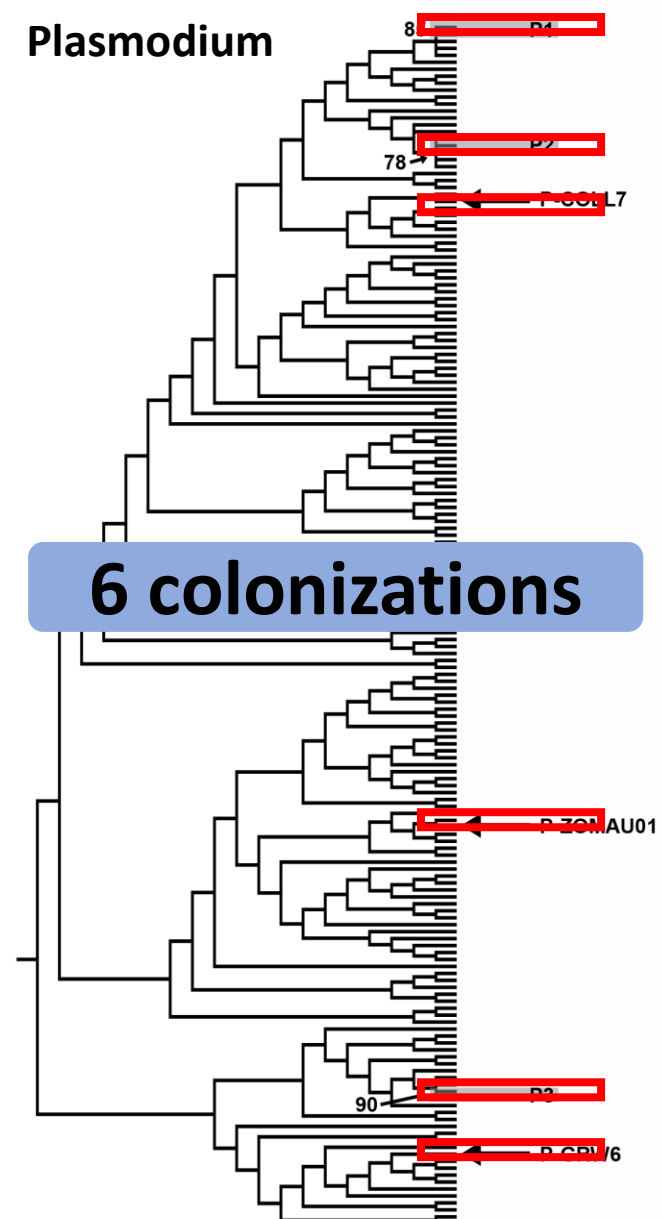
Proximal determinants of diversity:

- Number of colonizations
- Colonization time
- Diversification rate

# HEMOSPORIDIAN PARASITES – DIVERSITY IN THE MASCARENES



>



# HEMOSPORIDIAN PARASITES – DIVERSITY IN THE MASCARENES

	<b>Leucocytozoon</b>	<b>Plasmodium</b>
Colonization #	+	-
Colonization times	+	-
Diversification rate	=	=



**Greater diversity in Leucocytozoon**



# GENETIC STRUCTURE IN *PHELSUMA BORBONICA*

—

## IMPLICATIONS FOR CONSERVATION

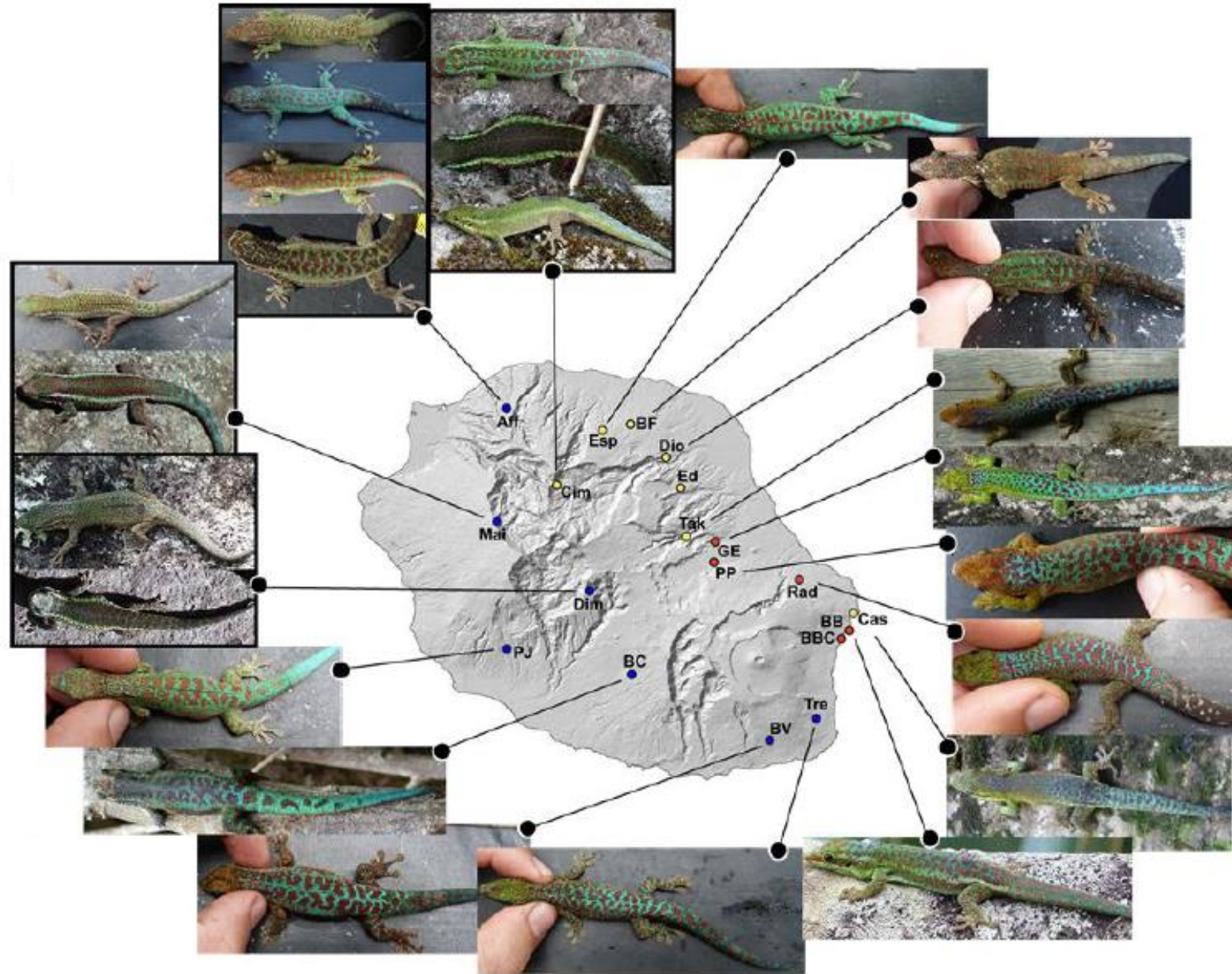
Josselin Cornuault, Mickaël Sanchez, Thomas Duval, Antoine Fouquet, Christophe Thébaud

Lab Evolution & Diversité Biologique



# *PHELSUMA BORBONICA* – GENERALITIES

- Almost endemic to Reunion island
- Endangered species (IUCN)
- Human-altered habitat
- Geographically-structured color variation





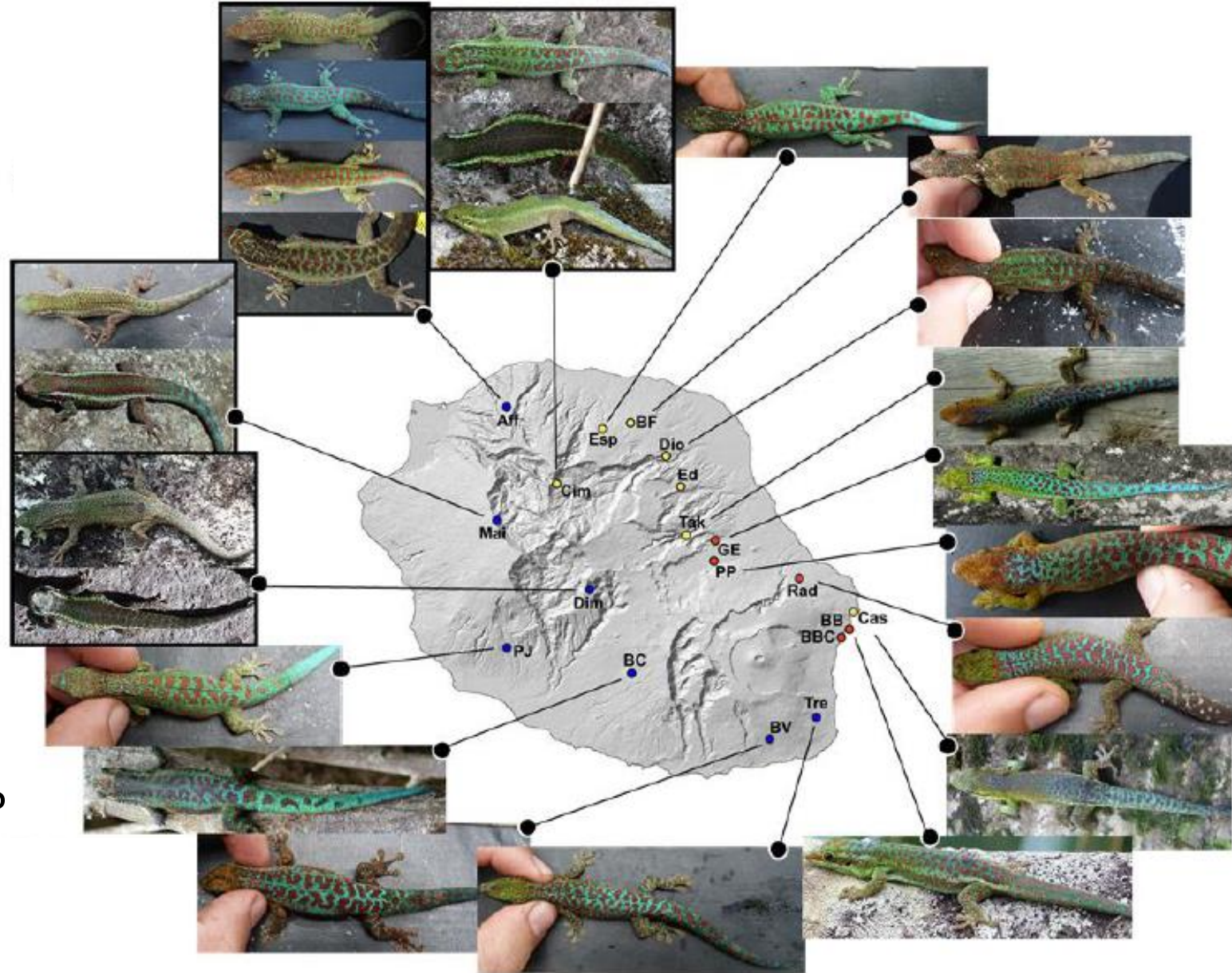
# *PHELSUMA BORBONICA* – GENERALITIES

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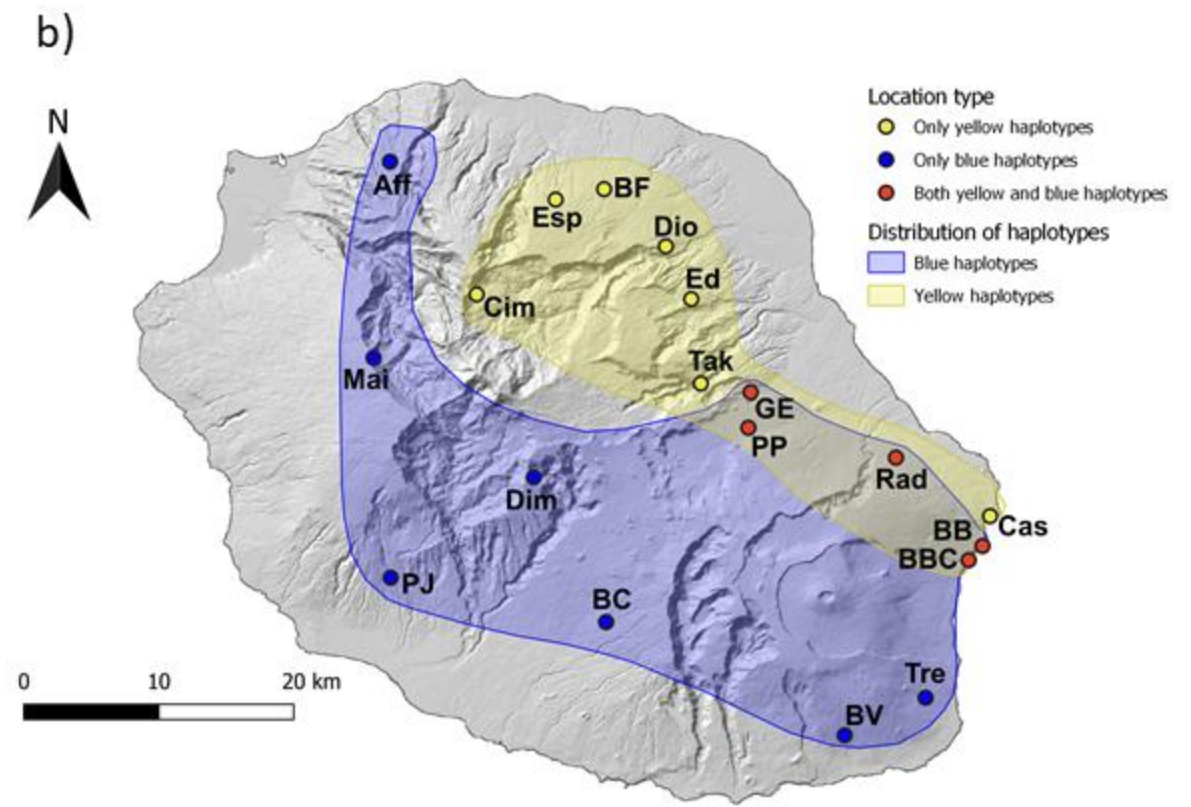
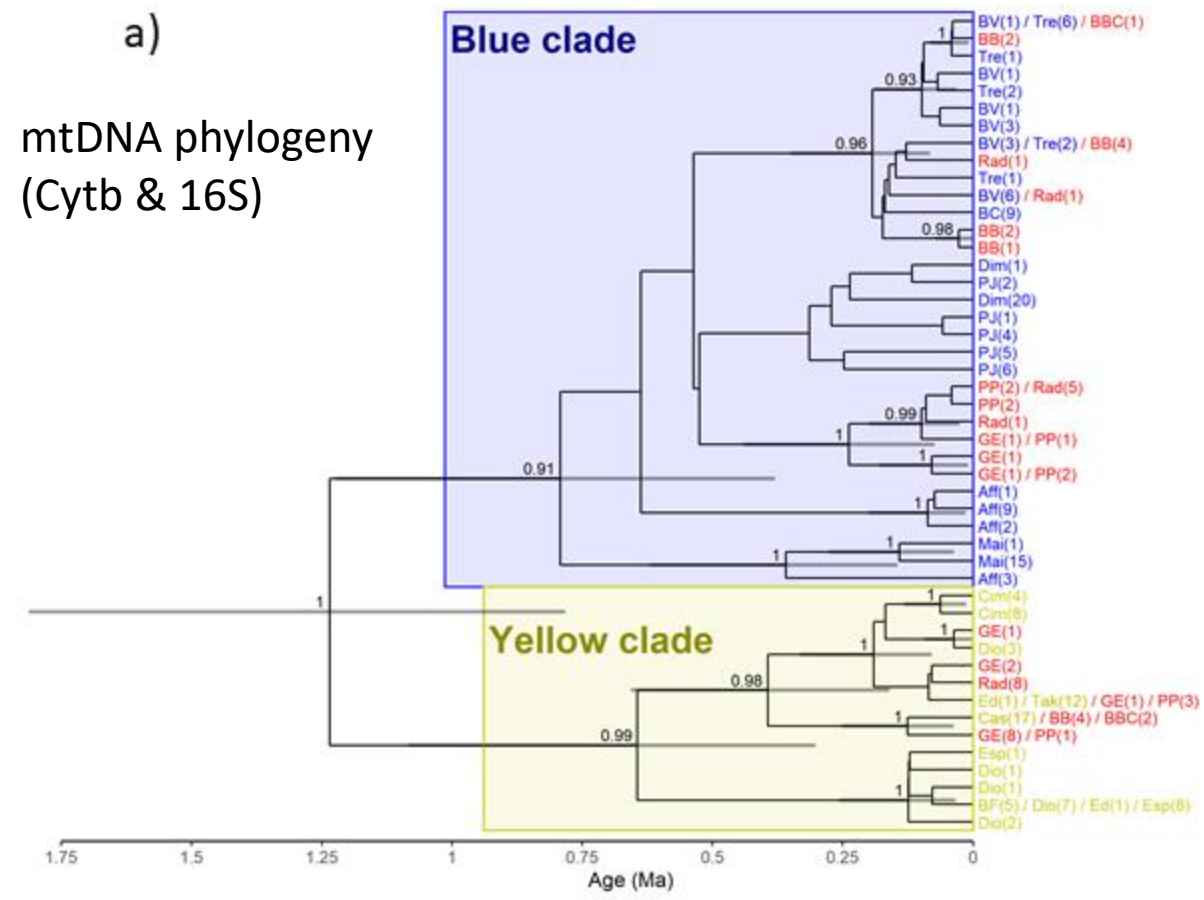


Genetic structure ?

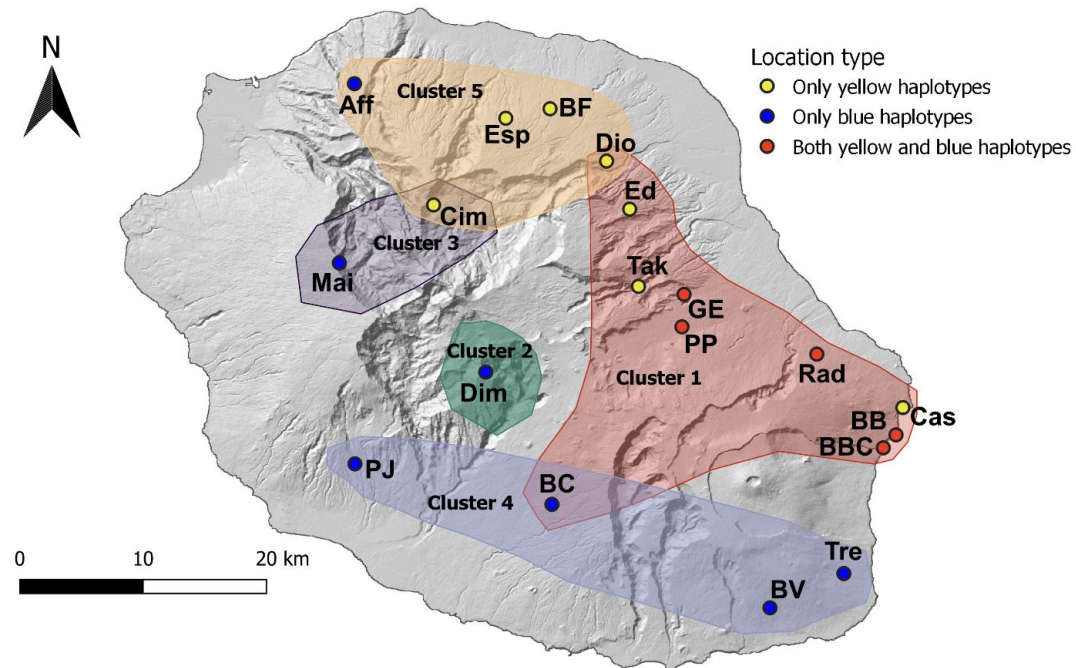
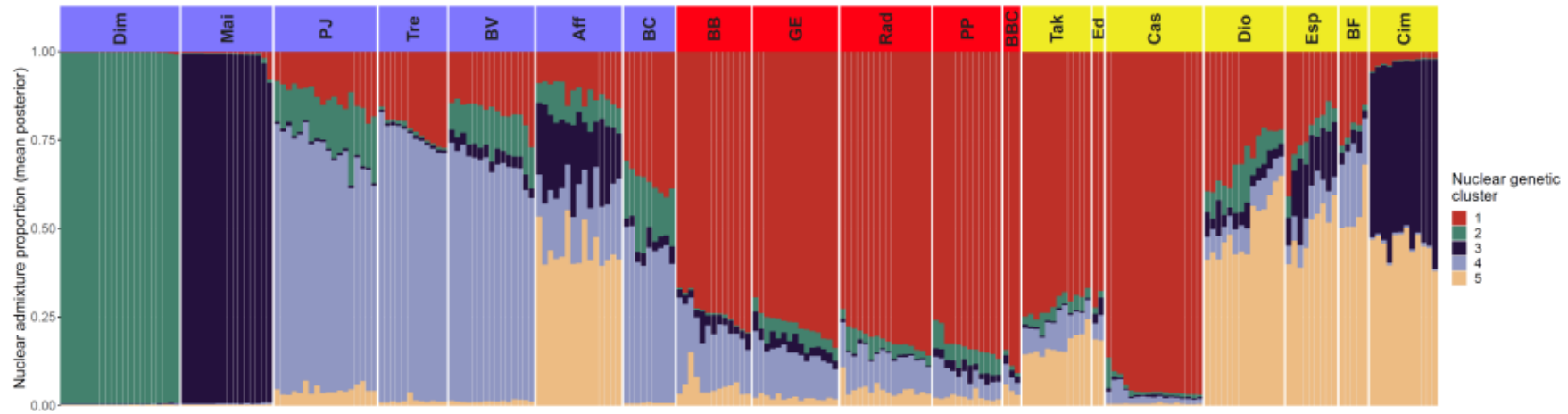
Different evolutionary significant units ?



# PHELSUMA BORBONICA – mtDNA STRUCTURE

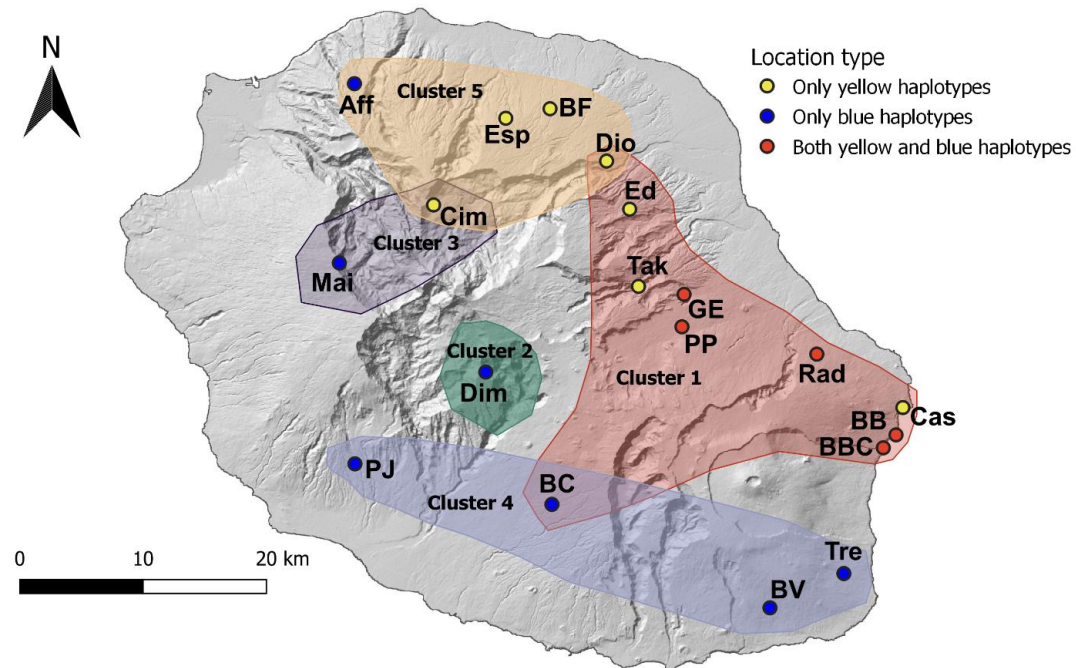
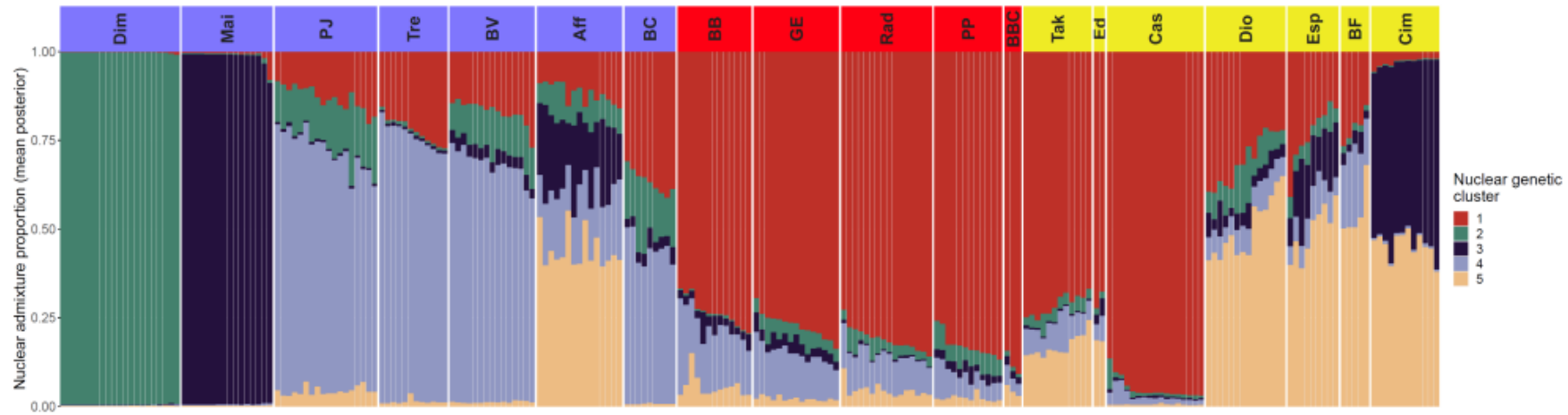


# *PHELSUMA BORBONICA* – MICROSATELLITE STRUCTURE





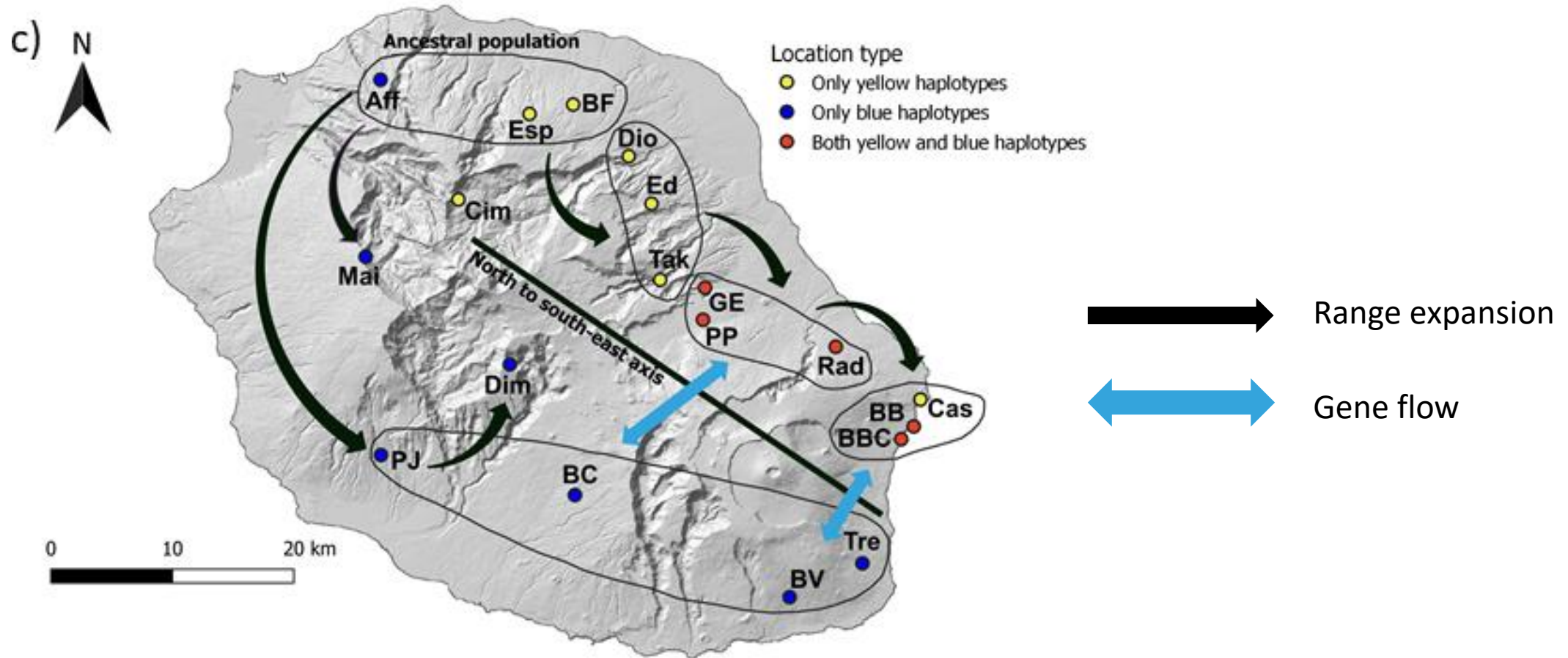
# *PHELSUMA BORBONICA* – MICROSATELLITE STRUCTURE



## High $F_{st}$ 's for some populations:

- Dimitile (Dim):  $F_{st}$ 's range from 0.38 to 0.63
- Maido (Mai):  $F_{st}$ 's range from 0.19 to 0.58

# *PHELSUMA BORBONICA* – PHYLOGEOGRAPHY



# *PHELSUMA BORBONICA* – EFFECTIVE POPULATION SIZES

Station	$N_e$ (overall) <sup>d</sup>
Aff	168 [1.0-587]
BB	136 [0.6-477]
BBC	63 [2.6-662]
BC	120 [0.7-467]
BF	277 [13.1-842]
BV	125 [1.4-396]
Cas	106 [12.8-329]
Cim	77 [0.0-276]
Dim	22 [0.5-79]
Dio	189 [19.9-562]
Ed	219 [6.0-40997]
Esp	140 [0.1-567]
GE	109 [0.0-407]
Mai	59 [0.0-178]
PJ	122 [13.1-342]
PP	124 [13.8-396]
Rad	140 [0.1-500]
Tak	105 [0.0-377]
Tre	110 [0.0-358]



- Long-lasting isolation of populations (especially montane populations)
- Small effective sizes (especially for montane populations)
  - ➡ **Take account of evolutionary history** in conservation practices (various ESUs)
  - ➡ Especially for **montane populations**

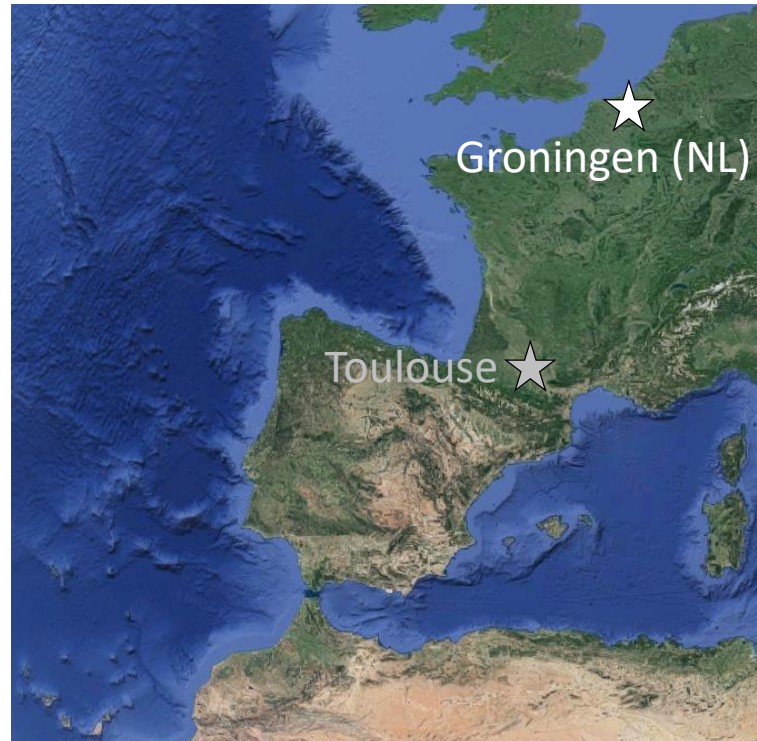
# CO-PHYLOGENY

—

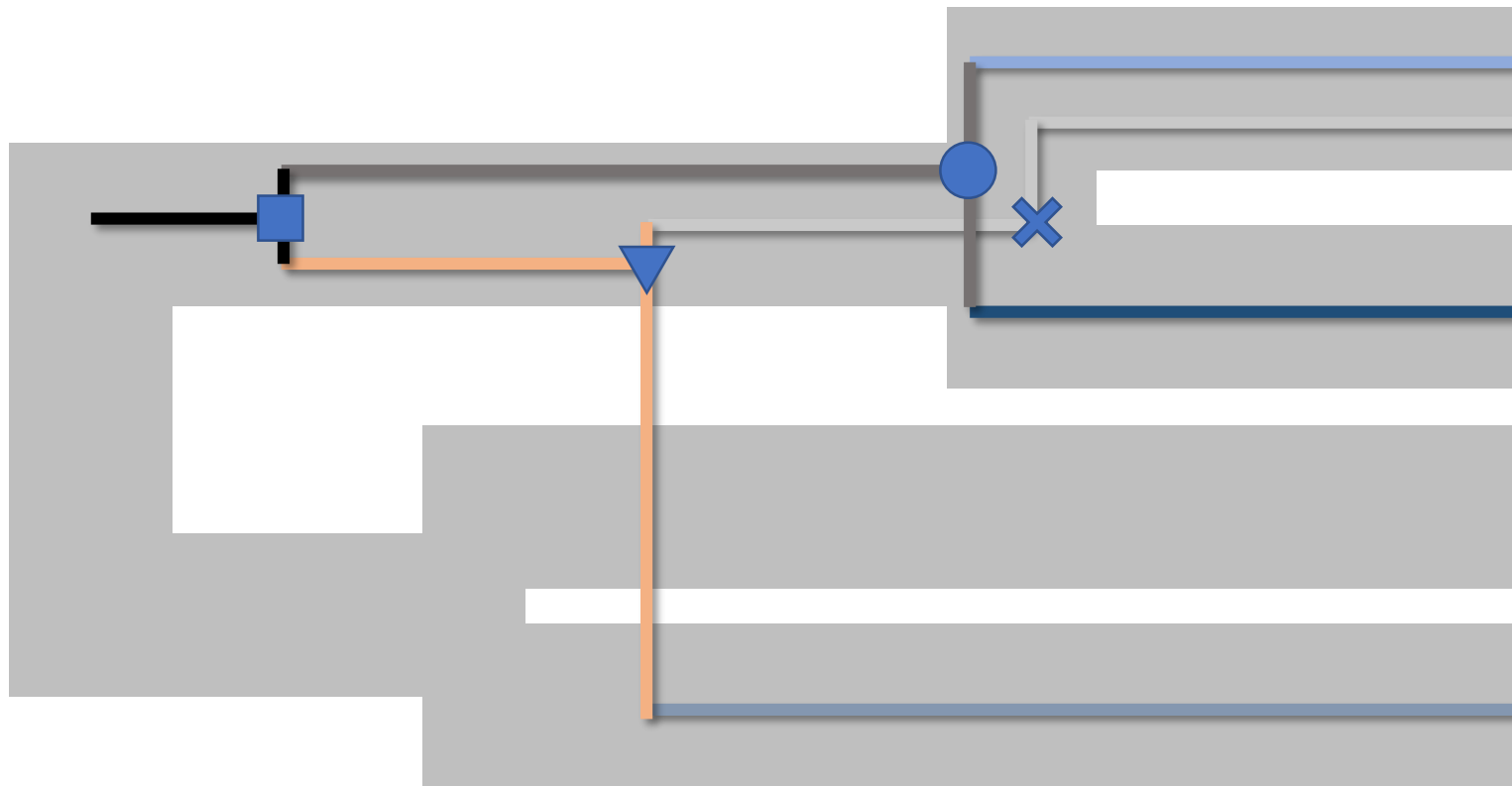
## A LIKELIHOOD-BASED APPROACH

Josselin Cornuault, Rampal Etienne

Lab GELIFES (Univ. Groningen)



# CO-PHYLOGENY – EVENTS

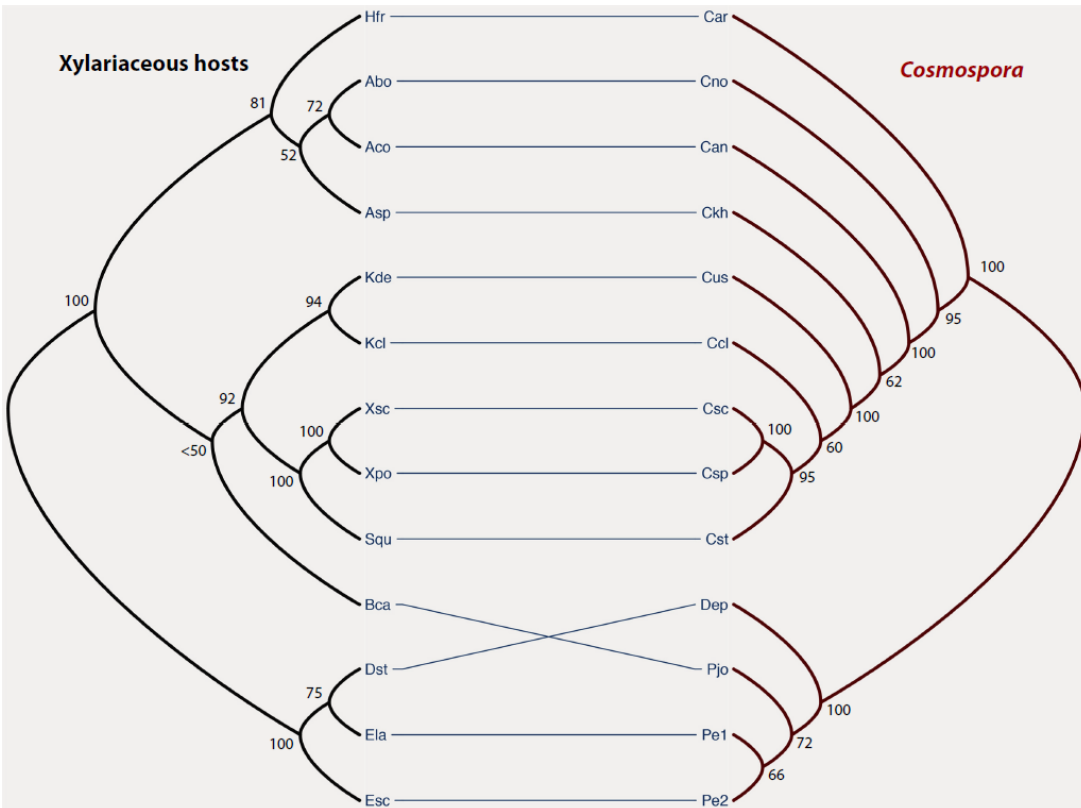


Host  
Parasite

- Cospeciation
- Duplication
- ✕ Loss
- ▼ Host switch

# CO-PHYLOGENY – RECONCILIATION ANALYSIS

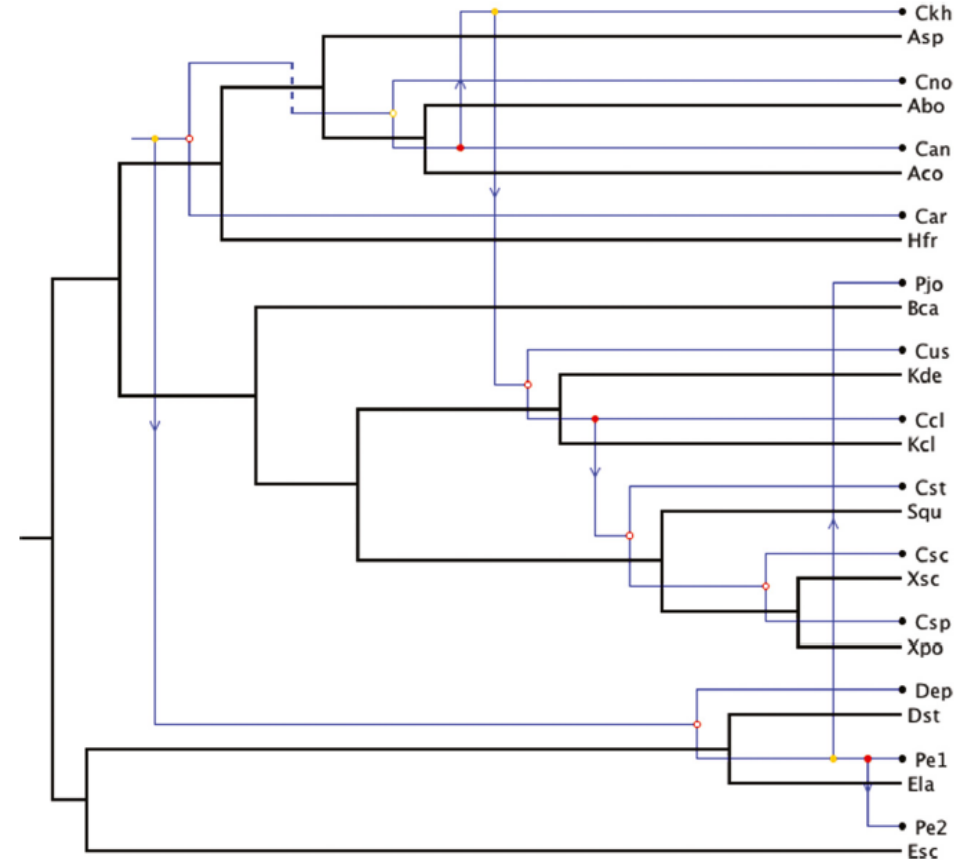
## Tanglegram



Maximum  
parsimony



## Reconciliation

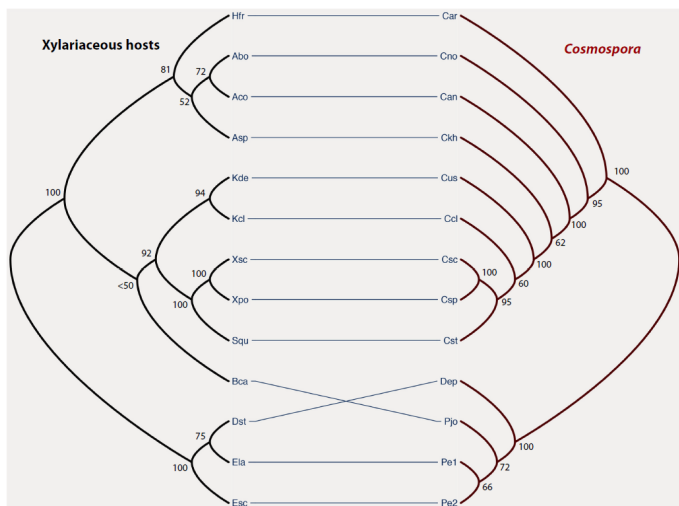


Most parsimonious reconciliation(s):

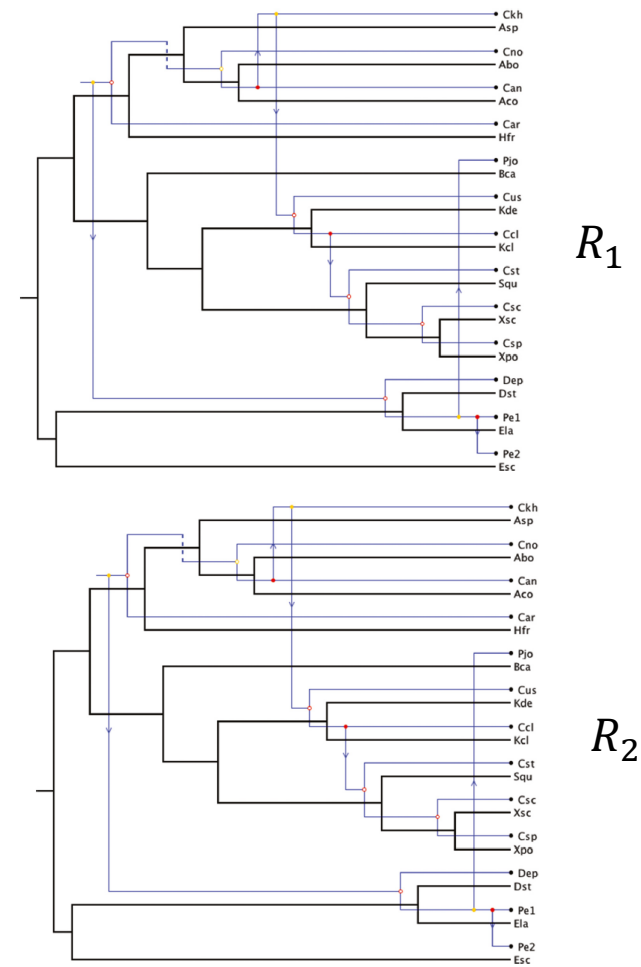
- No quantification of uncertainty
- No hypothesis testing

# CO-PHYLOGENY – LIKELIHOOD-BASED ANALYSIS

Tanglegram ( $T$ )



Reconciliations



$$P(T | R_1, \theta)$$

$$P(T | R_2, \theta)$$

Parameters:

$$\theta = \{d, s, l\}$$

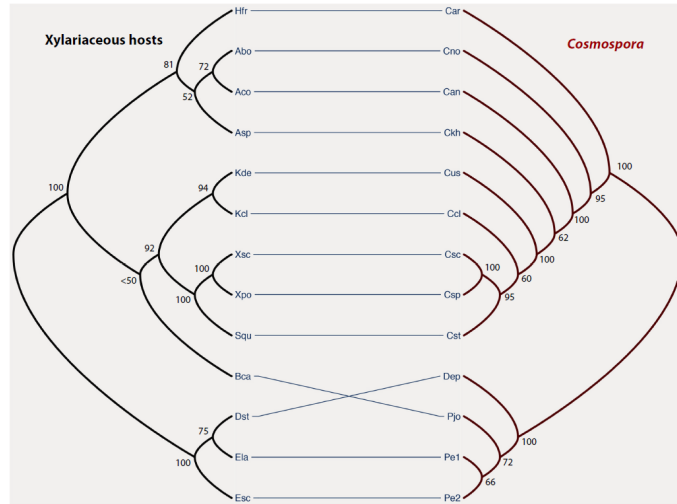
$d$  = duplication rate

$s$  = host-switch rate

$l$  = loss rate

# CO-PHYLOGENY – LIKELIHOOD-BASED ANALYSIS

Tanglegram ( $T$ )



$$P(T|\theta) = \sum_i P(T | R_i, \theta)$$

← Reconciliations are marginalized out

Parameters:

$$\theta = \{d, s, l\}$$

$d$  = duplication rate

$s$  = host-switch rate

$l$  = loss rate

Marginal likelihood approach:

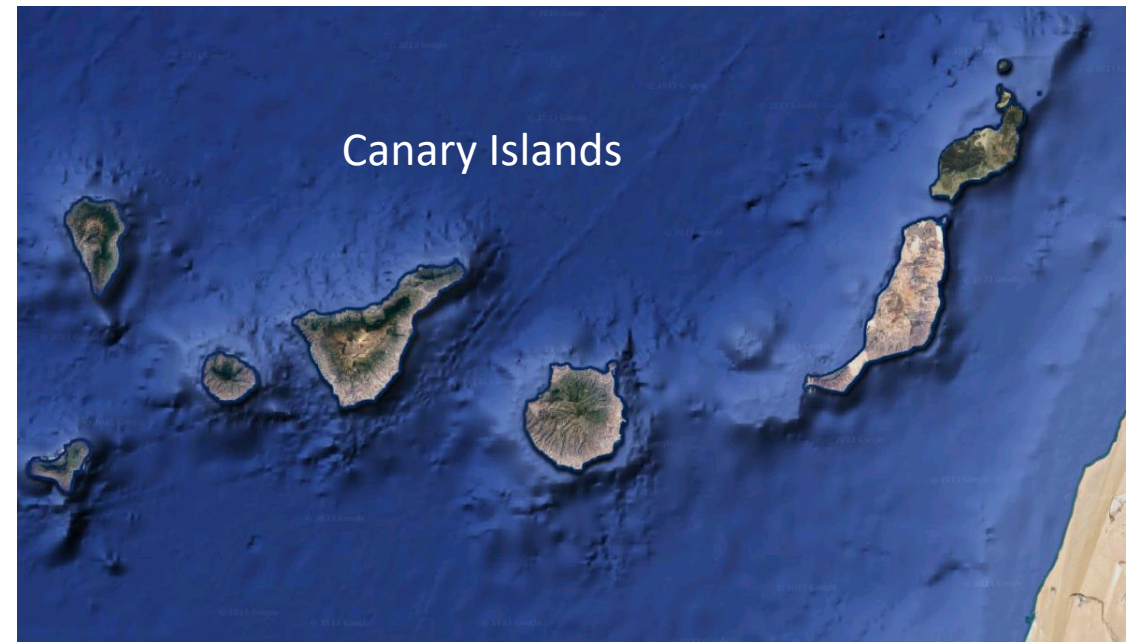
- Focus on estimating evolutionary rates (not reconciliations)
- Uncertainty quantified
- Hypothesis testing possible
- Multiple hosts per parasites and multiple parasites per hosts
- Current drawbacks:
  - Co-speciation not included
  - Hardly computable for more than 10 hosts

# STRUCTURED COALESCENT

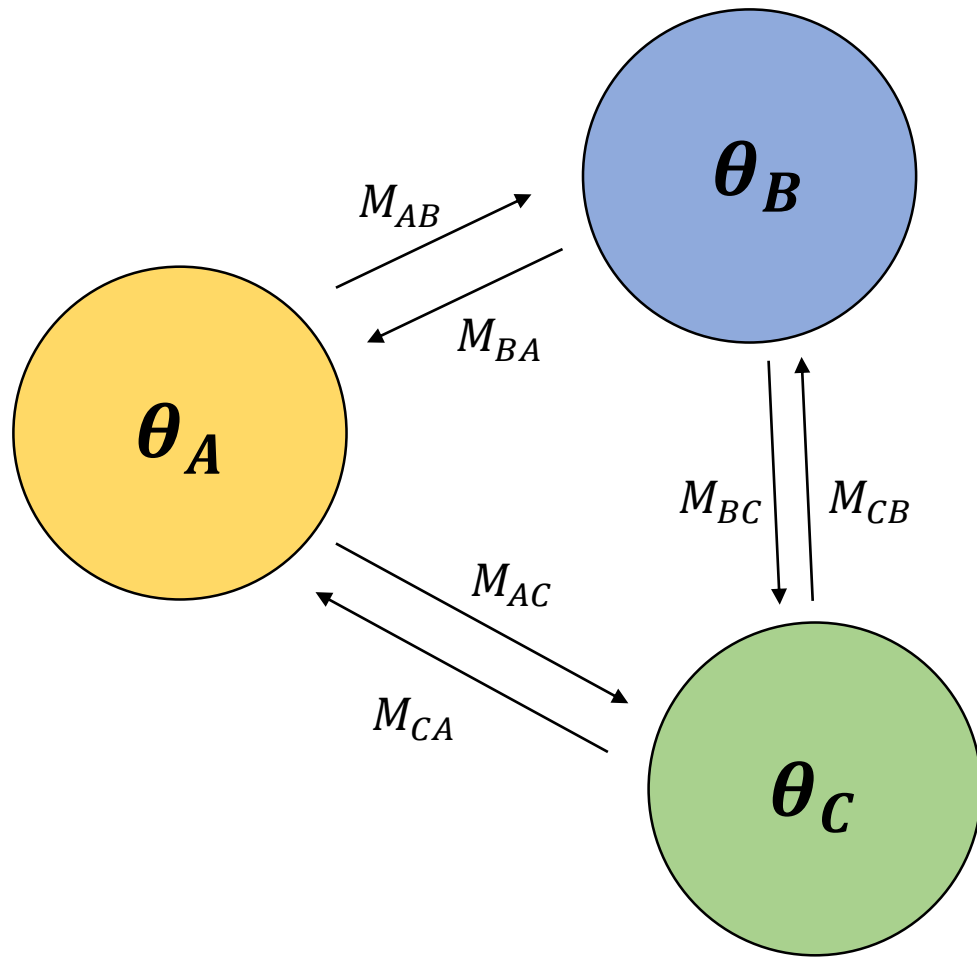
Josselin Cornuault, Antonia Salces Castellano, Brent Emerson, Isabel Sanmartin

Real jardin Botánico – CSIC – Madrid

Island Ecology and Evolution – IPNA/CSIC – Tenerife



# STRUCTURED COALESCENT – GENERALITIES

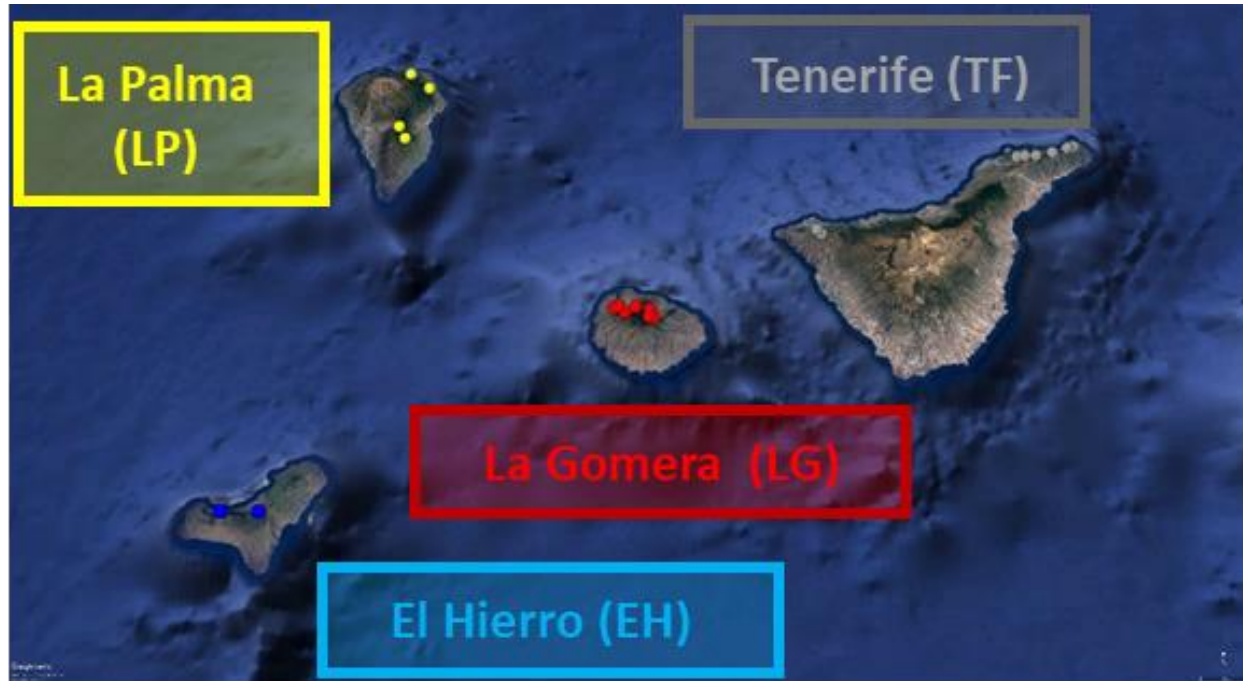


Coalescent model extended to multiple populations:

- Own effective population sizes ( $\theta_A, \theta_B \dots$ )
- Migration rates ( $M_{AB}, M_{BC} \dots$ )



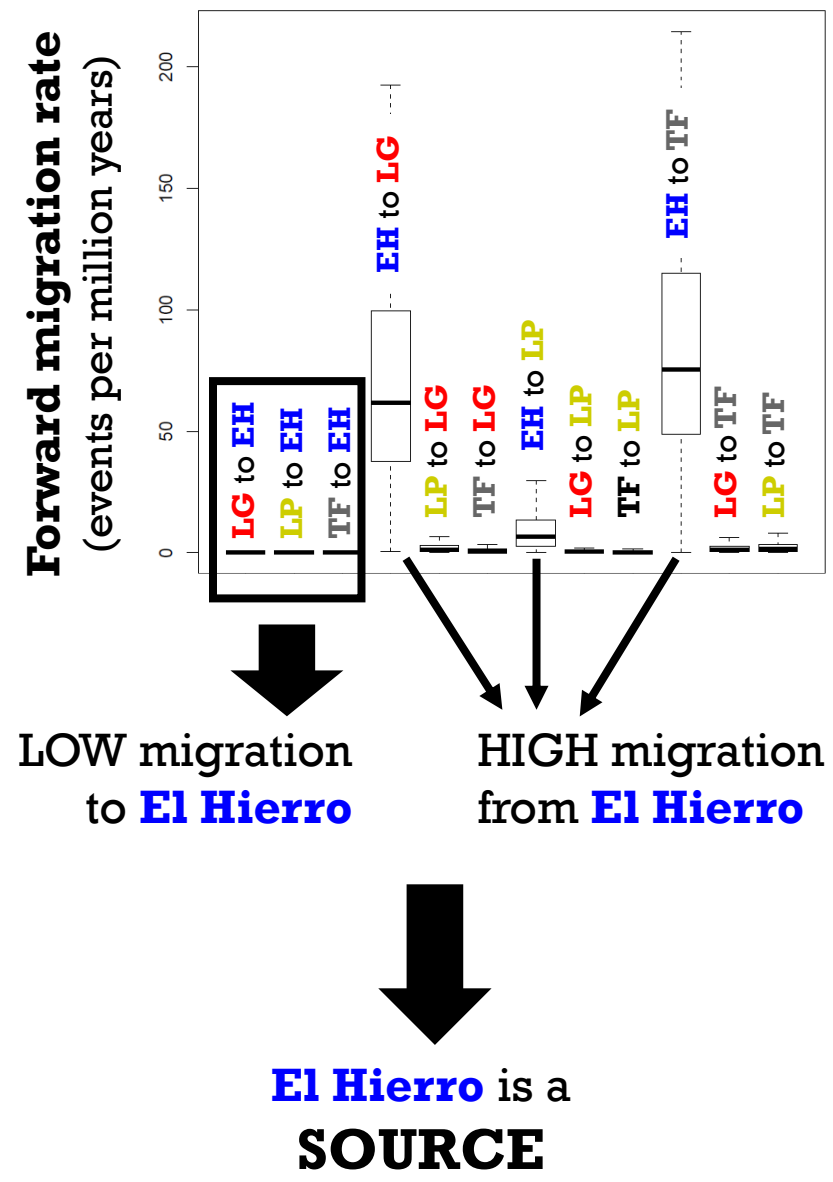
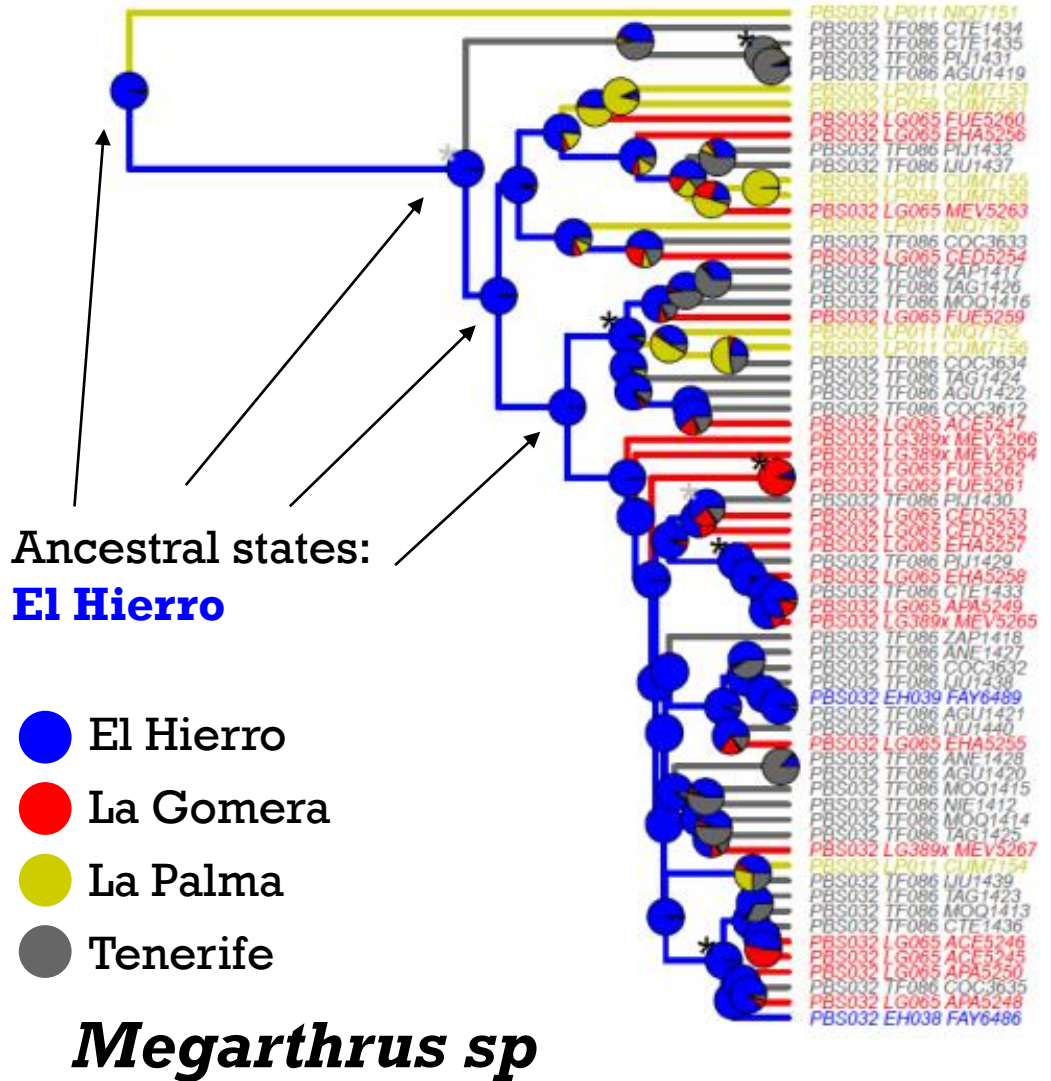
# STRUCTURED COALESCENT – CANARY ISLANDS



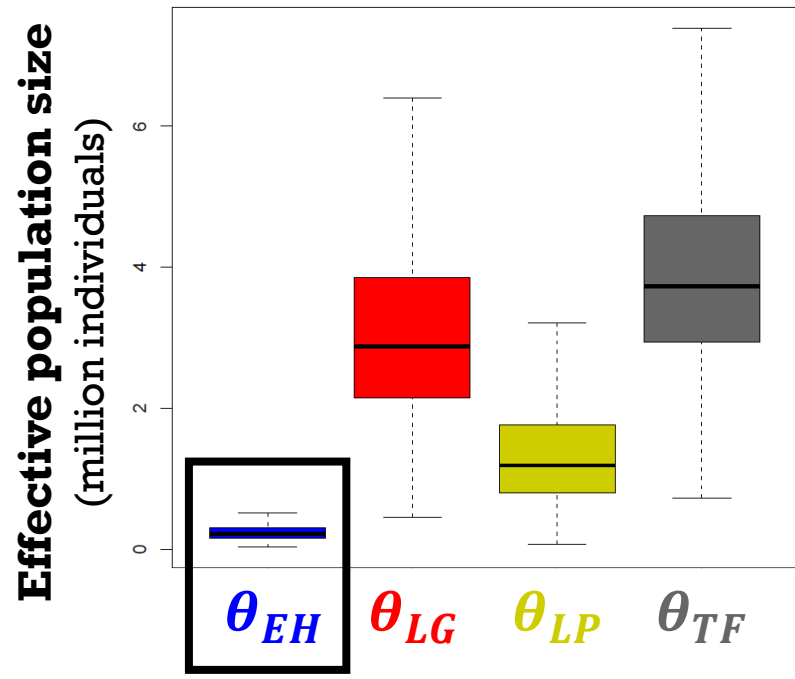
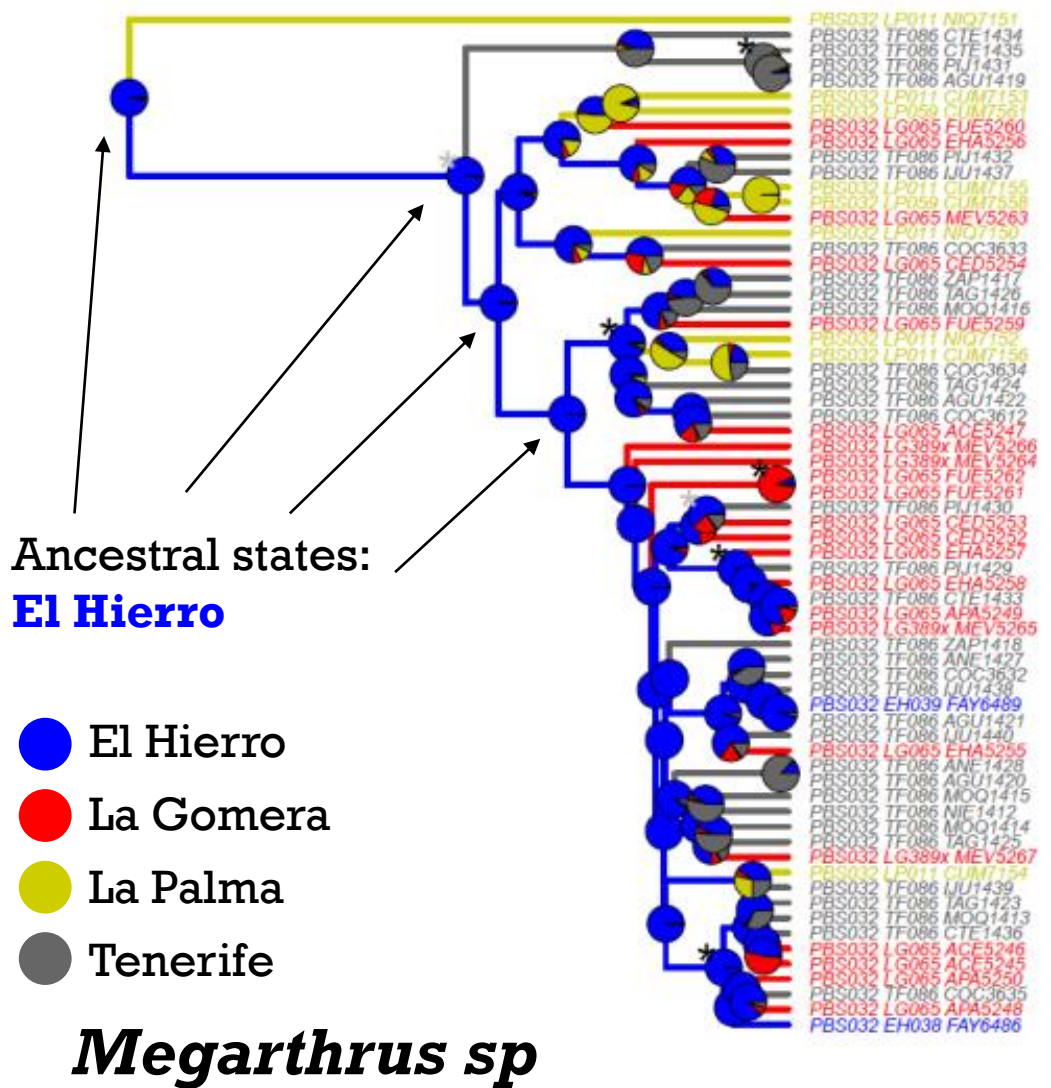
Genetic data for 200 Coleopteran species

- ➔ Estimate migration rates among islands for each species
- ➔ Determine main migration routes

# STRUCTURED COALESCENT – NONSENSICAL RESULTS



# STRUCTURED COALESCENT – NONSENSICAL RESULTS



**LOWER  $\theta_{EH}$  (El Hierro population size)**

Multimodal likelihood function (as many modes as there are populations)

- ➔ Possible to get the MCMC to get stuck in any of the following modes:
- 1) **El Hierro (EH) mode**: Ancestral locations = EH, low population size for EH, EH source of migration
  - 2) **La Gomera (LG) mode**: Ancestral locations = LG, low population size for LG, LG source of migration
  - 3) **Tenerife mode**: idem
  - 4) **La Palma mode**: idem

What type of datasets is more prone to the problem?

Can the problem be solved by using appropriate priors?

Is the model mathematically correctly defined?

# PHYLODYNAMICS — PHYLOGENETIC EPIDEMIOLOGY

Josselin Cornuault, Fabio Pardi, Celine Scornavacca

ISEM Montpellier



**1) Birth-Death-Sampling (BDS) model**

**2) Kingman coalescent model**

**a) Skyline approach**

**b) Mechanistic approach**

**1) Birth-Death-Sampling (BDS) model**

## 1) Birth-Death-Sampling (BDS) model

### Parameters:

- $\lambda(t)$  (transmission rate)
- $\mu(t)$  (loss rate)
- $\psi(t)$  (sampling rate)

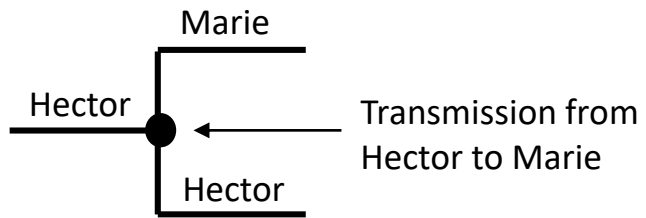


## 1) Birth-Death-Sampling (BDS) model

### Parameters:

- $\lambda(t)$  (transmission rate)
- $\mu(t)$  (loss rate)
- $\psi(t)$  (sampling rate)

Transmissions occur at rate  $\lambda(t)$

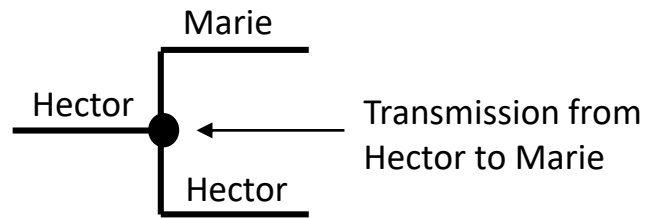


## 1) Birth-Death-Sampling (BDS) model

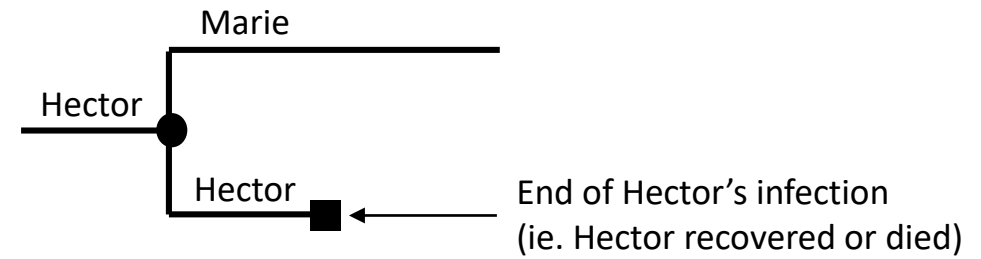
Parameters:

- $\lambda(t)$  (transmission rate)
- $\mu(t)$  (loss rate)
- $\psi(t)$  (sampling rate)

Transmissions occur at rate  $\lambda(t)$



Infections are lost at rate  $\mu(t)$

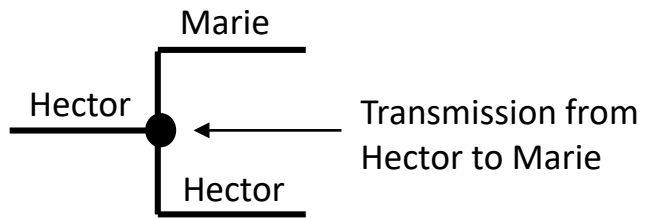


## 1) Birth-Death-Sampling (BDS) model

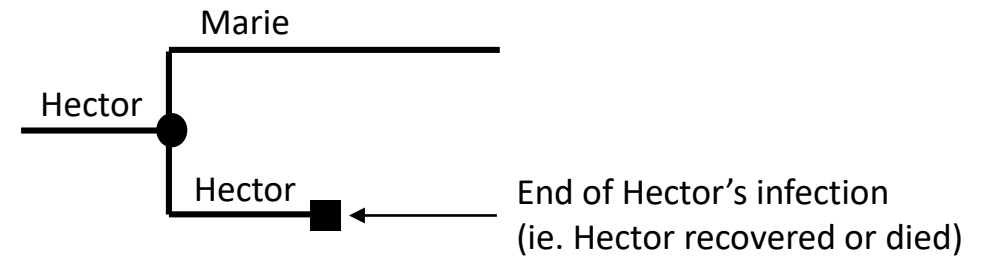
### Parameters:

- $\lambda(t)$  (transmission rate)
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- $\psi(t)$  (sampling rate)

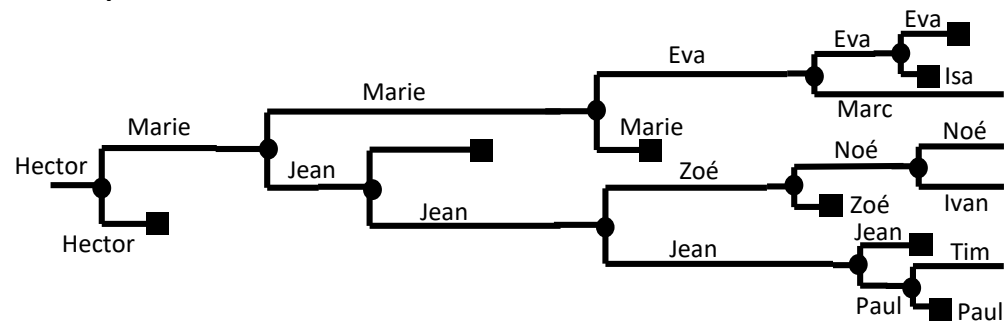
Transmissions occur at rate  $\lambda(t)$



Infections are lost at rate  $\mu(t)$



Complete transmission tree

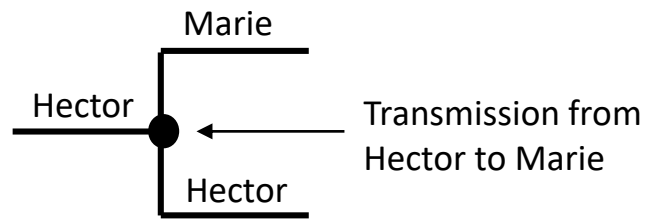


## 1) Birth-Death-Sampling (BDS) model

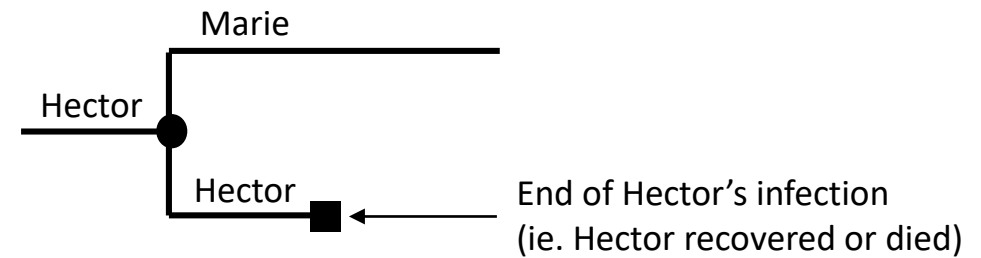
Parameters:

- $\lambda(t)$  (transmission rate)
- $\mu(t)$  (loss rate)
- $\psi(t)$  (sampling rate)

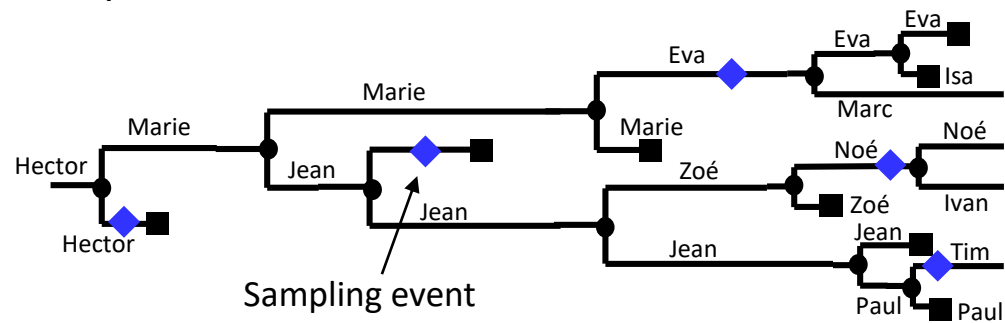
Transmissions occur at rate  $\lambda(t)$



Infections are lost at rate  $\mu(t)$



Complete transmission tree



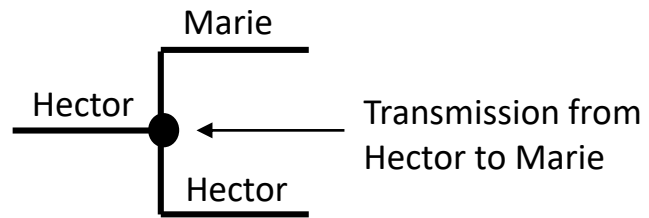
Sampling events occur at rate  $\psi(t)$

## 1) Birth-Death-Sampling (BDS) model

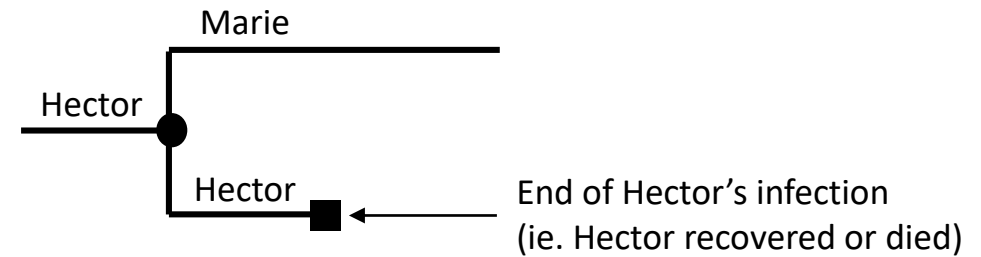
### Parameters:

- $\lambda(t)$  (transmission rate)
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- $\psi(t)$  (sampling rate)

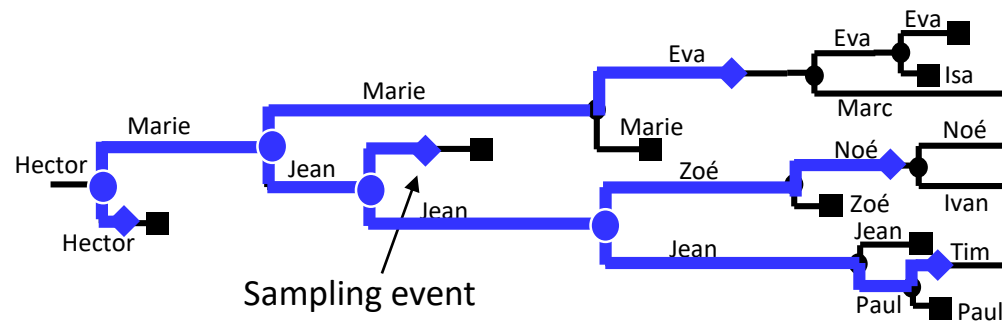
Transmissions occur at rate  $\lambda(t)$



Infections are lost at rate  $\mu(t)$



Complete transmission tree



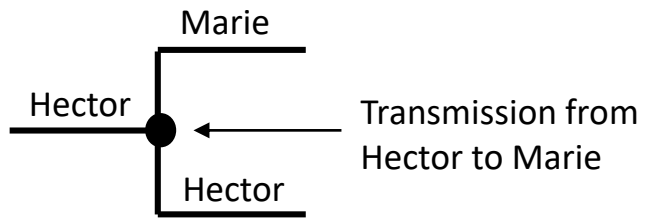
Sampling events occur at rate  $\psi(t)$

## 1) Birth-Death-Sampling (BDS) model

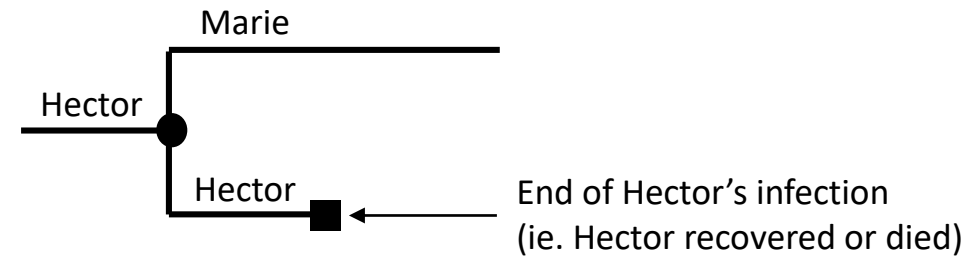
Parameters:

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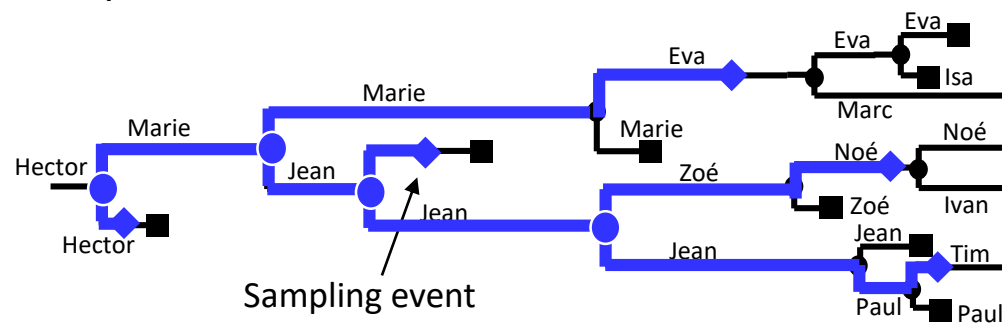
Transmissions occur at rate  $\lambda(t)$



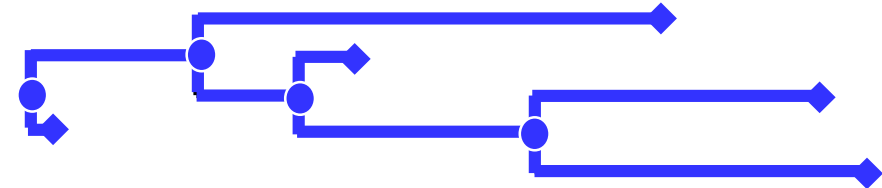
Infections are lost at rate  $\mu(t)$



Complete transmission tree



Sampled transmission tree



Sampling events occur at rate  $\psi(t)$



## 1) Birth-Death-Sampling (BDS) model

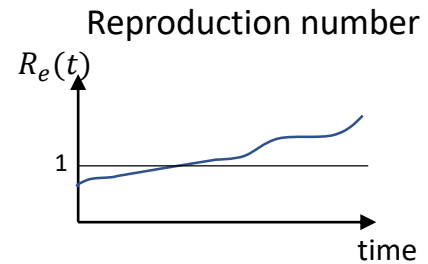
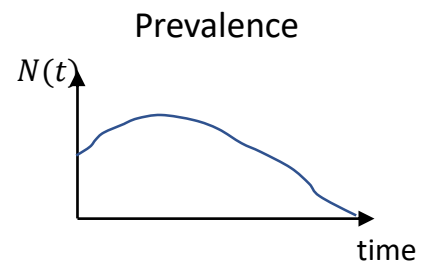
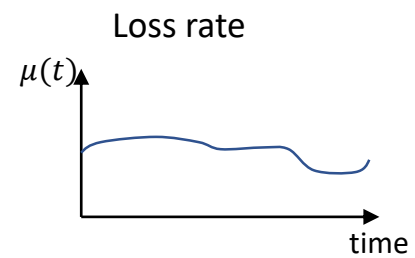
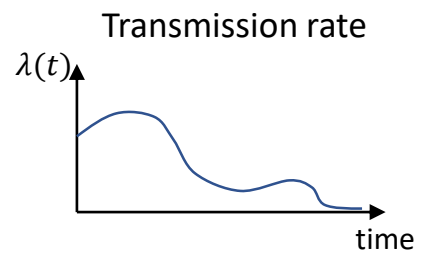
Advantages

Drawbacks

## 1) Birth-Death-Sampling (BDS) model

### Advantages

- Interesting epidemiological parameters can be estimated:

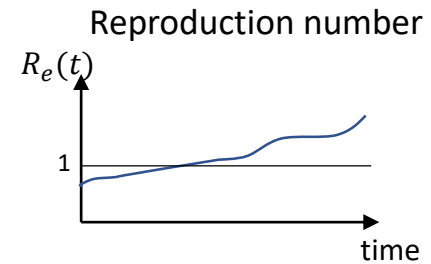
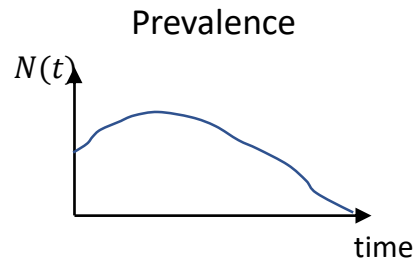
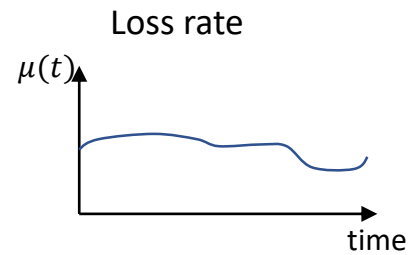
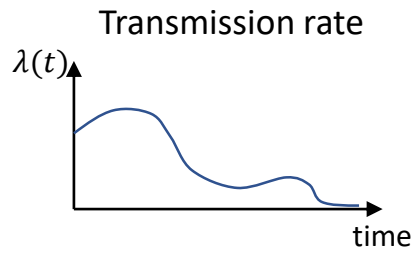


### Drawbacks

## 1) Birth-Death-Sampling (BDS) model

### Advantages

- Interesting epidemiological parameters can be estimated:



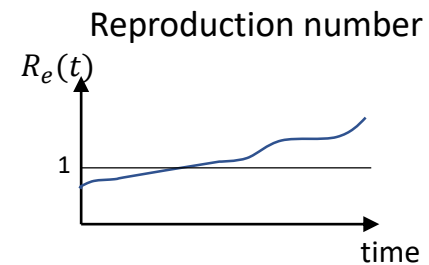
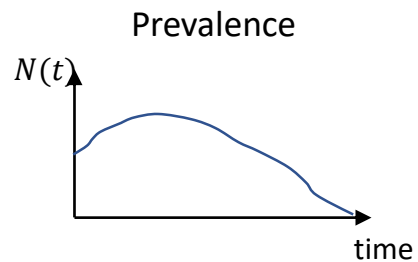
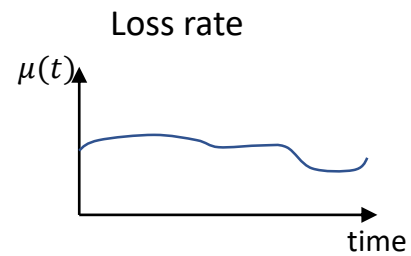
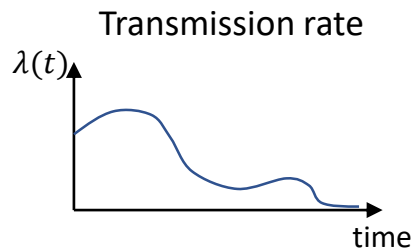
### Drawbacks

- Sampling procedure needs to be assumed ( $\psi(t)$ )

## 1) Birth-Death-Sampling (BDS) model

### Advantages

- Interesting epidemiological parameters can be estimated:



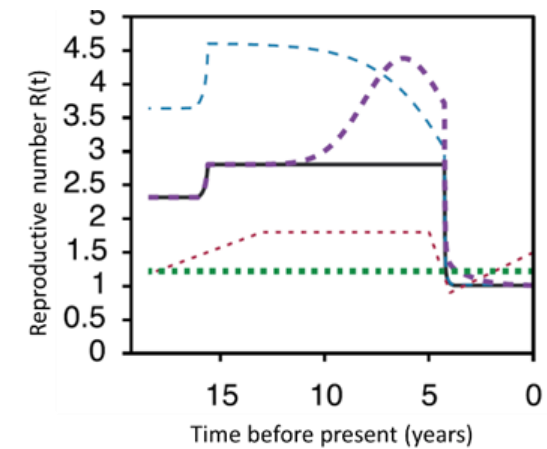
### Drawbacks

- Sampling procedure needs to be assumed ( $\psi(t)$ )

- Parameters are not identifiable

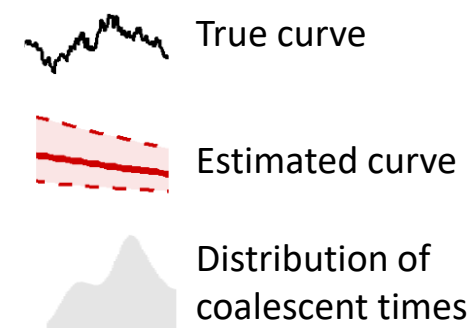
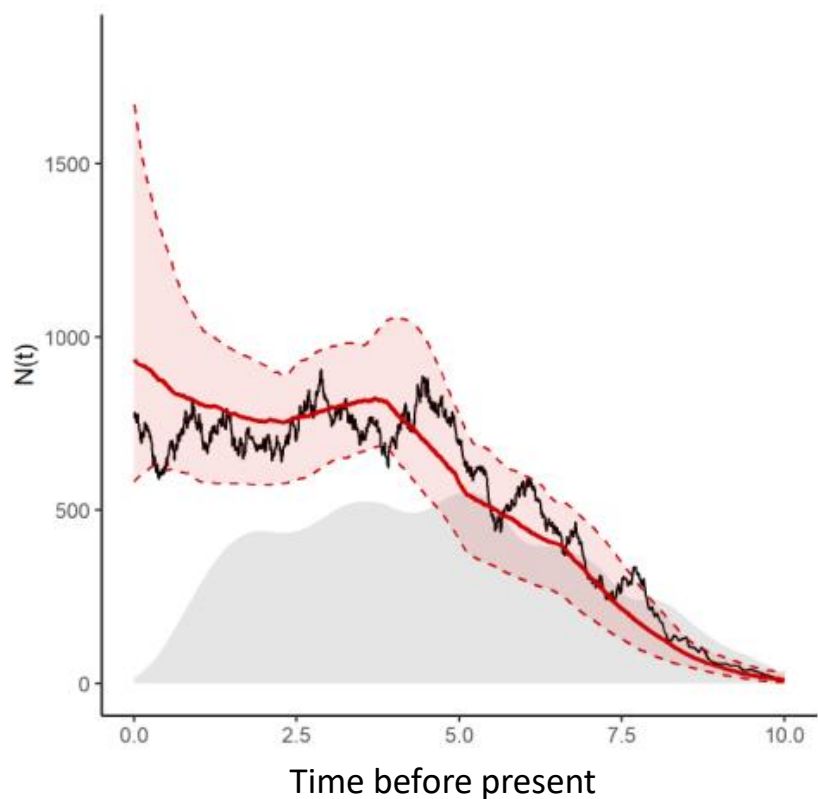
#### Fundamental Identifiability Limits in Molecular Epidemiology

Stilianos Louca<sup>\*,1,2</sup> Angela McLaughlin,<sup>3,4</sup> Ailene MacPherson,<sup>5,6,7</sup> Jeffrey B. Joy,<sup>3,4,8</sup> and Matthew W. Pennell<sup>\*,5,6</sup>



## 1) Birth-Death-Sampling (BDS) model

BDS inference with correct  $\psi(t)$

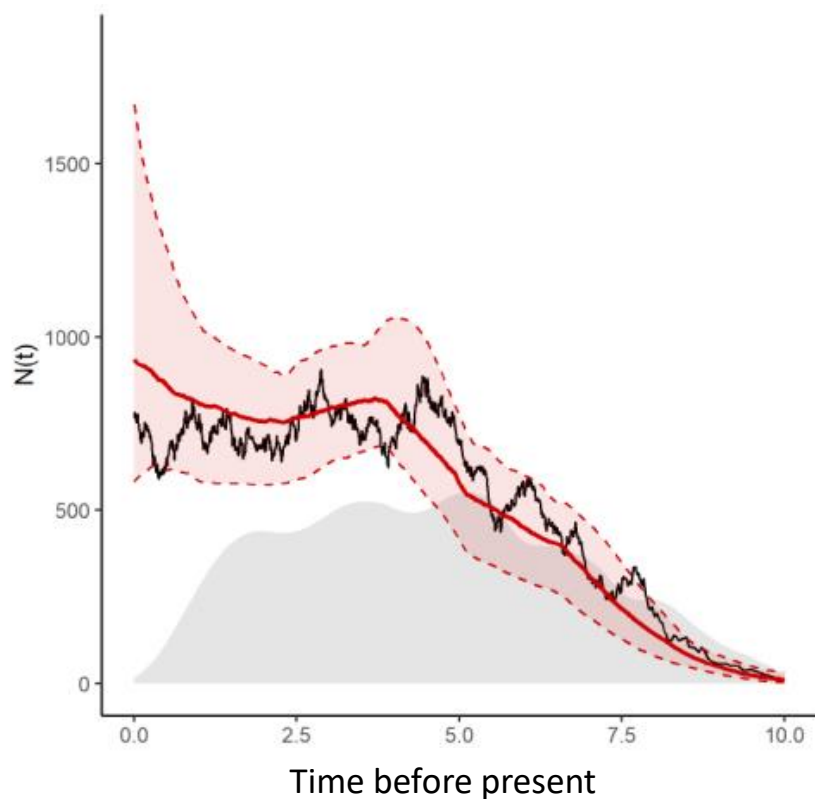


Simulation:  $\psi(t) = \psi$

Inference:  $\psi(t) = \psi$

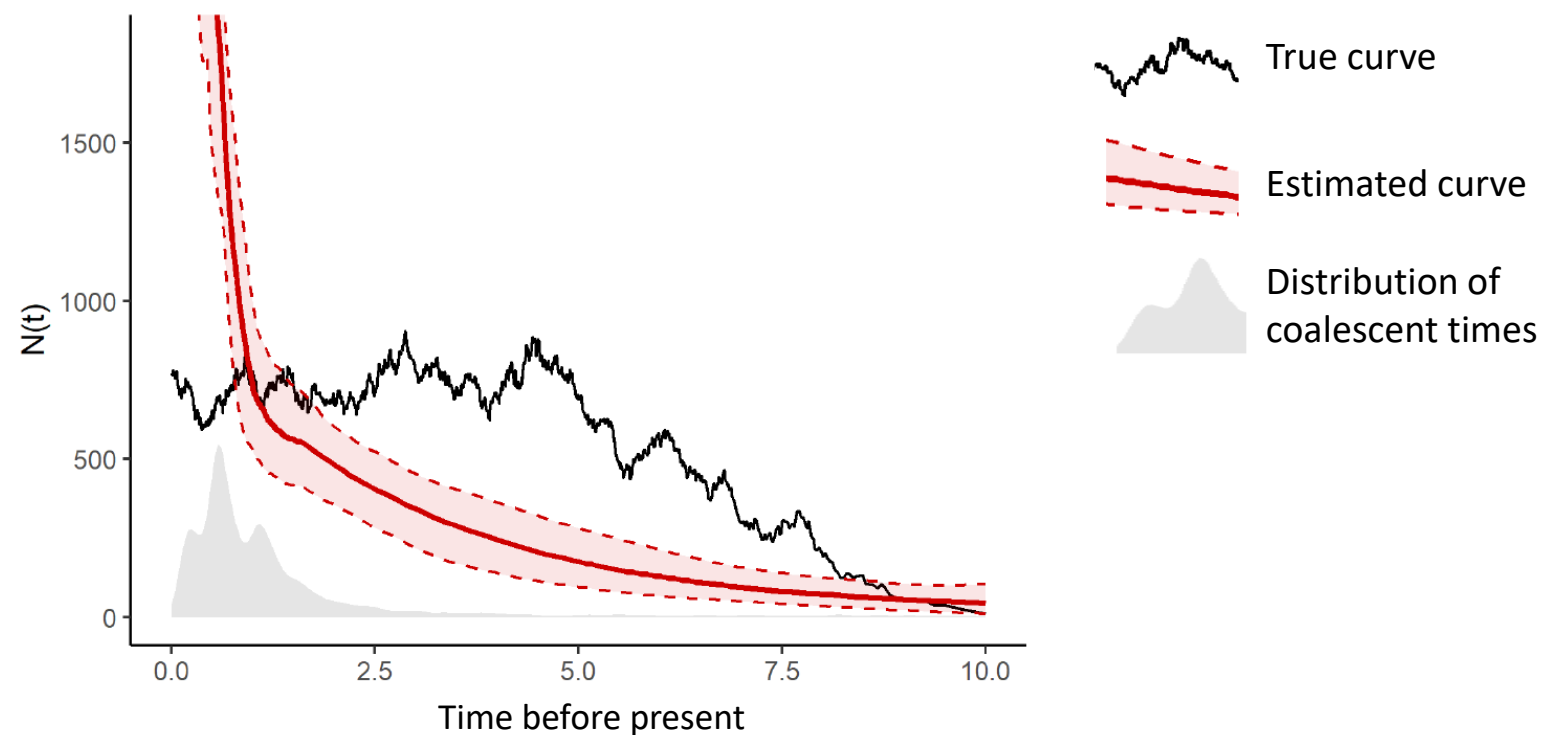
## 1) Birth-Death-Sampling (BDS) model

BDS inference with correct  $\psi(t)$



Simulation:  $\psi(t) = \psi$   
Inference:  $\psi(t) = \psi$

BDS inference with incorrect  $\psi(t)$



Simulation:  $\psi(t) \neq \psi$   
Inference:  $\psi(t) = \psi$



## 2) Kingman Coalescent (KC) model

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Parameters:

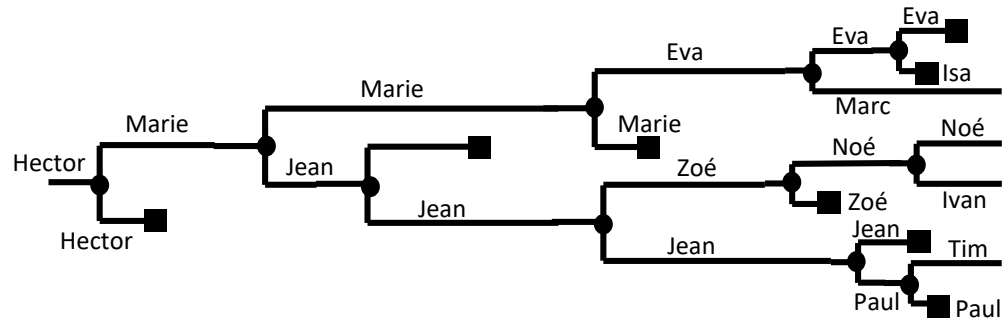
- $\theta(t)$  (instantaneous effective population size)

## 2) Kingman Coalescent (KC) model

### Parameters:

- $\theta(t)$  (instantaneous effective population size)

### Complete transmission tree



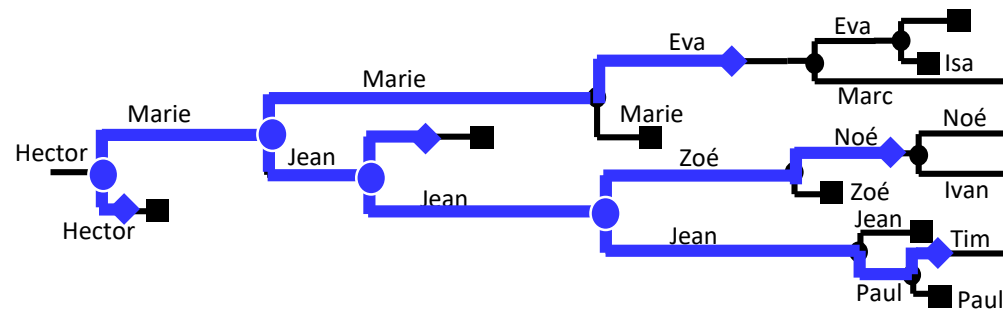
- Few assumptions about the model that generated the complete transmission tree

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### Complete transmission tree



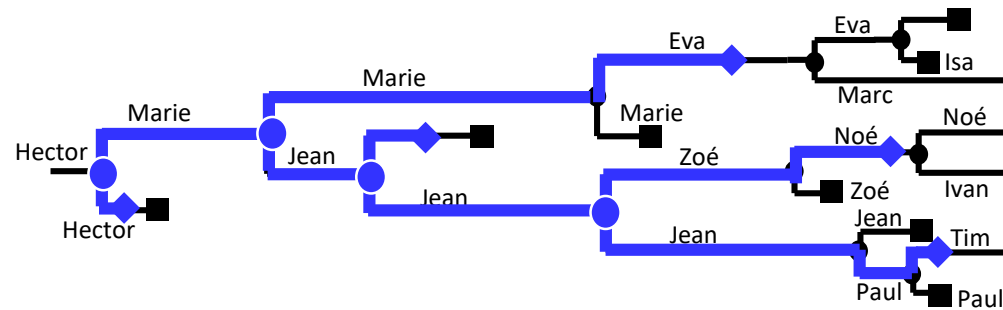
- Few assumptions about the model that generated the complete transmission tree
- No assumptions about the sampling procedure

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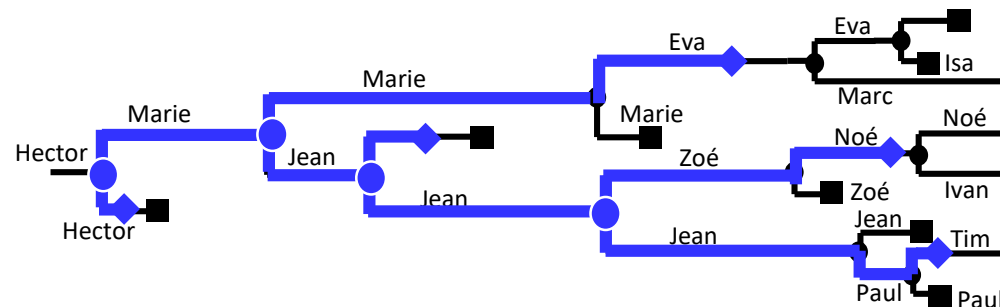
Coalescence of two lineages occurs at rate  $\frac{1}{\theta(t)}$

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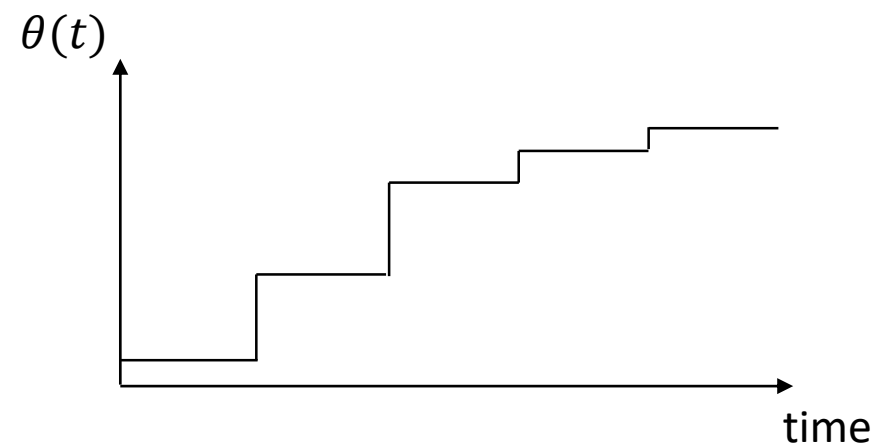
Coalescence of two lineages occurs at rate  $\frac{1}{\theta(t)}$

Two approaches for parametrizing  $\theta(t)$ :

- Skyline approach
- Mechanistic approach

## 2) Kingman Coalescent (KC) model

### a) Skyline approach

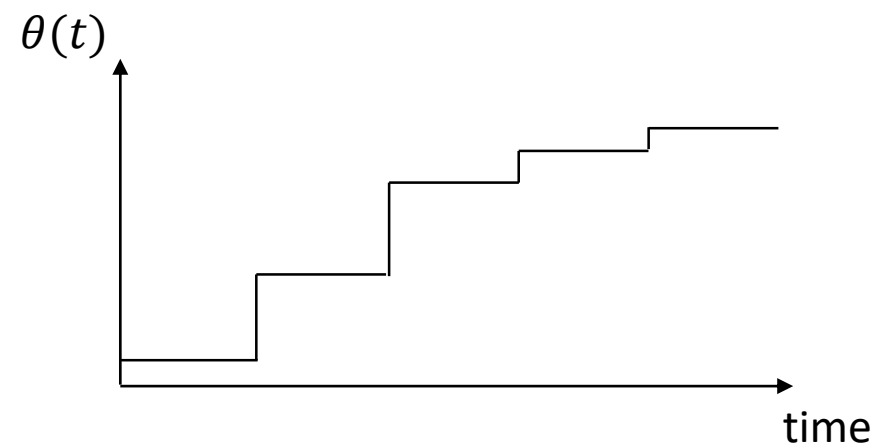


$\theta(t)$  is represented phenomenologically by a piecewise function



## 2) Kingman Coalescent (KC) model

### a) Skyline approach



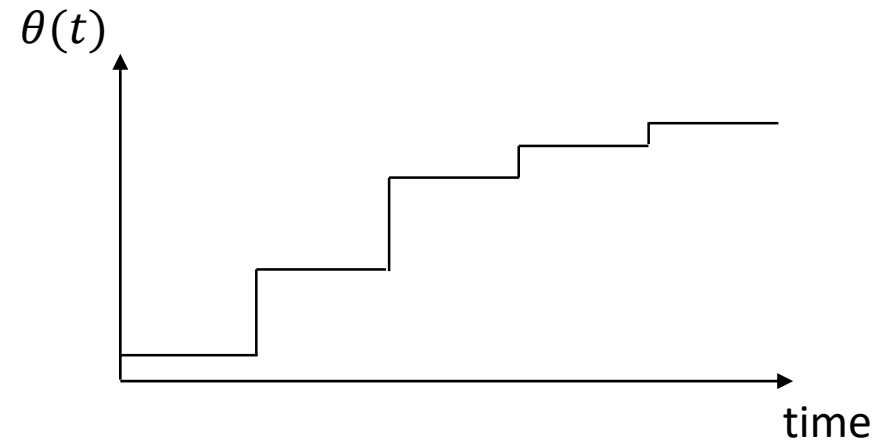
$\theta(t)$  is represented phenomenologically by a piecewise function

Advantages

Drawbacks

## 2) Kingman Coalescent (KC) model

### a) Skyline approach



$\theta(t)$  is represented phenomenologically by a piecewise function

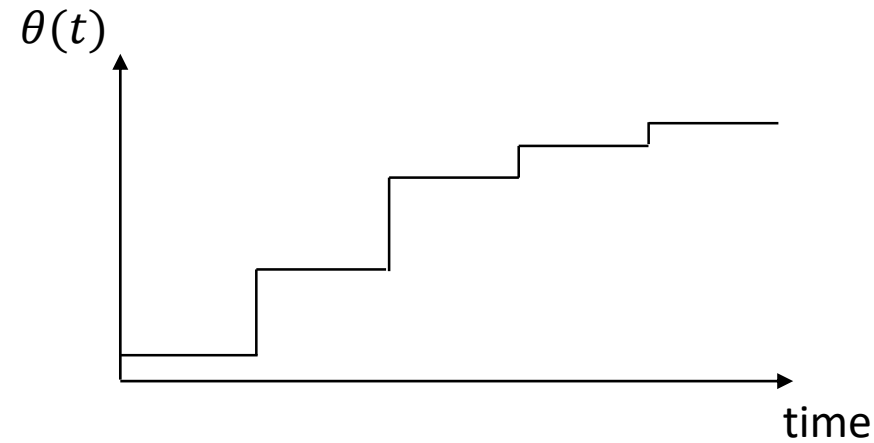
#### Advantages

- No assumption on the sampling procedure (the KC conditions on sampling times)

#### Drawbacks

## 2) Kingman Coalescent (KC) model

### a) Skyline approach



$\theta(t)$  is represented phenomenologically by a piecewise function

#### Advantages

- No assumption on the sampling procedure (the KC conditions on sampling times)

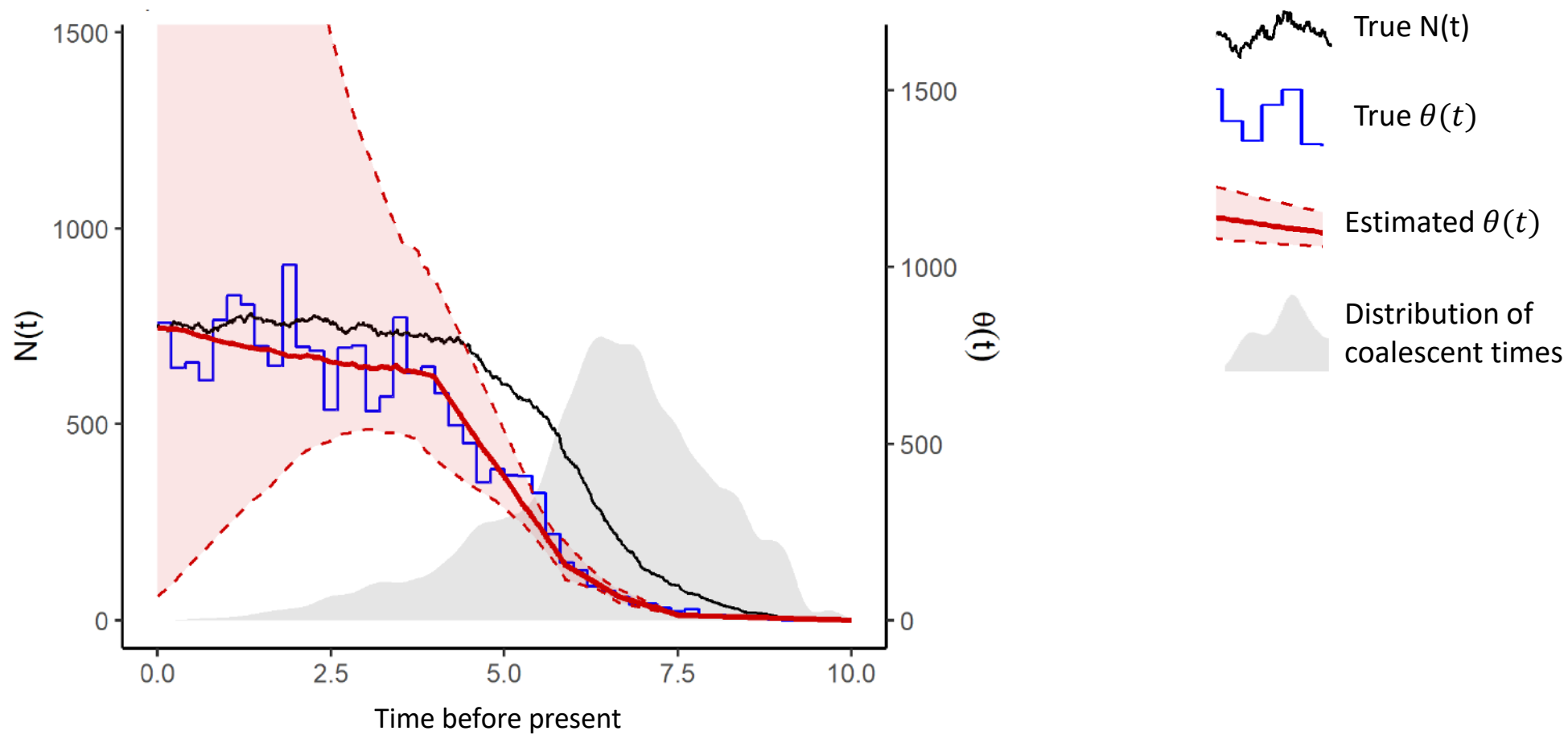
#### Drawbacks

- Interesting epidemiological parameters **cannot** be estimated:
  - ➔  $\lambda(t), \mu(t), N(t), R_e(t)$  are not parameters
  - ➔  $\theta(t)$  is not necessarily proportional to the prevalence  $N(t)$

## 2) Kingman Coalescent (KC) model

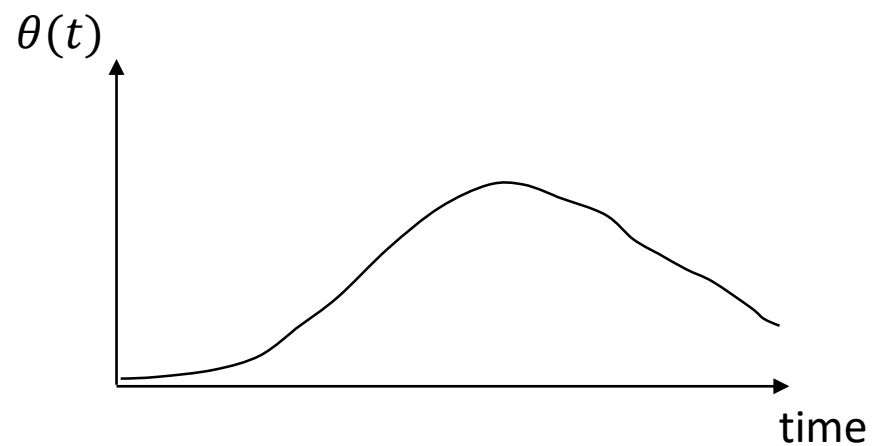
### a) Skyline approach

Skyline KC inference when  $\theta(t)$  is not proportional to  $N(t)$



## 2) Kingman Coalescent (KC) model

### b) Mechanistic approach



$\theta(t) = k N(t)$  with  $N(t)$  the population size as predicted by an epidemiological model

## 2) Kingman Coalescent (KC) model

### b) Mechanistic approach

Example: SIR epidemiological model

$S(t)$  = # susceptible individuals

$I(t)$  = # infected individuals

$R(t)$  = # removed individuals (ie. immunised or dead)

$K = S(t) + I(t) + R(t)$  = total population size (constant)

## 2) Kingman Coalescent (KC) model

### b) Mechanistic approach

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$$I'(t) = \frac{\beta S(t)}{K} I(t) - \mu I(t)$$

$$S'(t) = -\frac{\beta S(t)}{K} I(t)$$

$$R'(t) = -\mu I(t)$$

## 2) Kingman Coalescent (KC) model

### b) Mechanistic approach

Example: SIR epidemiological model


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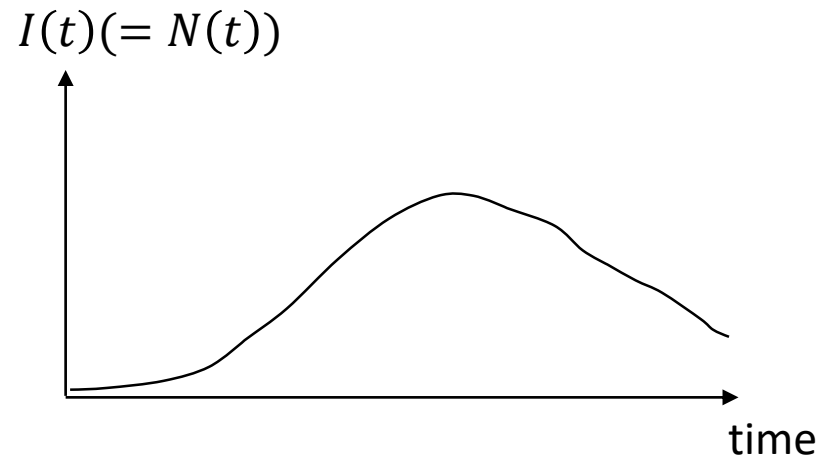
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Solving 





## 2) Kingman Coalescent (KC) model

### b) Mechanistic approach

Example: SIR epidemiological model


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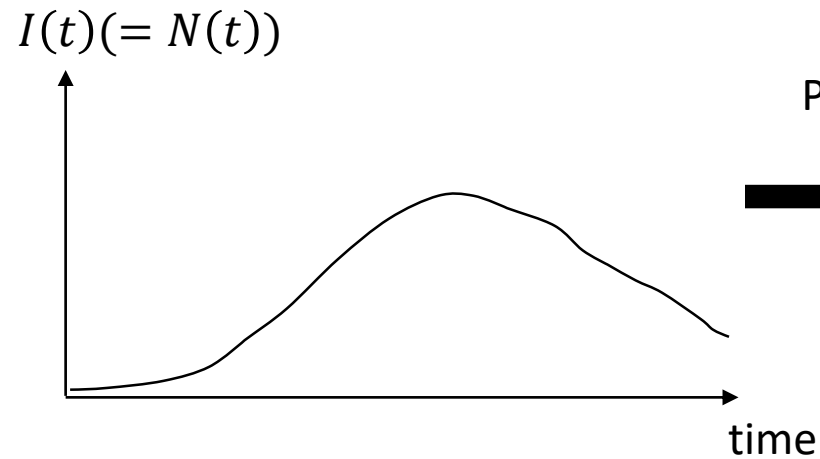
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Solving 



Parametrizing the KC   $\theta(t) = k I(t)$

## 2) Kingman Coalescent (KC) model

### b) Mechanistic approach

Advantages

Drawbacks

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#### Advantages

- No assumption on the sampling procedure (the KC conditions on sampling times)

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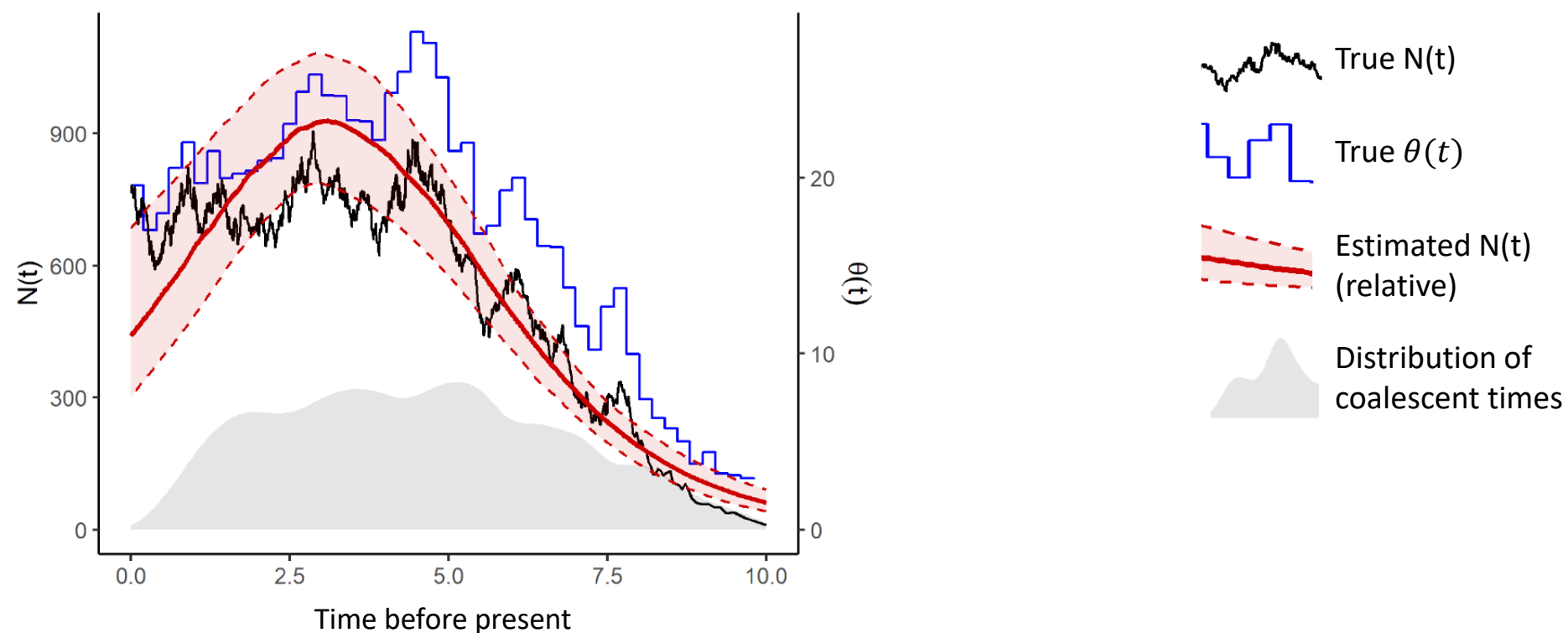
#### Drawbacks

- $\theta(t)$  is not necessarily proportional to the prevalence  $N(t)$
- Sensitive to model choice

## 2) Kingman Coalescent (KC) model

### b) Mechanistic approach

Mechanistic KC inference with incorrect model



Simulation: SIS model ( $N(t)$  reaches a plateau)

Inference: SIR model ( $N(t)$  reaches a maximum and decreases)





Advantages

Drawbacks

## Advantages

- No assumption on the sampling procedure (based on the KC)

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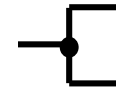
- The sampled tree is not enough information to identify the parameters
  - ➔ Requires auxilliary data

## 1) Mathematical foundation

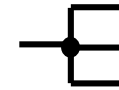
### Assumptions:

- The epidemic unraveled according to a **BD-type model** (ie. multiple simultaneous births are not allowed)

Allowed



Not allowed

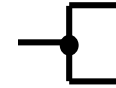


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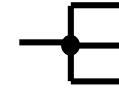
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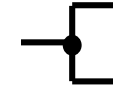


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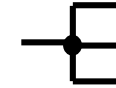
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### Result:

In the limit of large population size, the probability distribution of the sampled tree under a BD-type model converges to that of a Kingman coalescent with parameter

$$\theta(t) = \frac{N(t)}{2\lambda(t)}$$

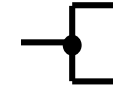


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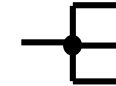
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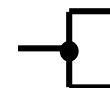
$$\theta(t) = \frac{N(t)}{2\lambda(t)} = \frac{N_0 \exp \int_0^t (\mu(s) - \lambda(s)) ds}{2\lambda(t)}$$

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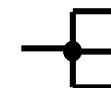
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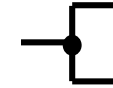
The three parameters  $\lambda(t)$ ,  $\mu(t)$  and  $N_0$  are not separately identifiable

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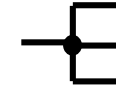
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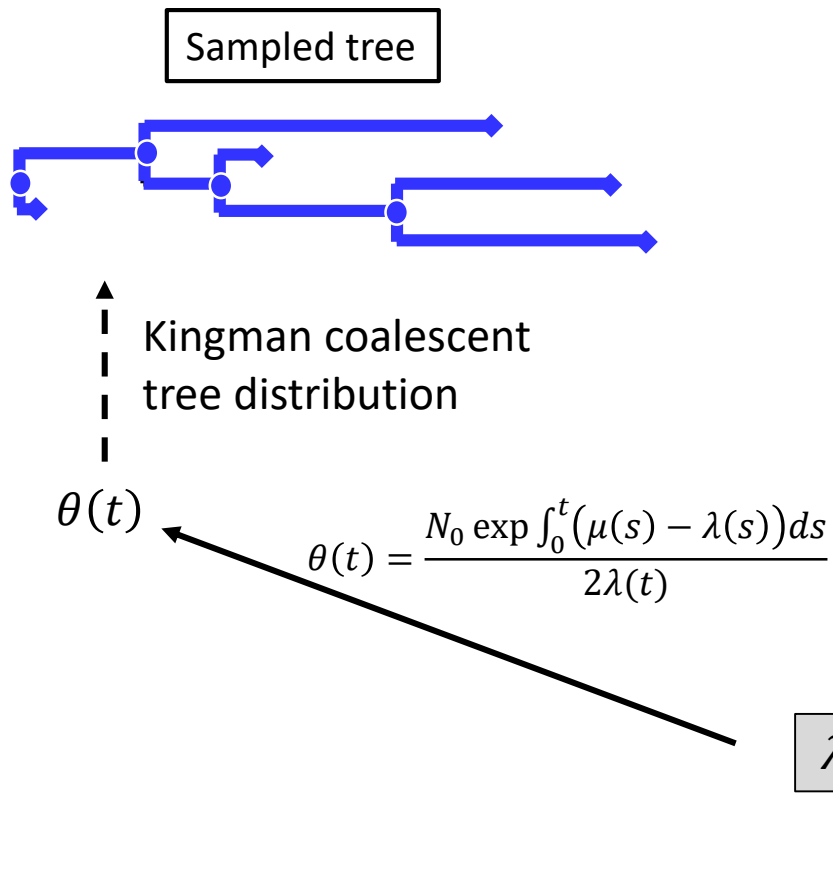


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Auxilliary data required

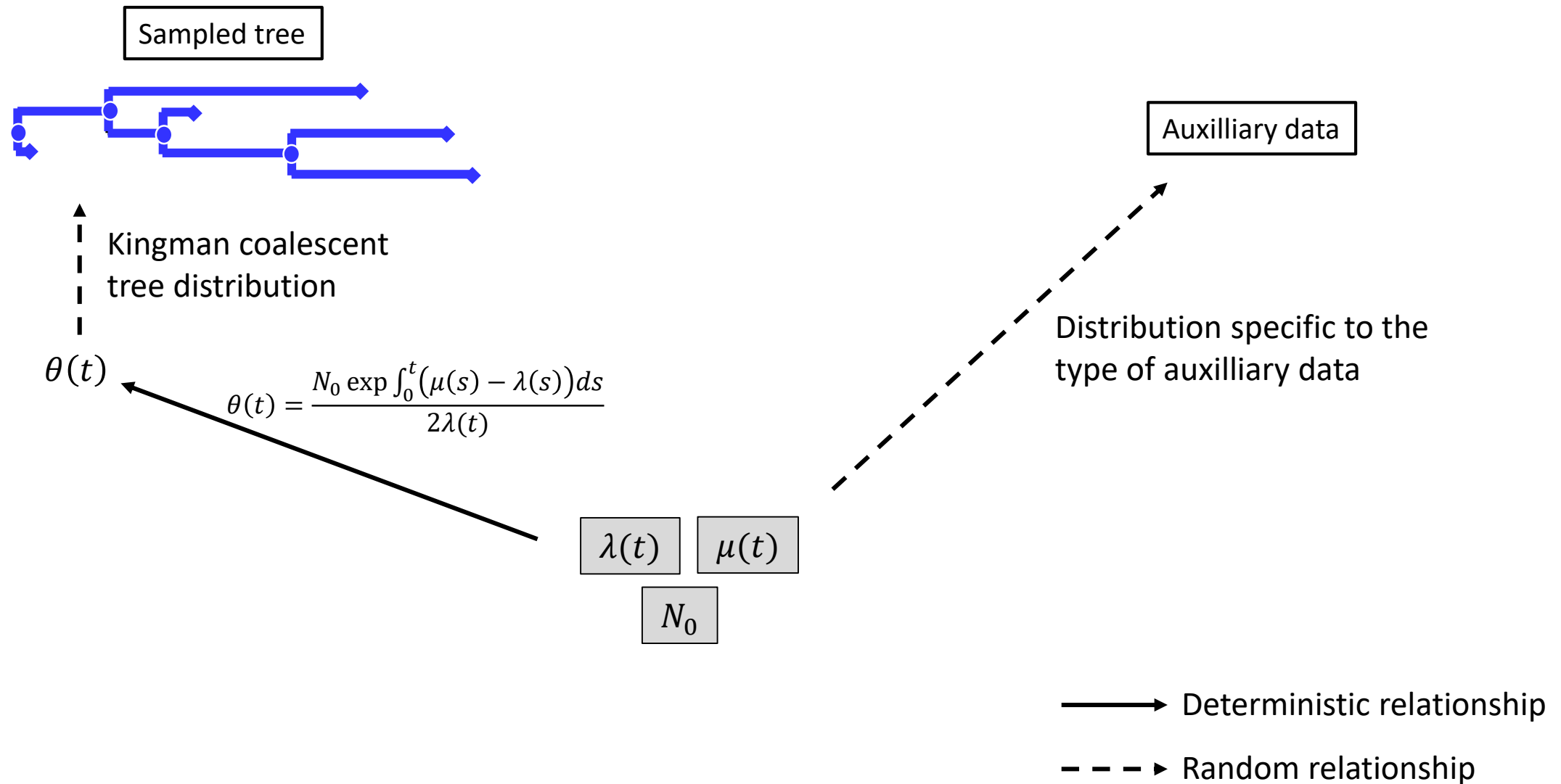
## 2) Statistical inference



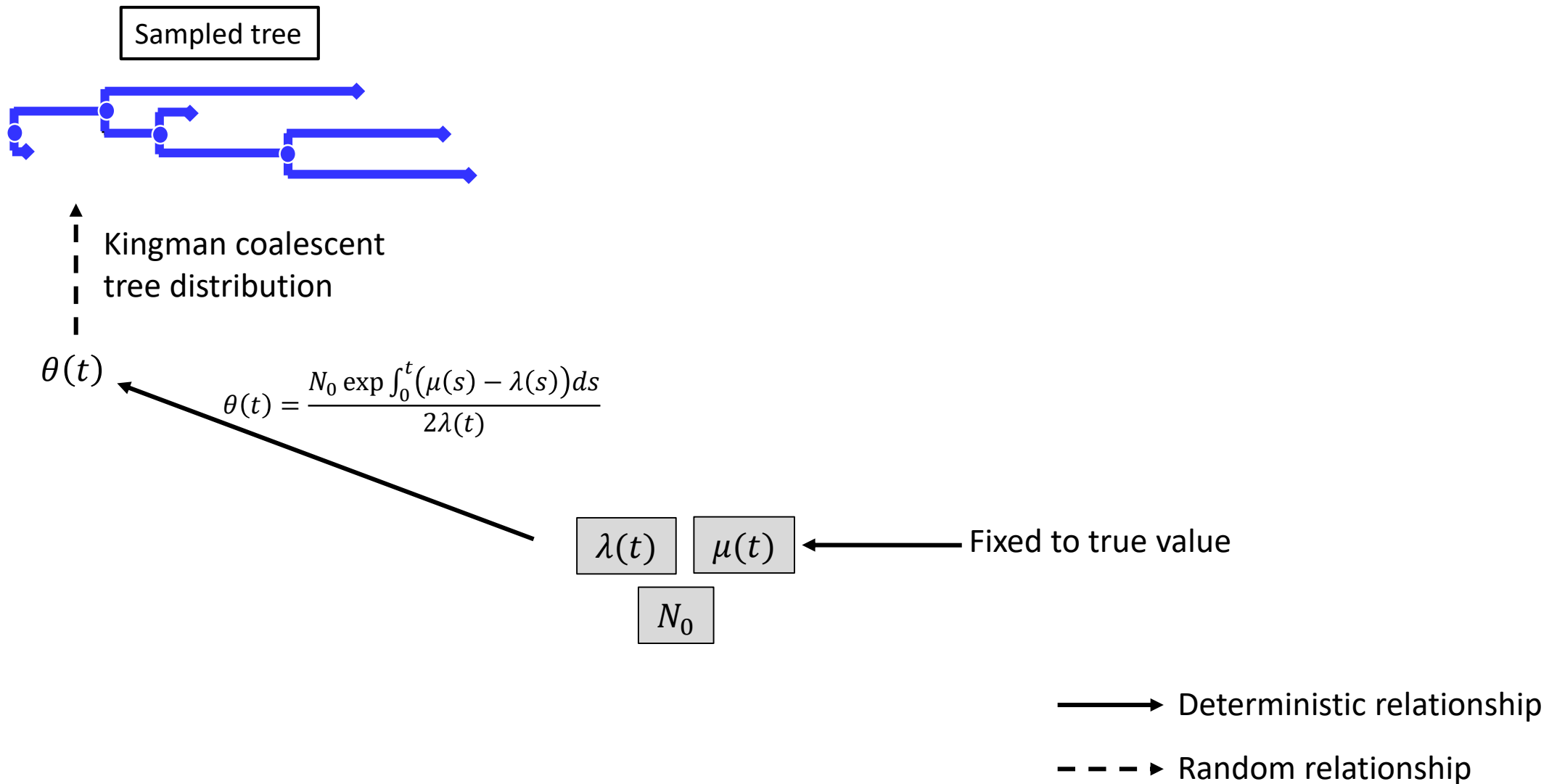
—————▶ Deterministic relationship

- - - -▶ Random relationship

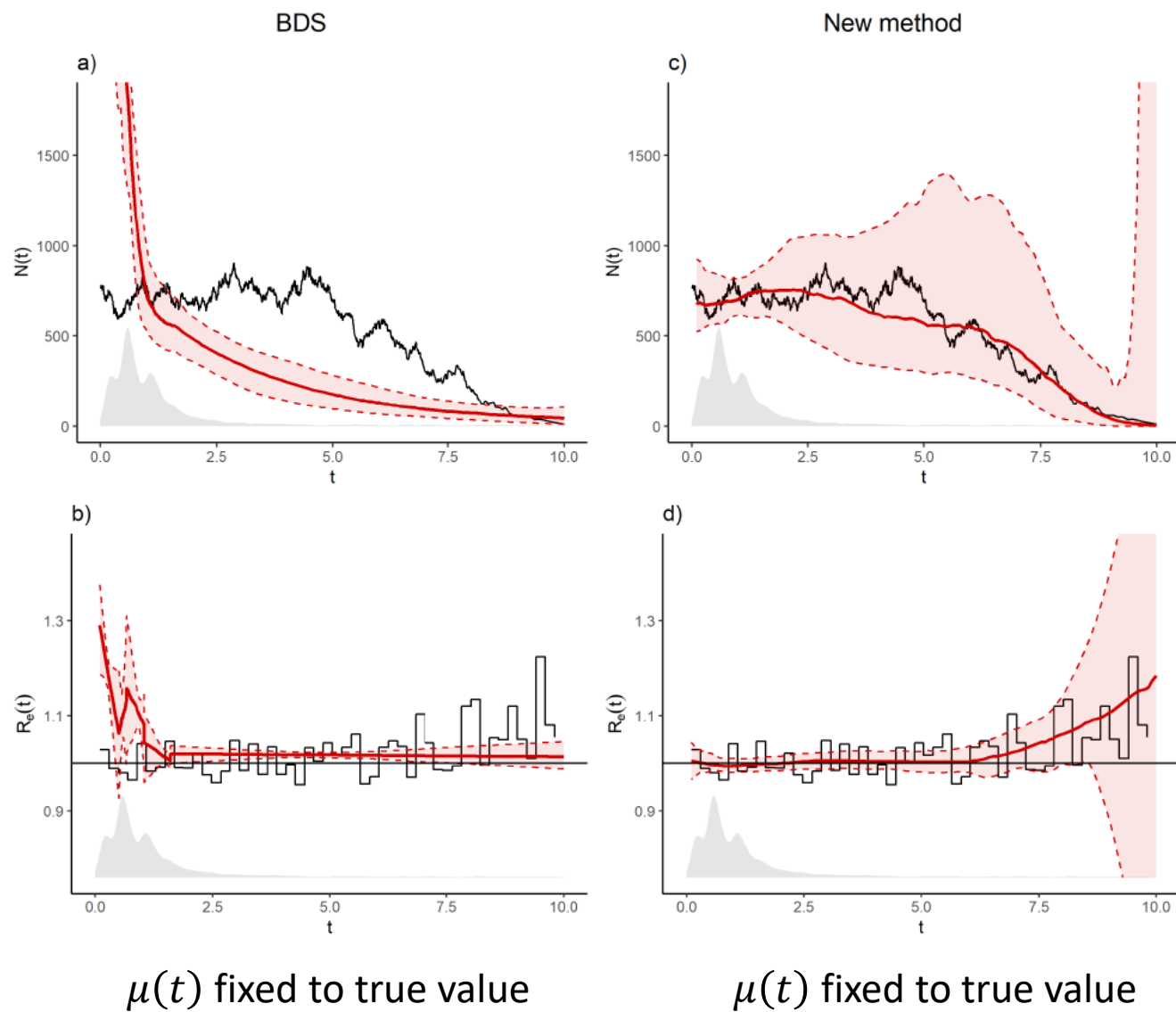
## 2) Statistical inference



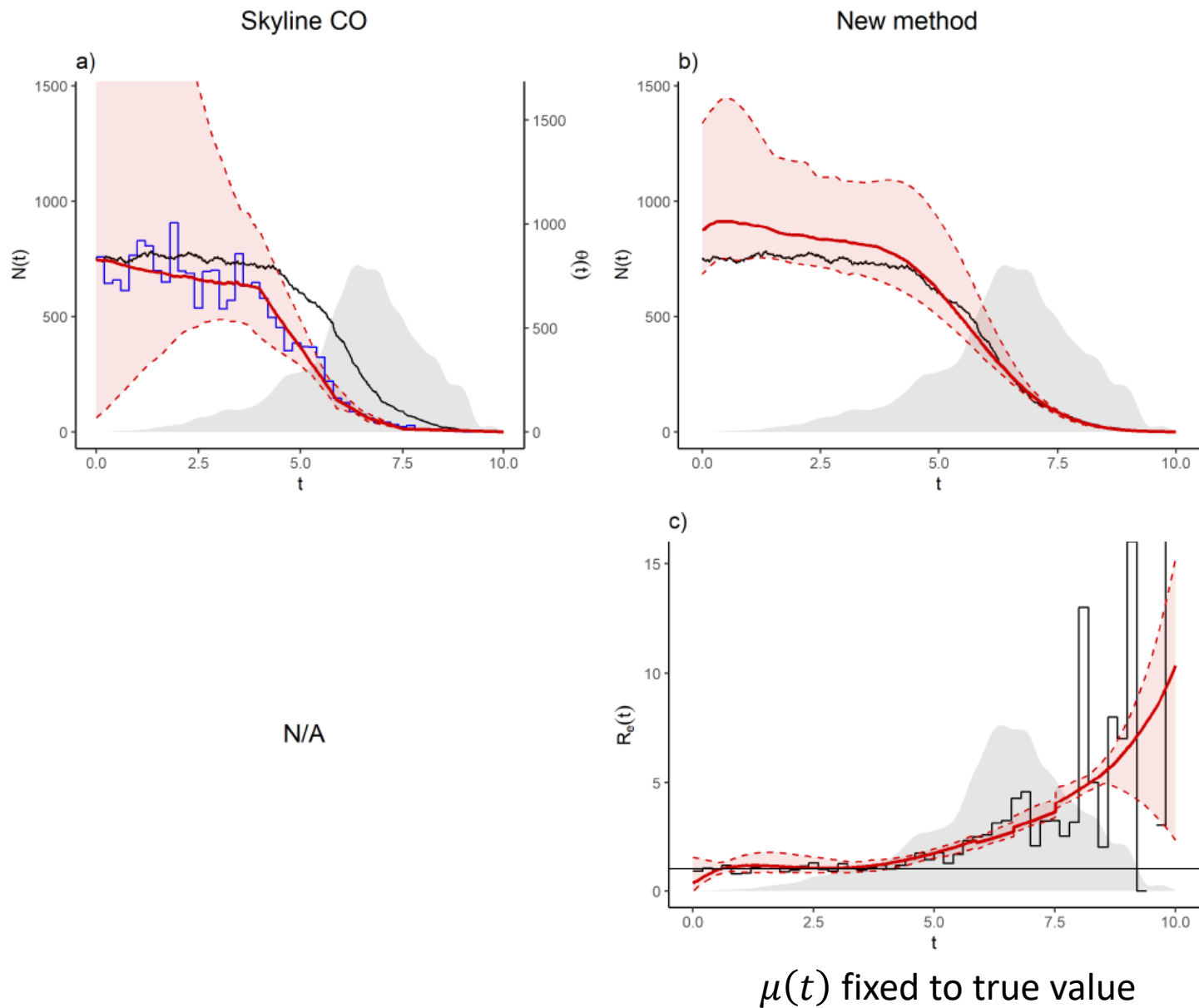
## 2) Statistical inference



## 3) Comparison with other methods

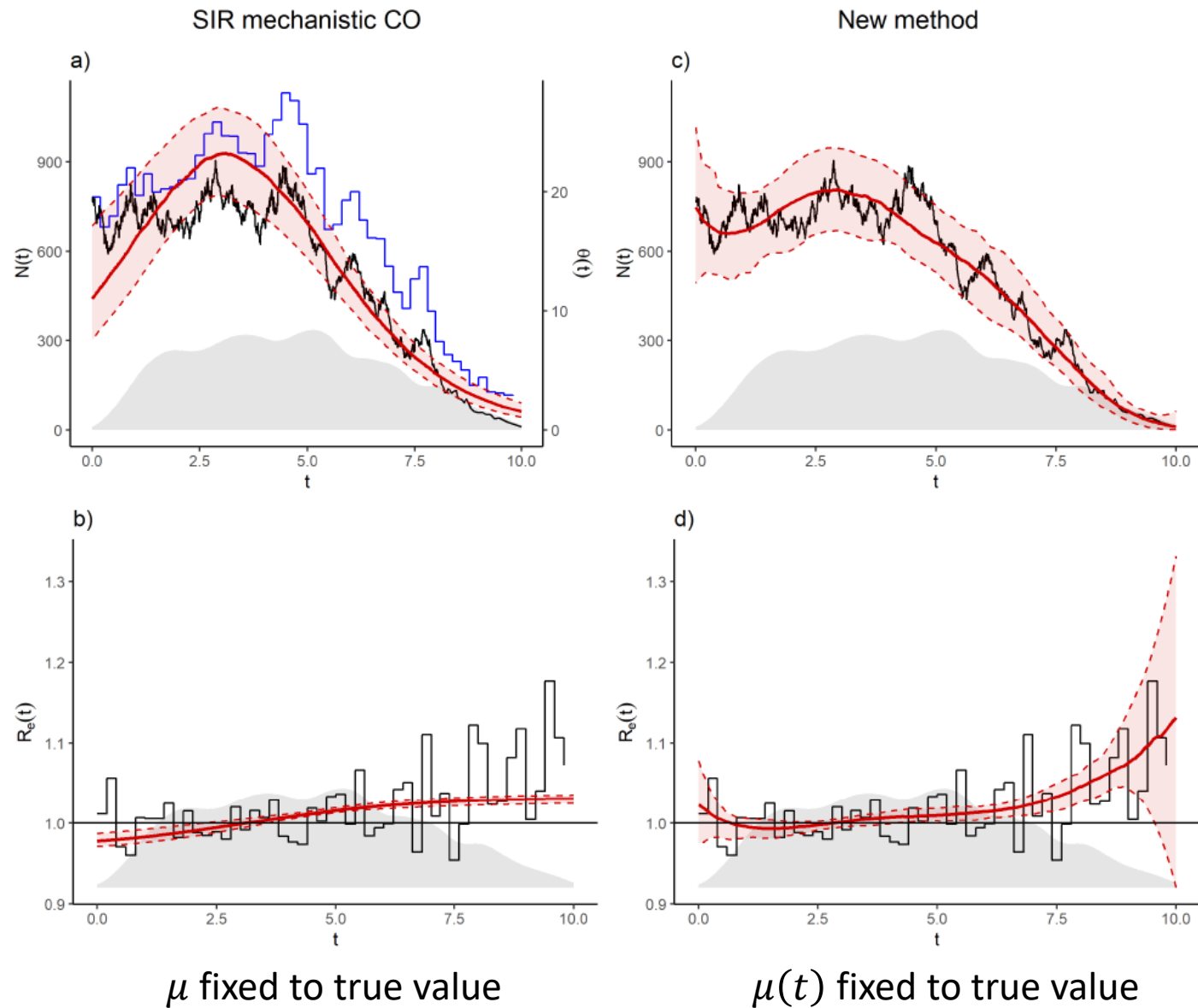


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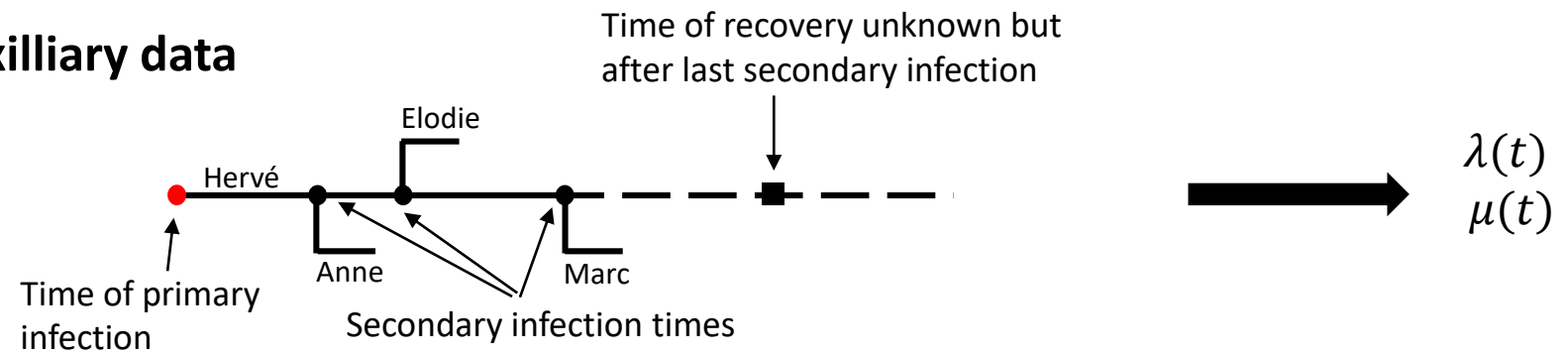
**4) Test of the method**

**a) With various types of auxilliary data**

## 4) Test of the method

### a) With various types of auxilliary data

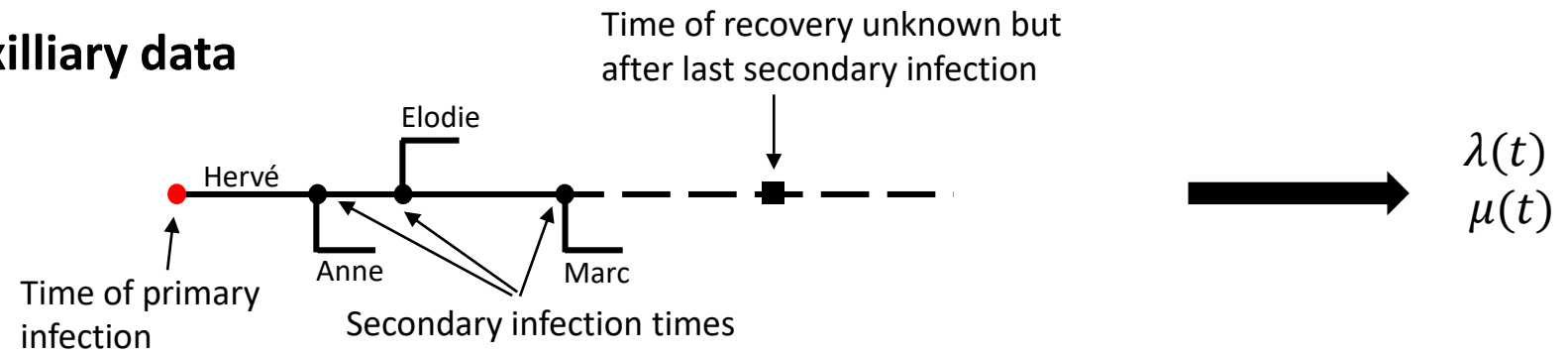
- Transmission chains



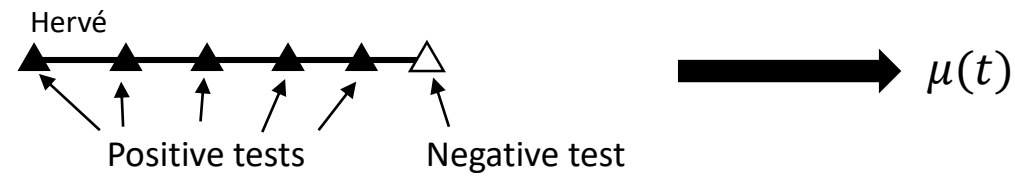
## 4) Test of the method

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- Transmission chains



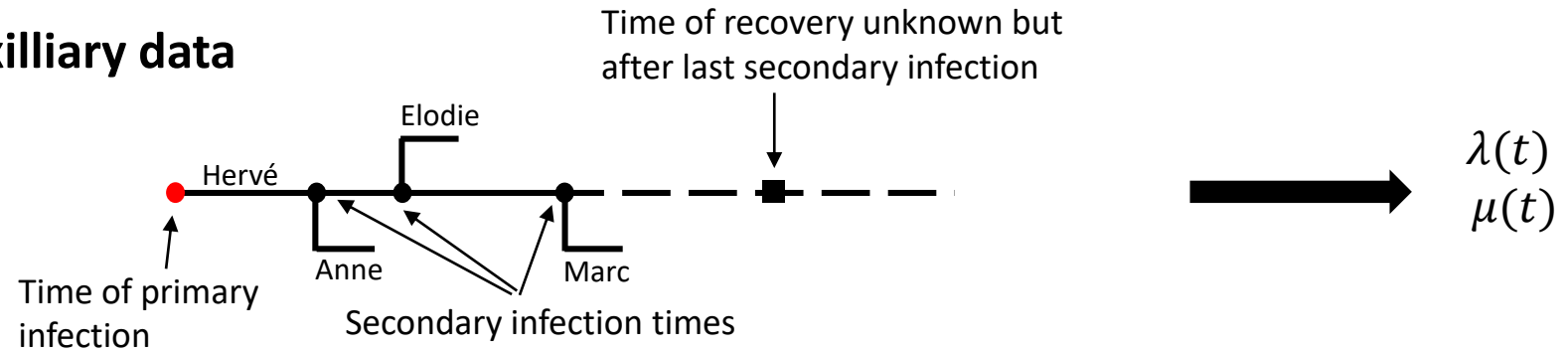
- Duration of infection



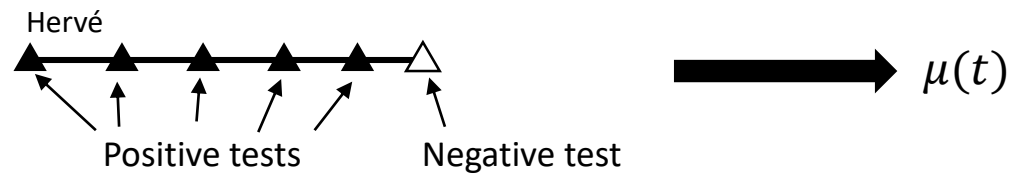
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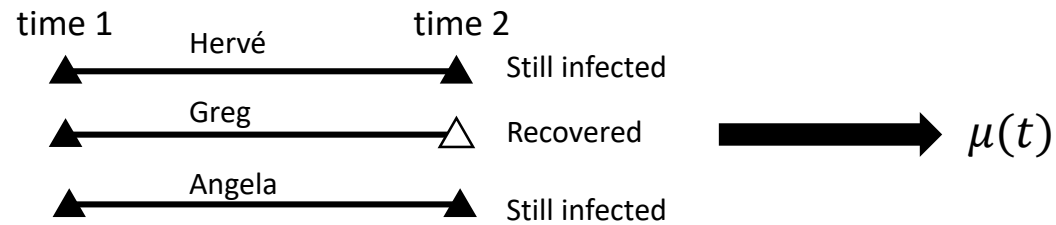
- Transmission chains



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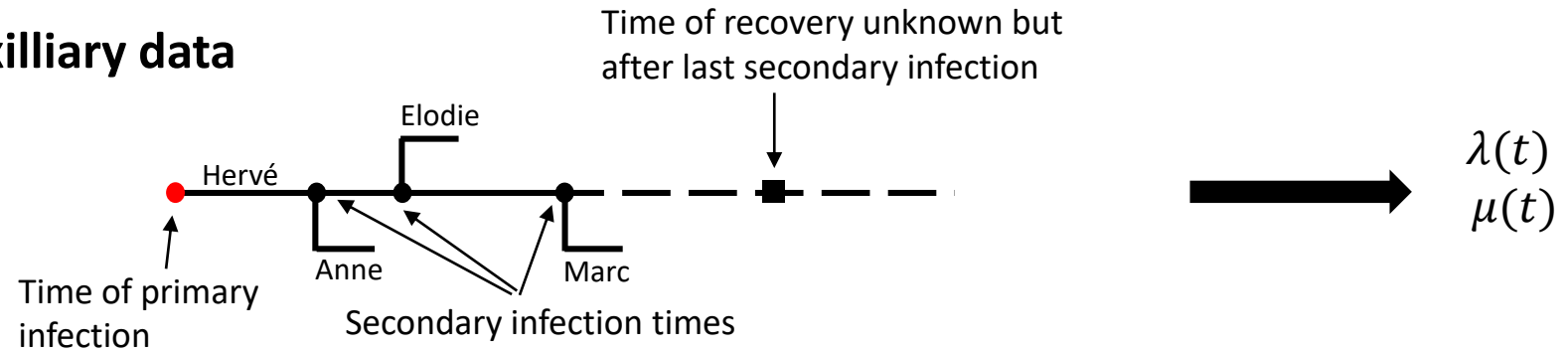
- Incidence of recovery



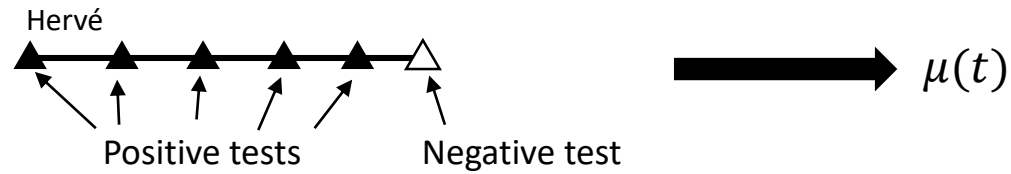
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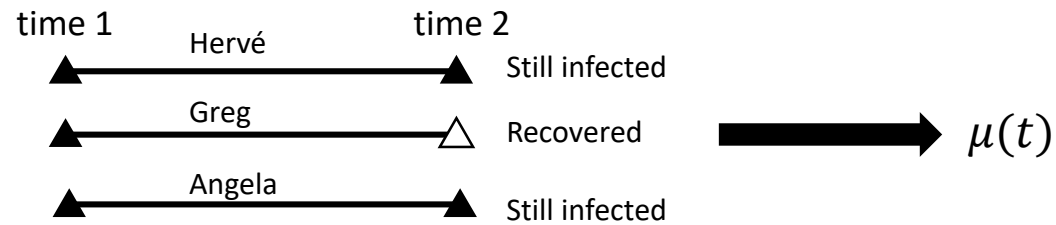
- Transmission chains



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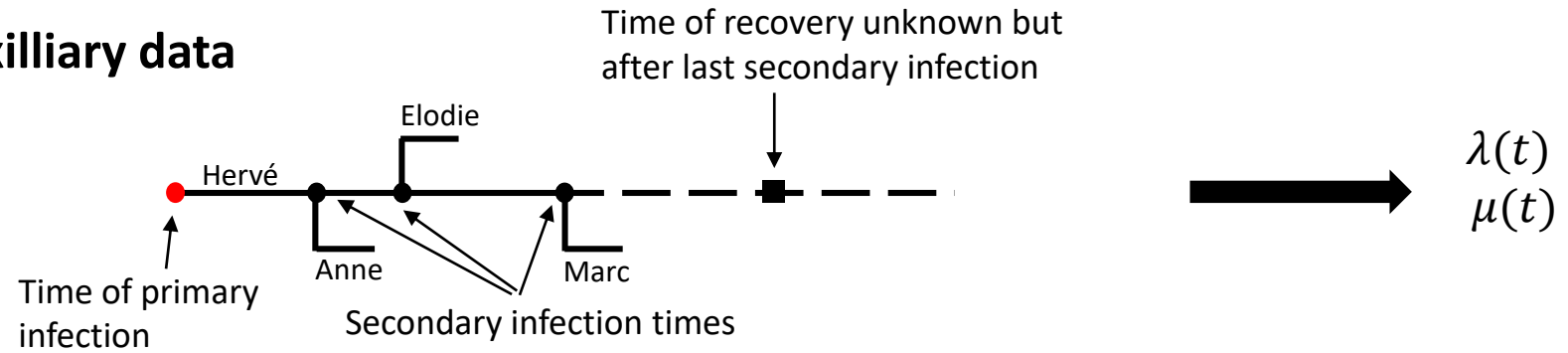
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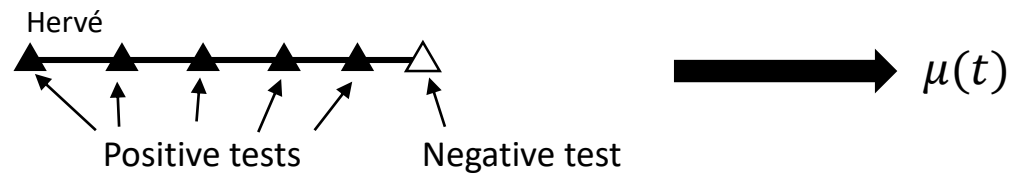
## 4) Test of the method

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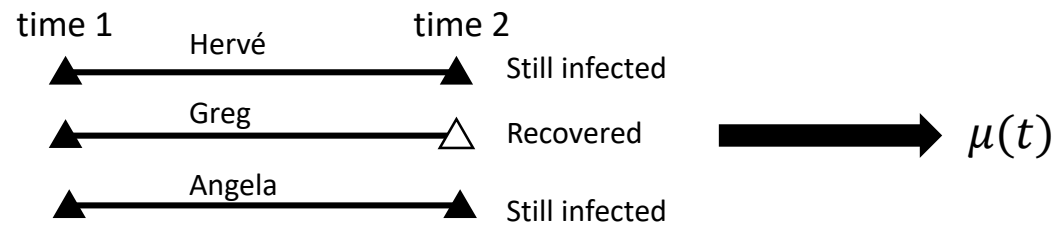
- Transmission chains



- Duration of infection



- Incidence of recovery



- Incidence of new cases

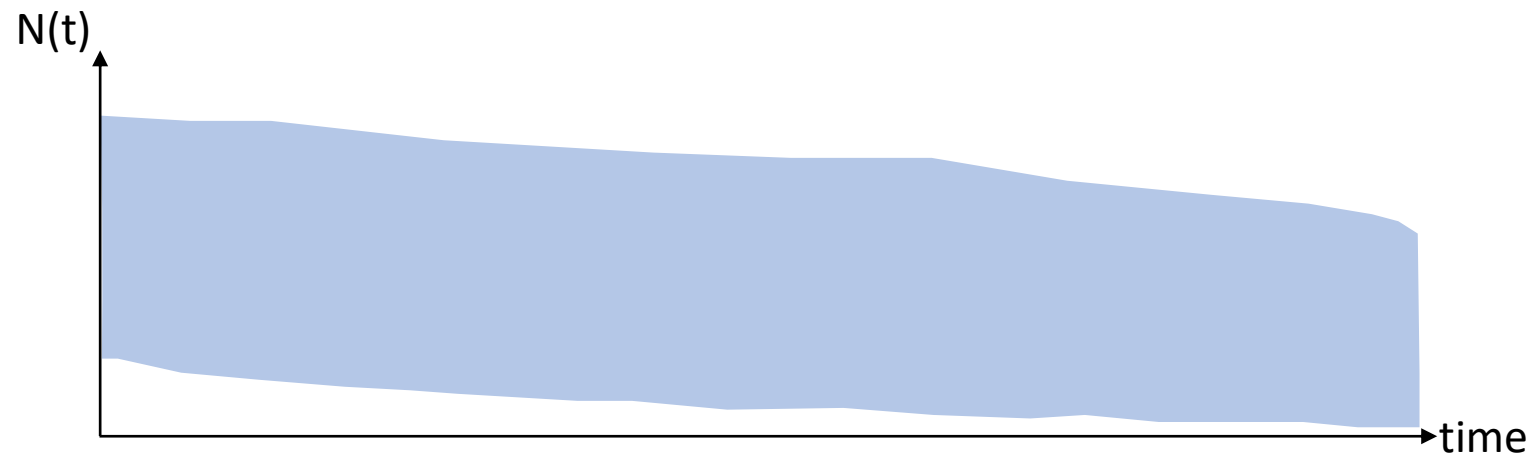
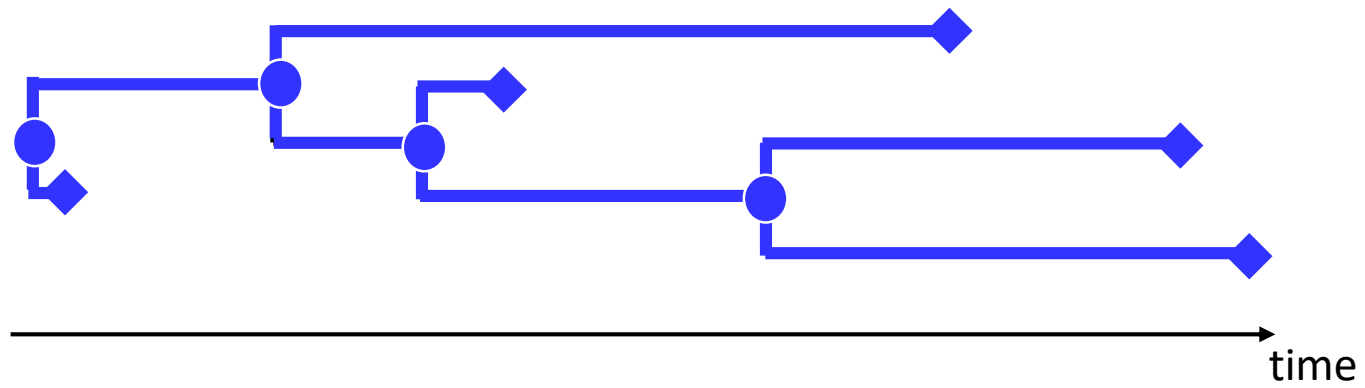


- Prevalence



## 4) Test of the method

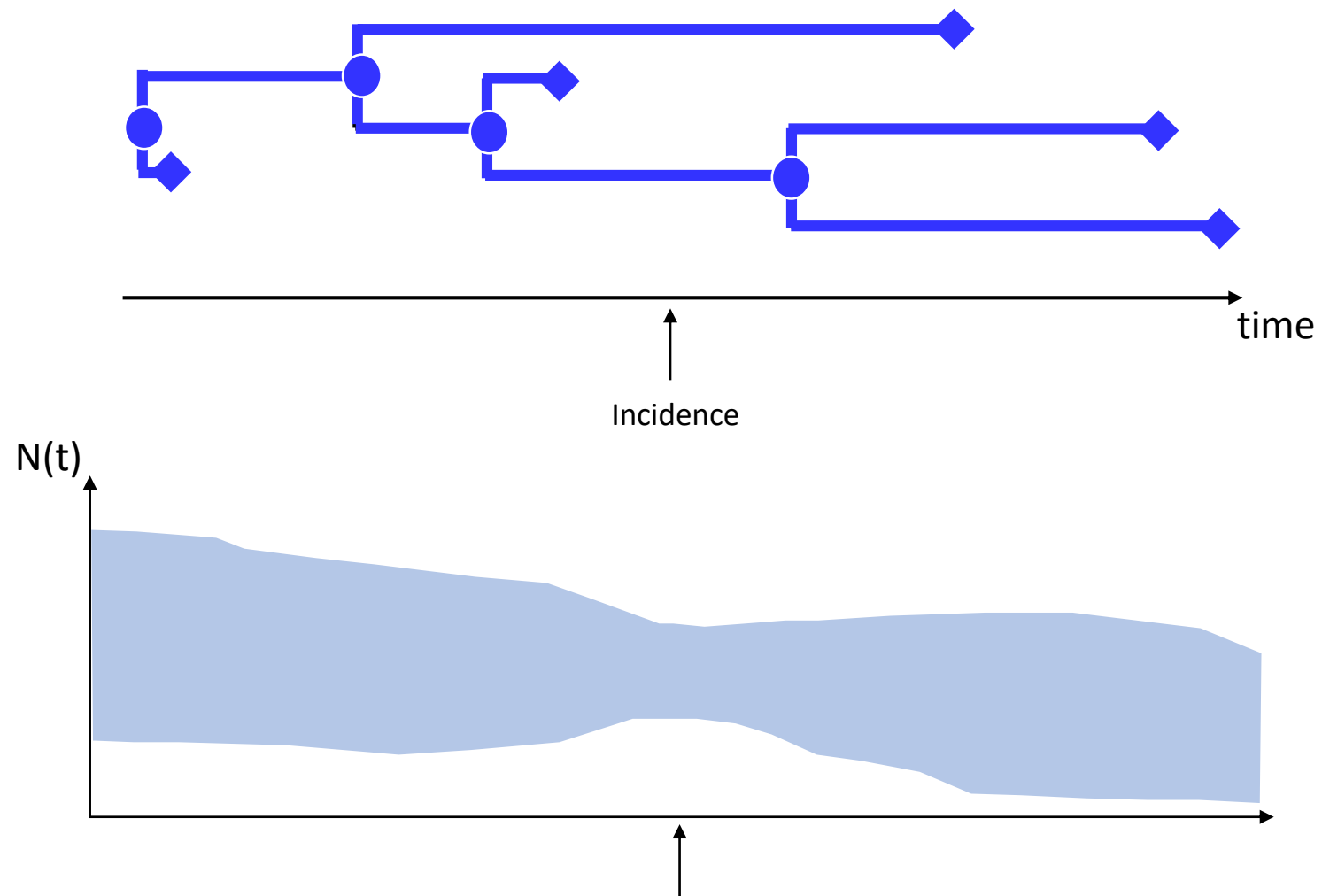
### a) With various types of auxiliary data





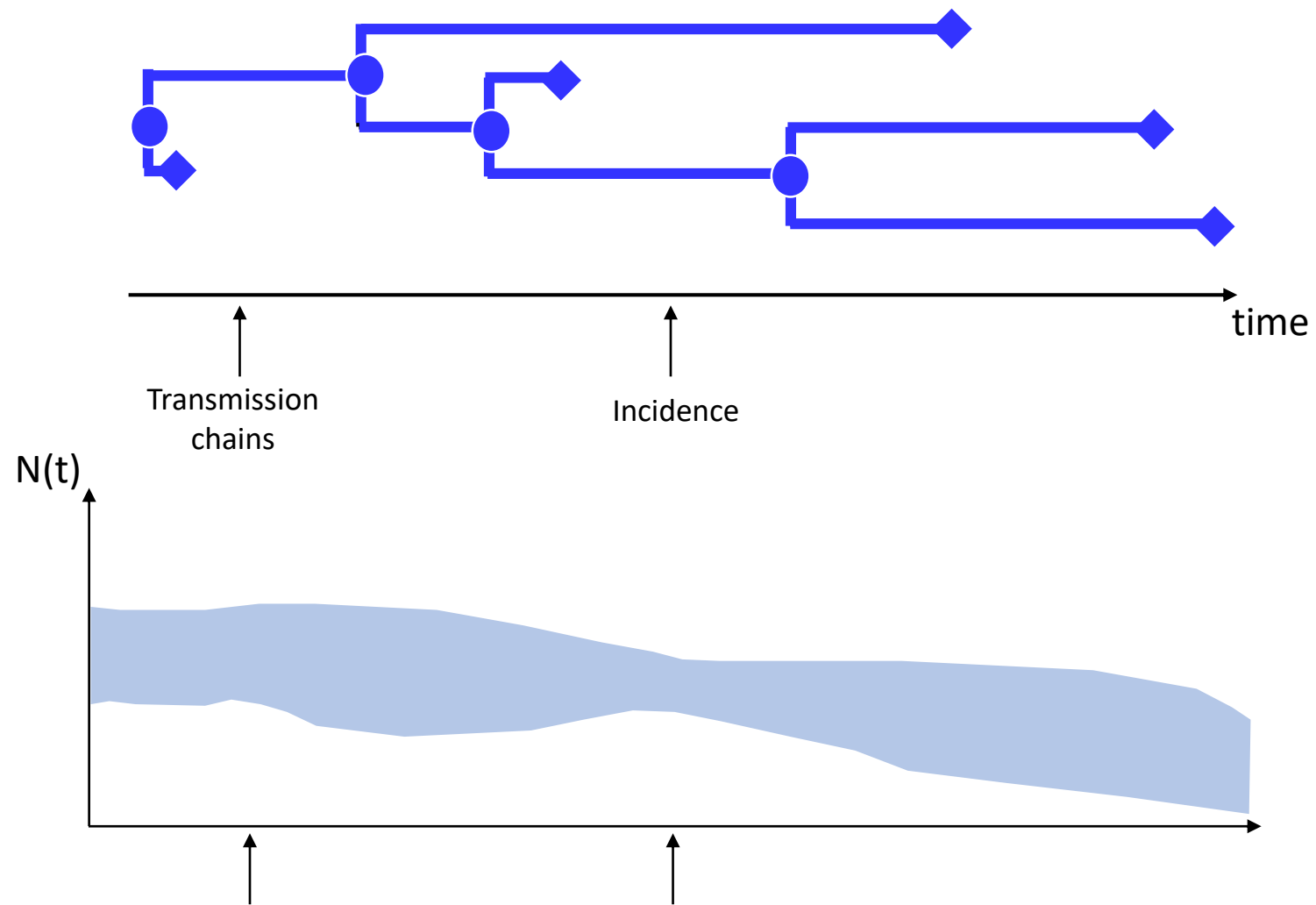
## 4) Test of the method

### a) With various types of auxiliary data



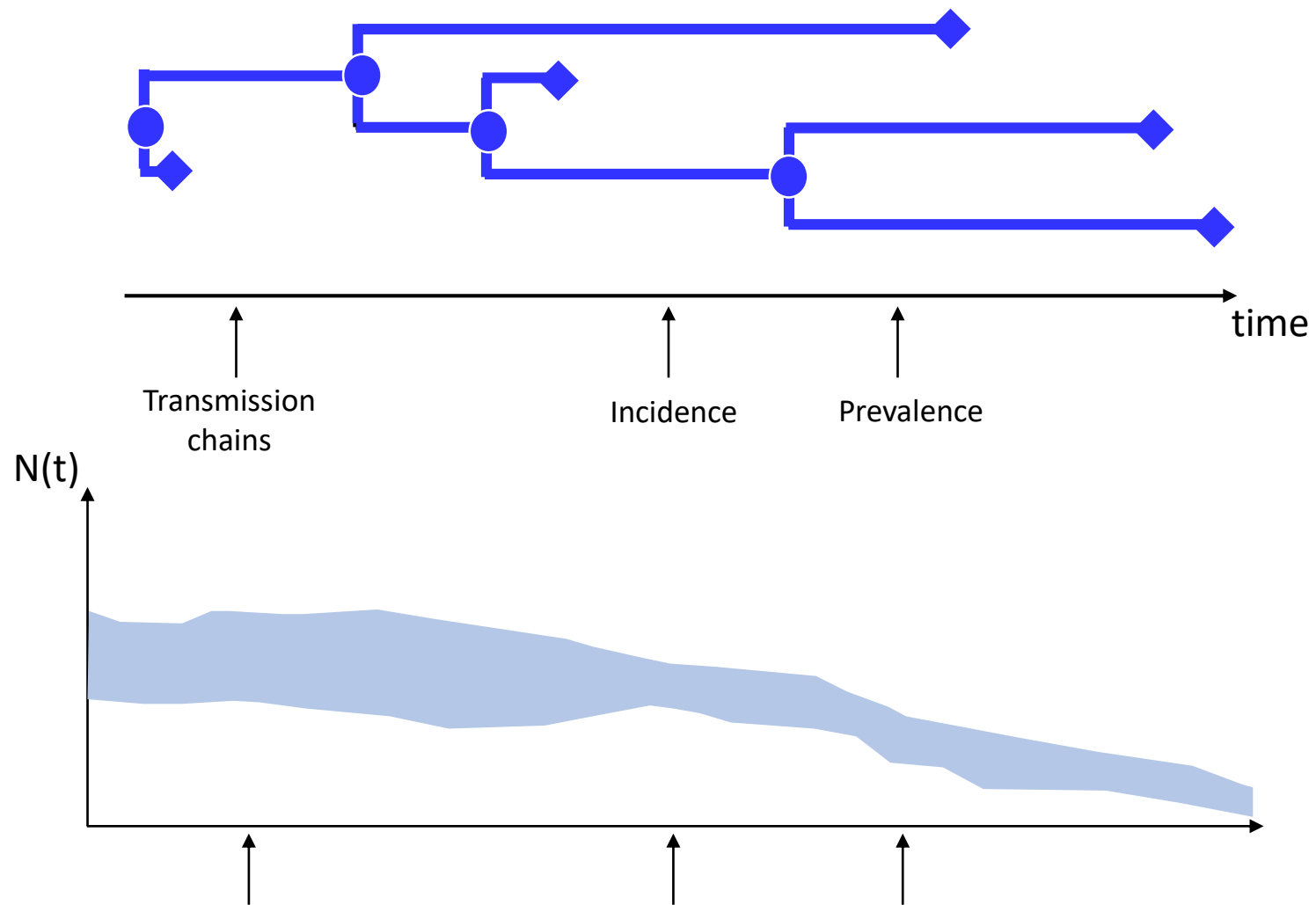
## 4) Test of the method

### a) With various types of auxiliary data



## 4) Test of the method

### a) With various types of auxiliary data



## 4) Test of the method

### b) With structured models

- Geographic structure
- Different types of individuals (multi-stage infections)
- Different variants

THANK YOU FOR YOUR  
ATTENTION