

Tracking uncertainties in mechanistic models *for risk assessment of pest control strategies*

Virgile BAUDROT

CBGP – 24 septembre 2019

PhD 2013-2016

Post-Doc 2016-2018

Post-Doc 2018-2020



Modélisation des interactions trophiques impliquant des transferts de contaminants biologiques (*E. multilocularis*) et chimiques (ETMs)

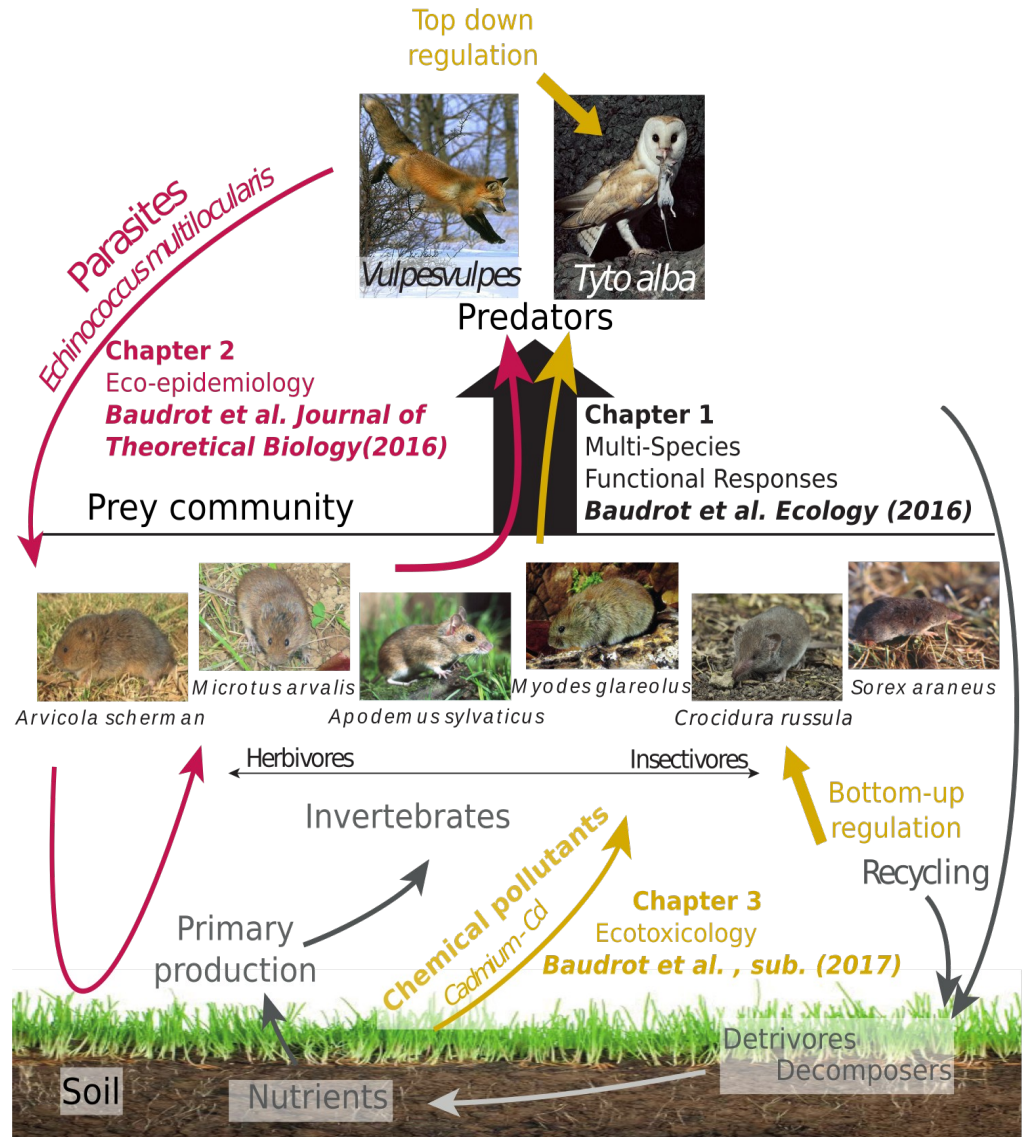
Director:

Francis Raoul

Co-supervisors:

Clémentine Fritsch,

Antoine Perasso

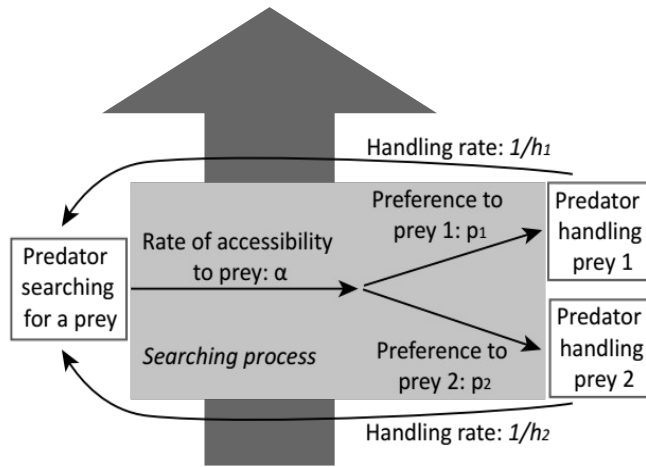




Vulpes vulpes



Tyto alba



Arvicola scherman



Microtus arvalis



Myodes glareolus



Sorex sp.

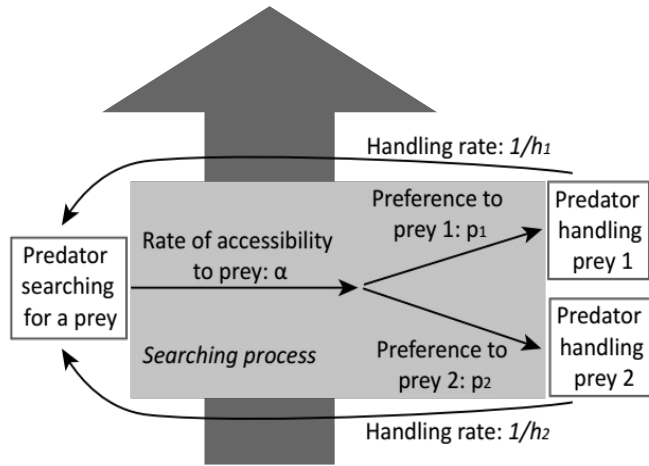
$$\Phi_i(\vec{x}) = p_i(\vec{x}) \times \frac{\alpha(\vec{x})}{1+h\alpha(\vec{x})} = p_i(\vec{x}) \times \Theta(\vec{x})$$



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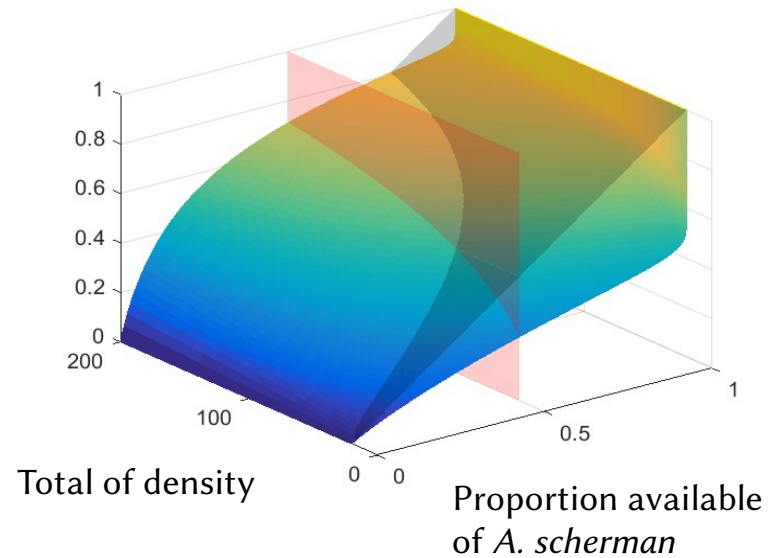
Prey switching ...

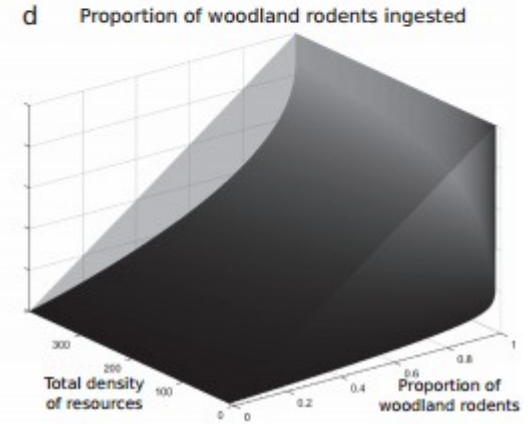
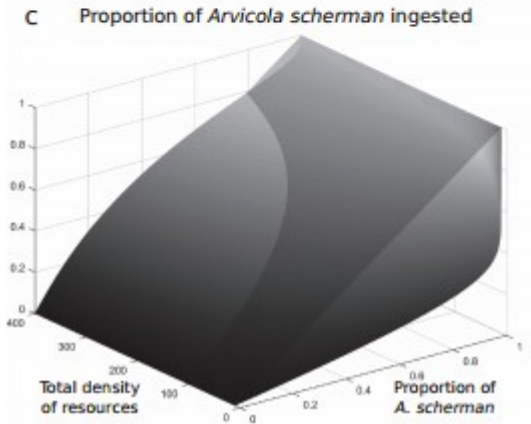
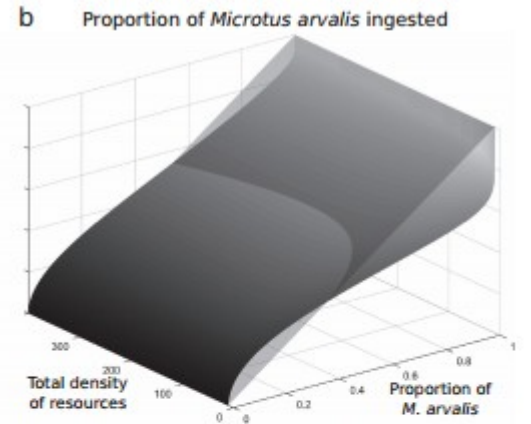
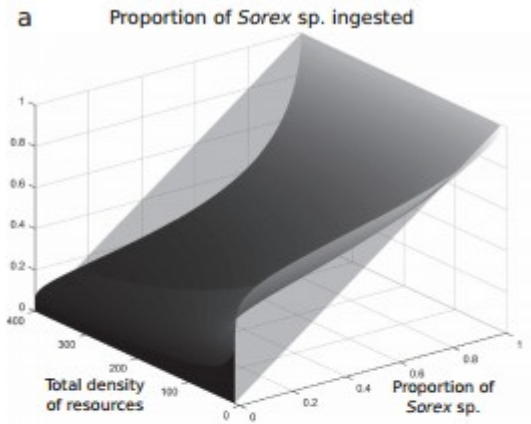
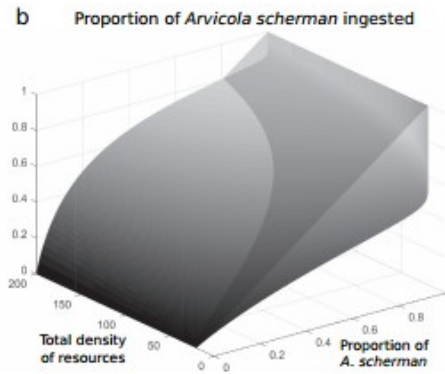
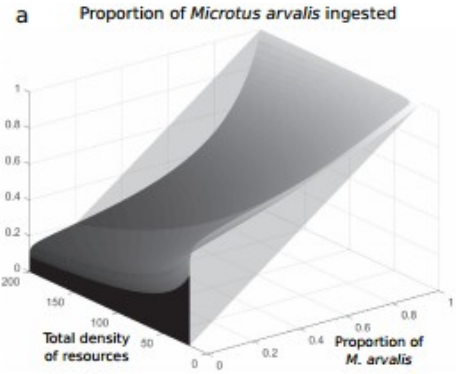
... density dependent

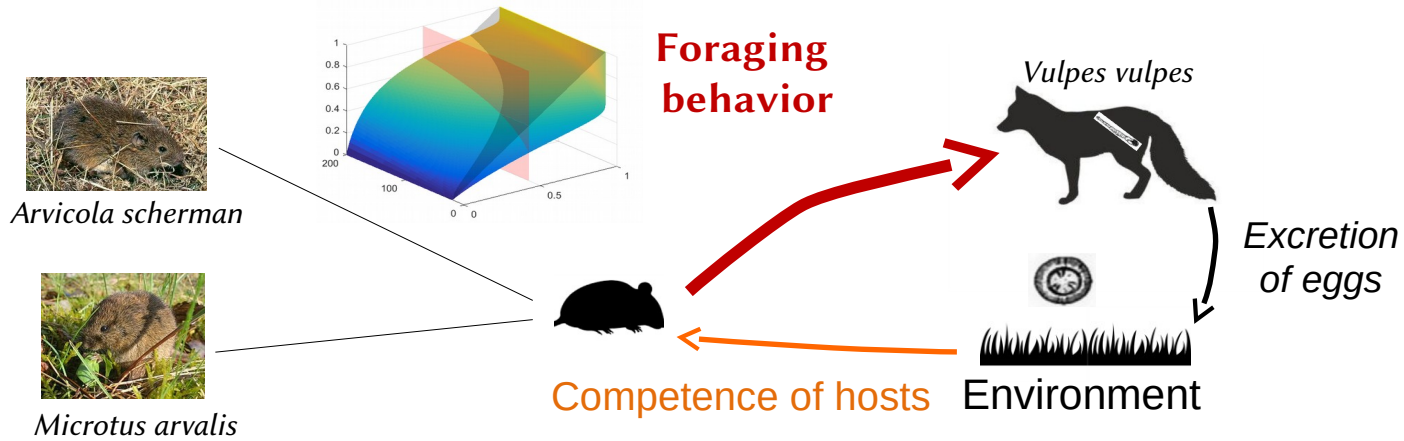
... frequency dependent

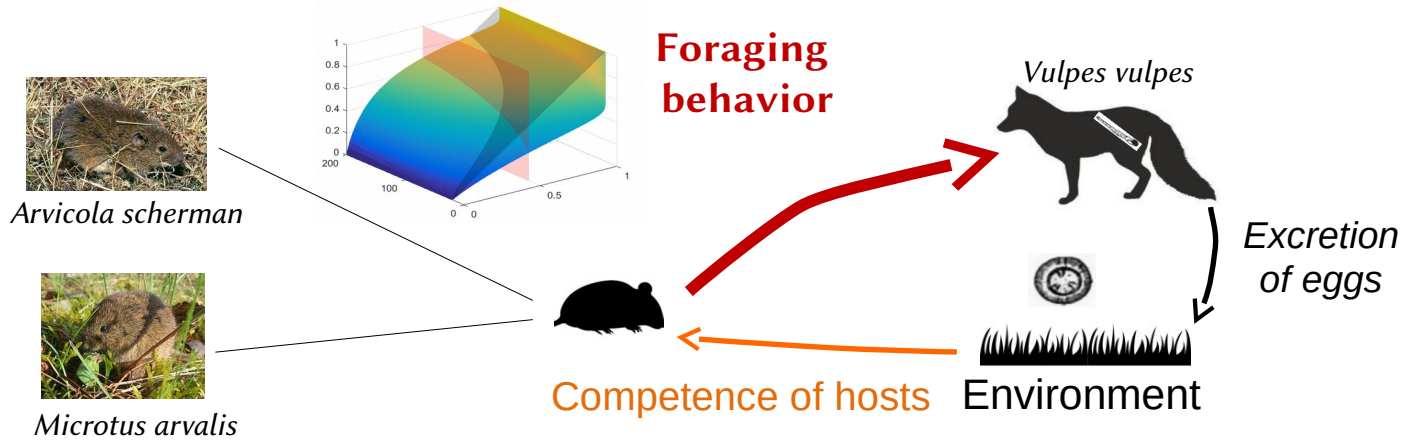
$$\Phi_i(\vec{x}) = p_i(\vec{x}) \times \frac{\alpha(\vec{x})}{1+h\alpha(\vec{x})} = p_i(\vec{x}) \times \Theta(\vec{x})$$

Prop. *A. scherman* ingested / *V. vulpes*









Basic reproductive number

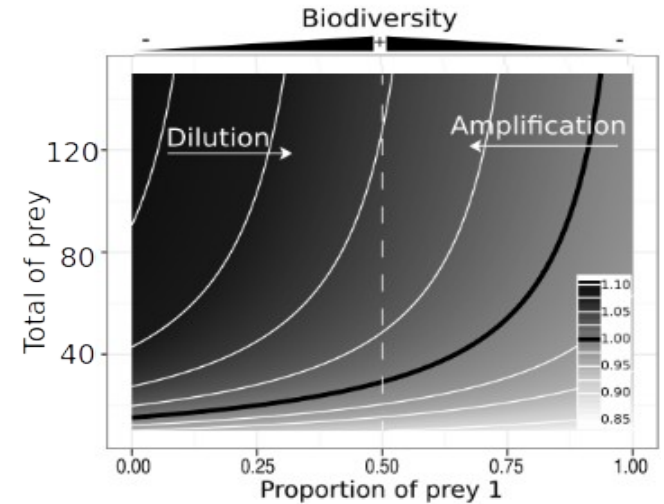
$$\mathcal{R}_0 = \frac{\eta z^*}{\sqrt{b(b_z + \mu)}} \times (\Gamma_1 \Phi_1(x_1^*, x_2^*) + \Gamma_2 \Phi_2(x_1^*, x_2^*))$$

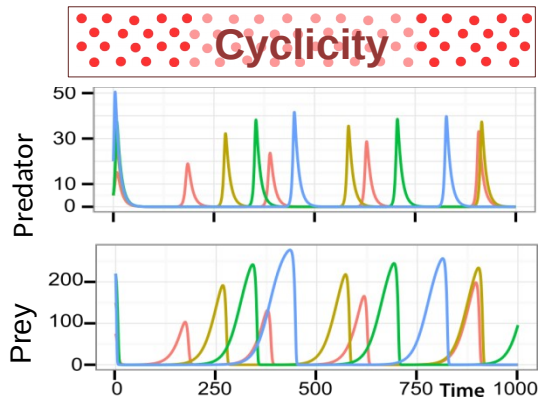
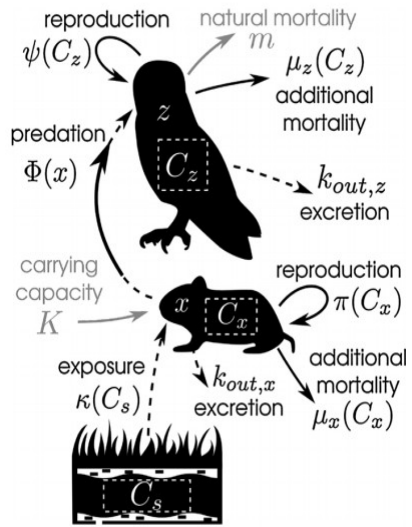
“Introduction” of susceptibles

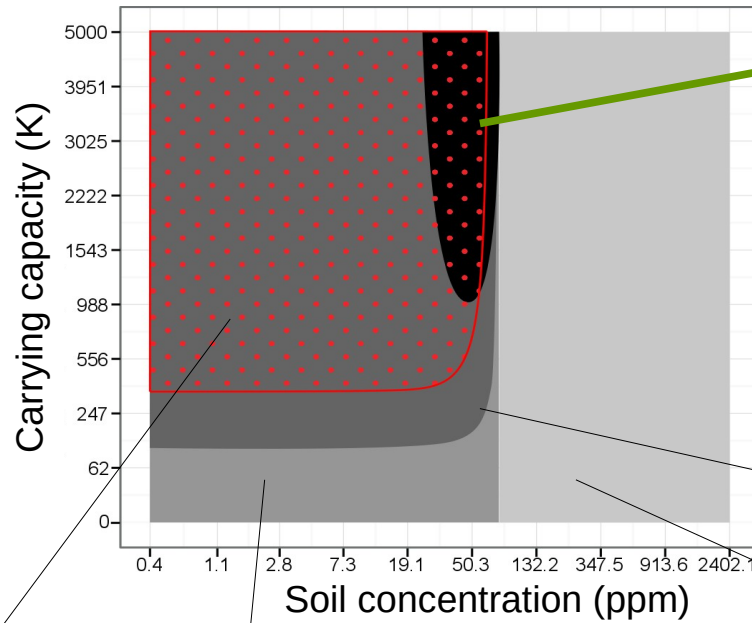
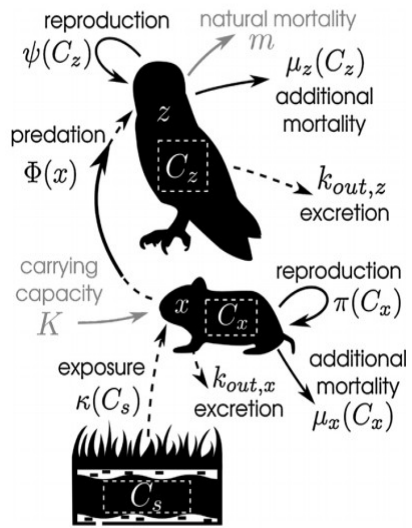
Foraging behavior (MSFR)

Competence of hosts

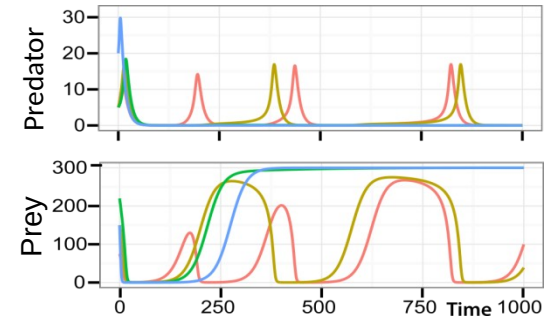
hosts diversity & disease risk



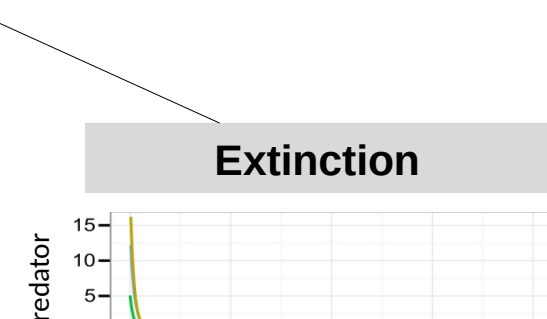




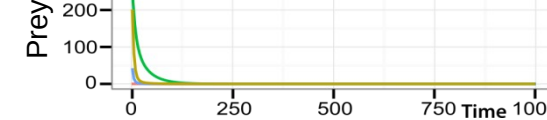
Bistability



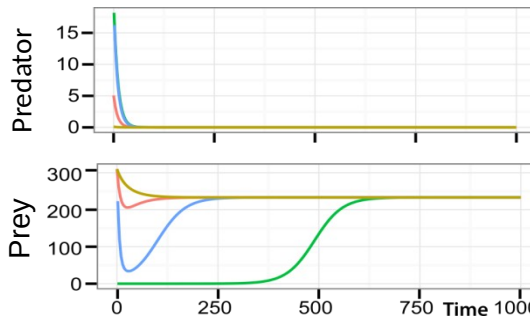
Coexistence



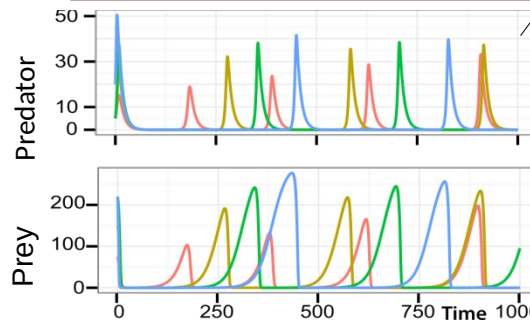
Extinction

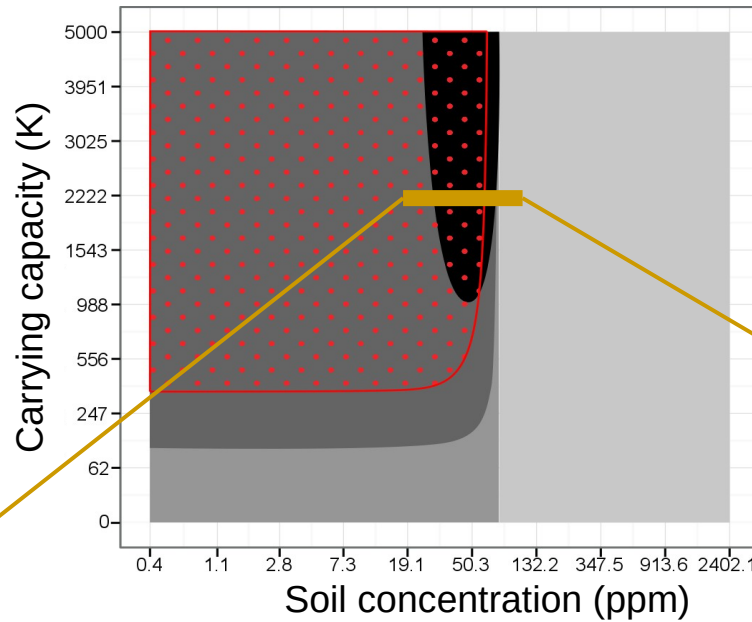
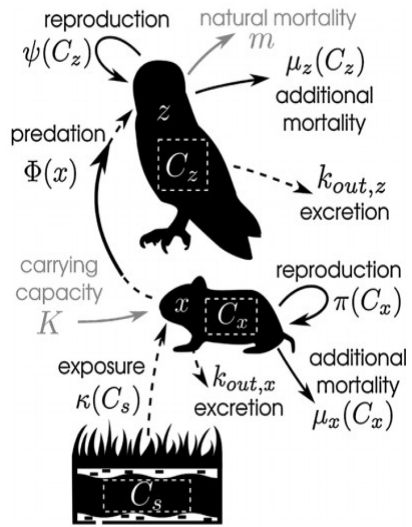


Prey-only



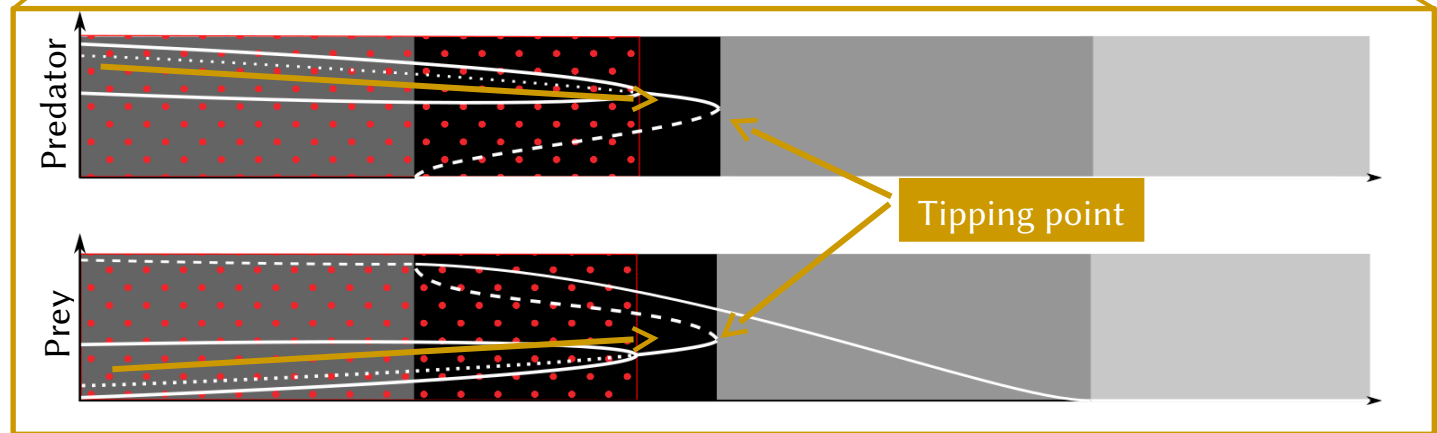
Cyclicity

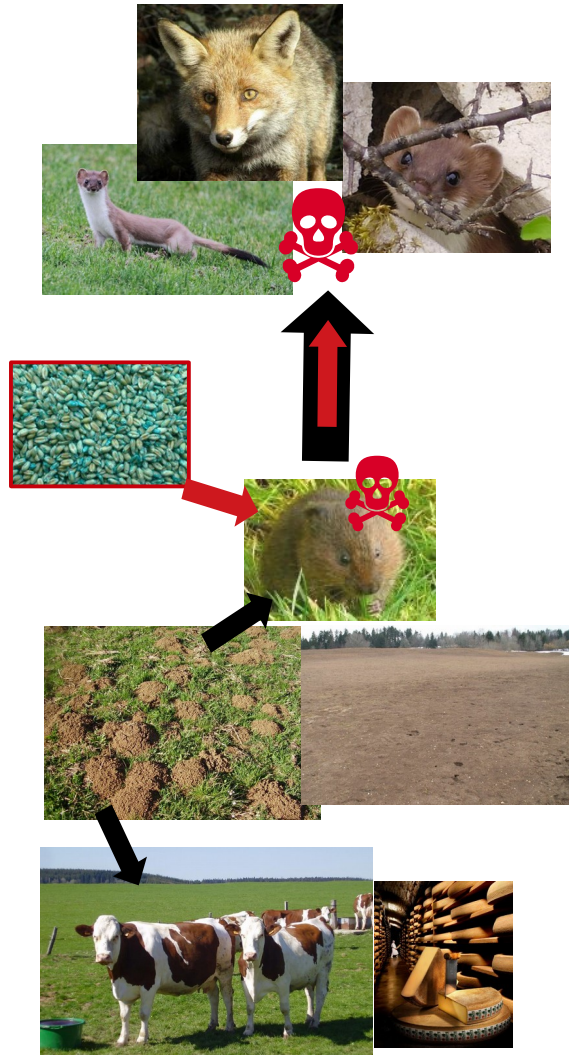


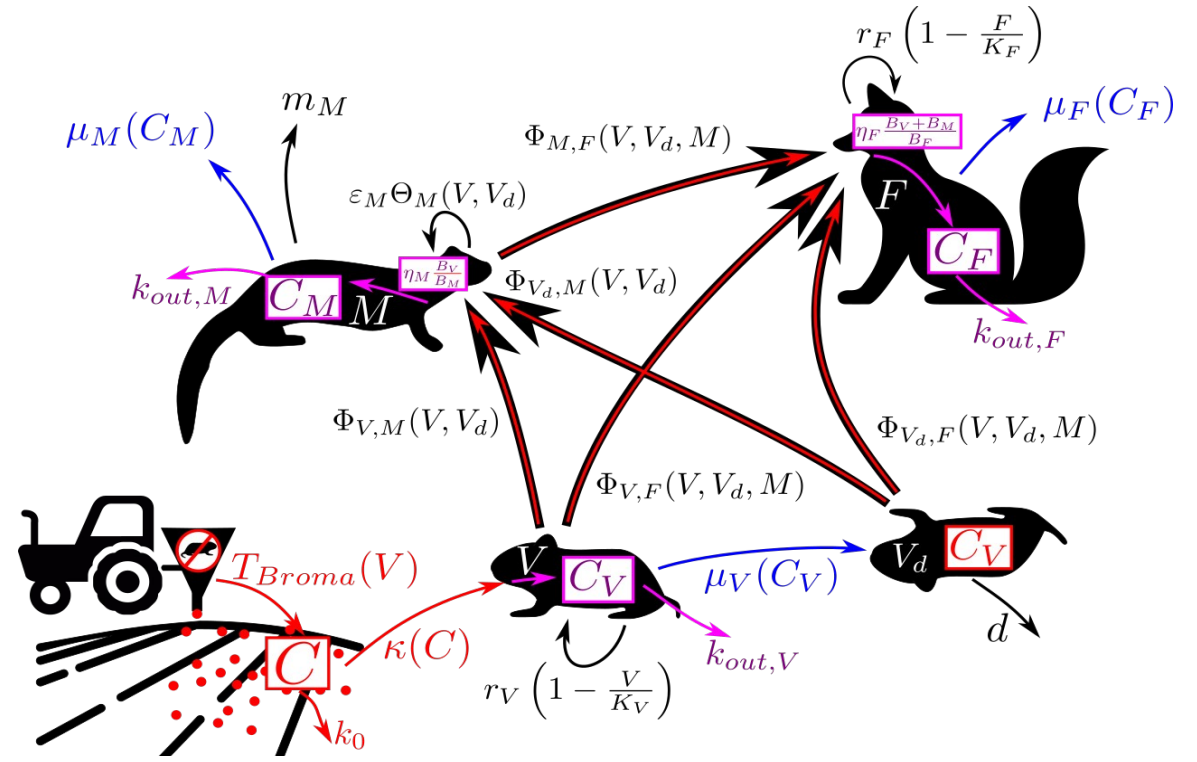
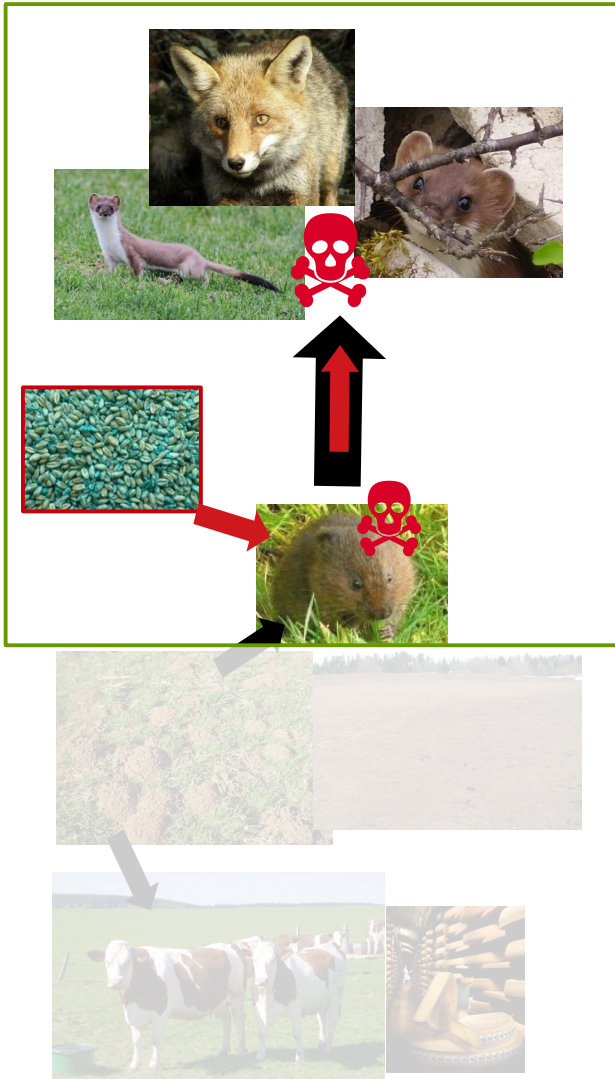


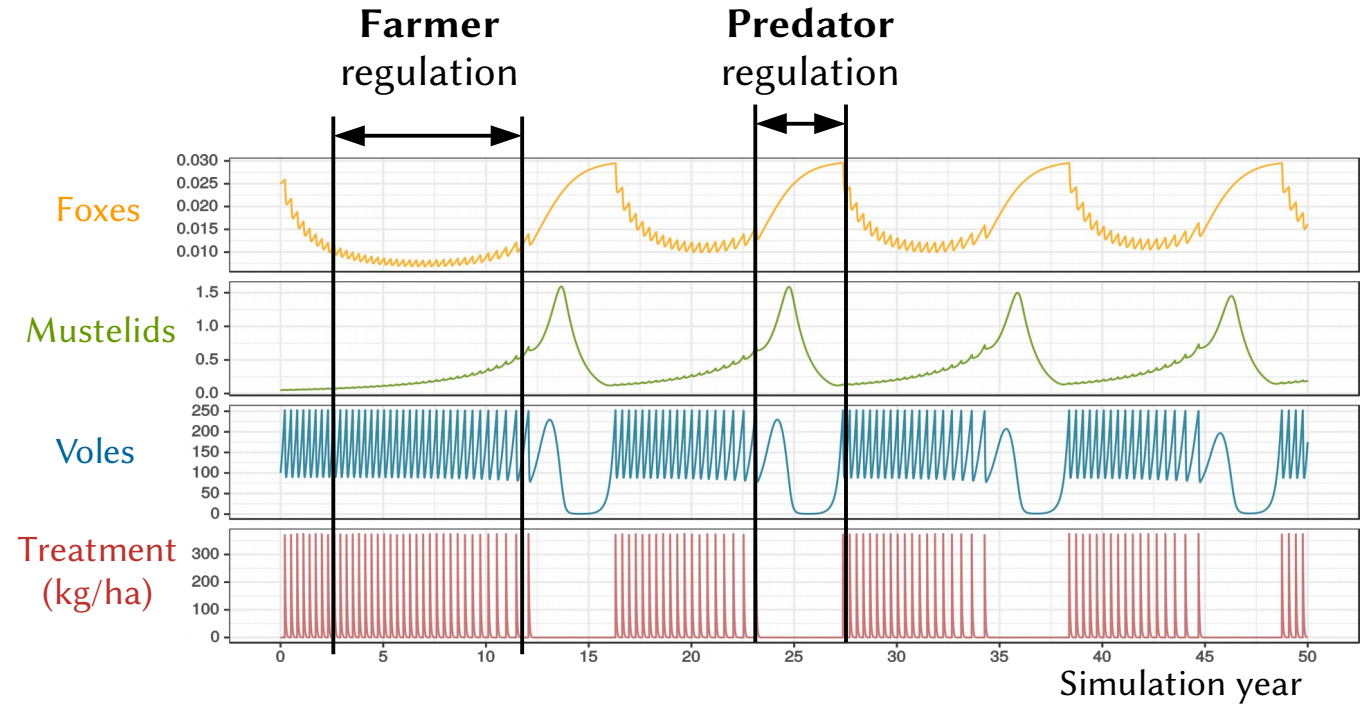
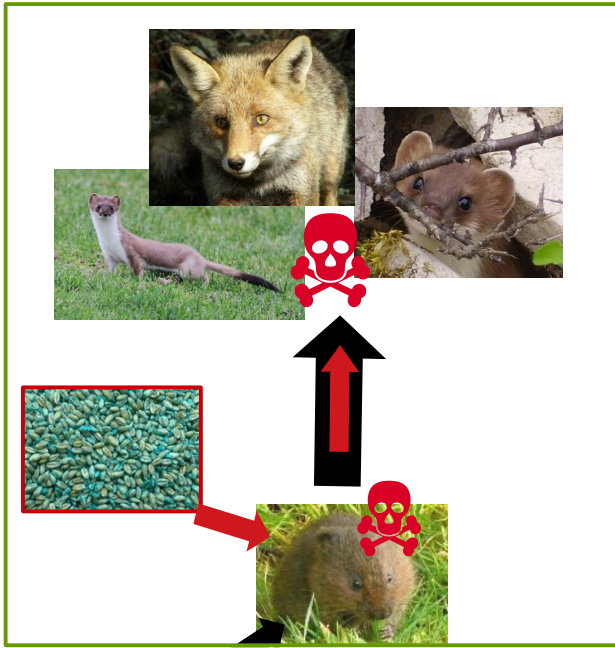
From observation of simple system, tipping point are hardly predictable...

... so in real complex !









➔ **Buffer in time to maintain biocontrol**



Implementation of Bayesian
inference for TKTD models
A way to track the propagation
of uncertainties in
environmental risk assessment

Virgile BAUDROT
Sandrine CHARLES

“In biology, variability is the main invariant”

Giuseppe Longo & Francis Bailly (2006)

Mathématiques et sciences de la nature ; la singularité physique du vivant

Mechanistic models

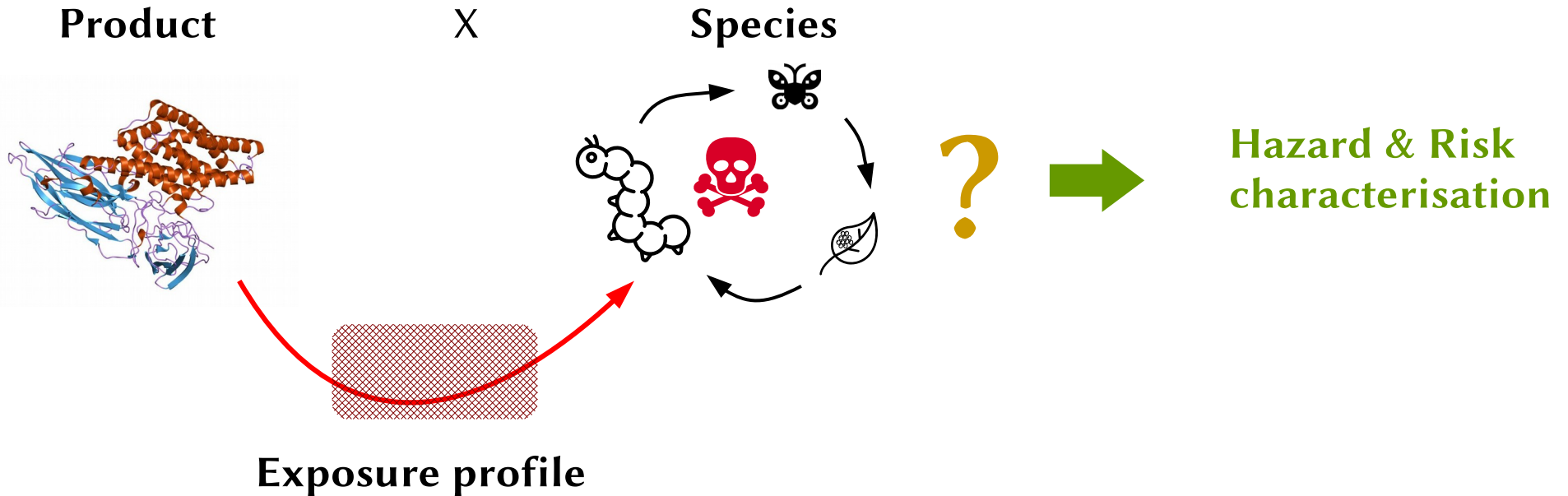


Challenge theories



Application?

Hazard identification



Risk identification

Hazard identification

Product x Species

**Data**

$$\mathcal{D} = \{\mathcal{E}, \mathbf{N}\}$$

- experimental design
- observation (survivors)

CalibrationLikelihood $\pi(\mathcal{D}|\theta)$  $\hat{\theta}(\mathcal{D})$ Point estimators of true parameters**Mechanistic models** $\mathcal{M}(\theta), \theta$ parameters

Hazard identification

Product x Species

**Data**

$$\mathcal{D} = \{\mathcal{E}, \mathbf{N}\}$$

- experimental design
- observation (survivors)

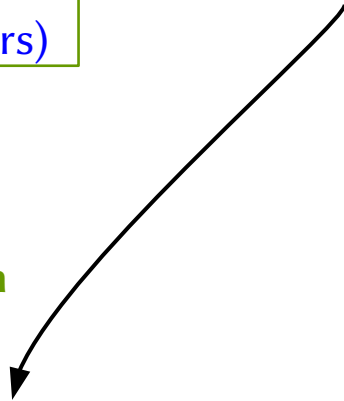
**Risk identification**Exposure profile \mathcal{E}'

Prediction $\mathcal{R}(\mathcal{E}'|\hat{\theta})$

CalibrationLikelihood $\pi(\mathcal{D}|\theta)$ 

$$\hat{\theta}(\mathcal{D})$$

Point estimators of true parameters

Mechanistic models $\mathcal{M}(\theta)$, θ parameters

Hazard identification

Product x Species

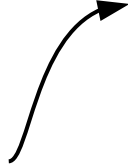
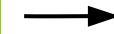
**Data**

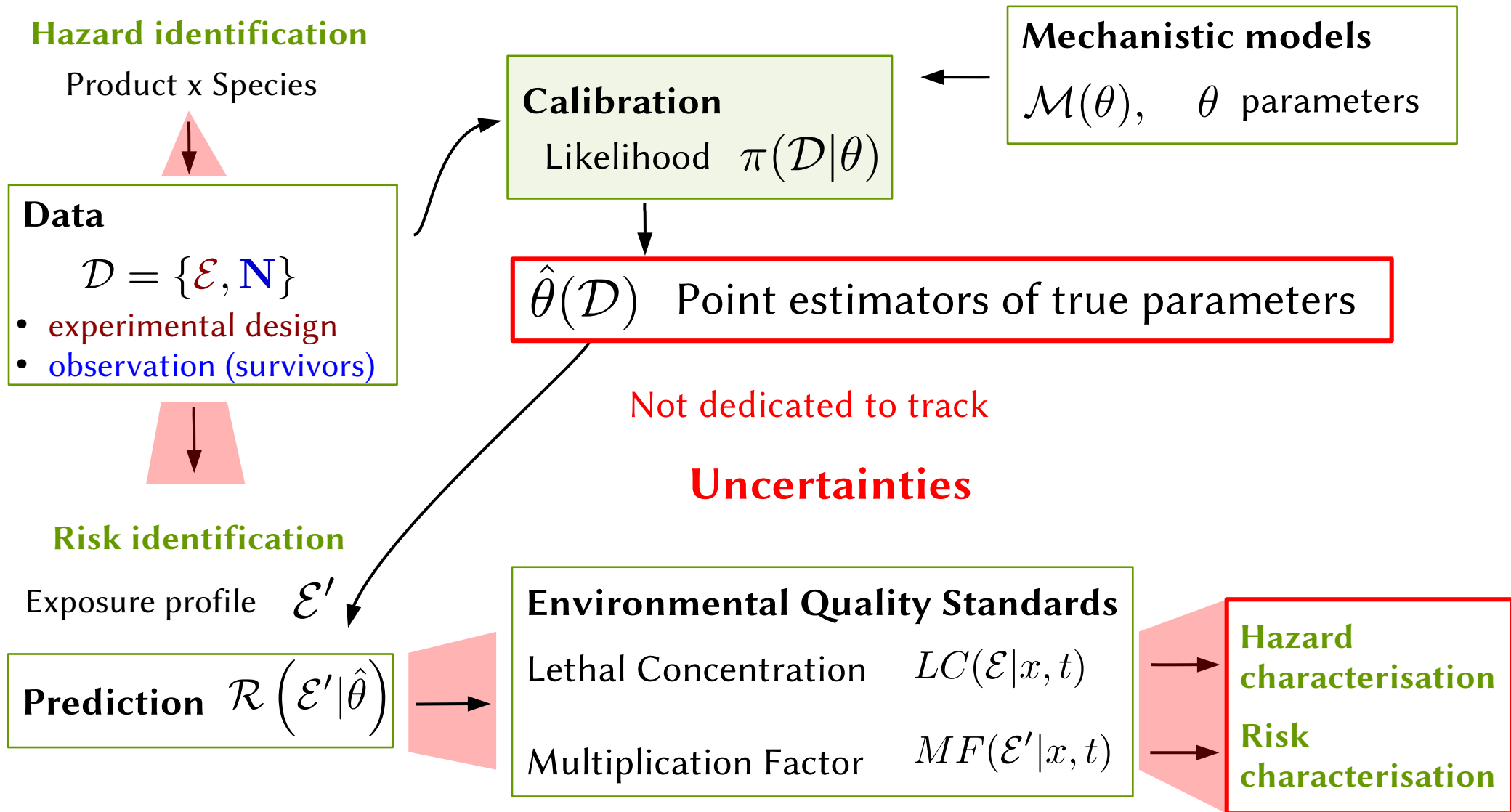
$$\mathcal{D} = \{\mathcal{E}, \mathbf{N}\}$$

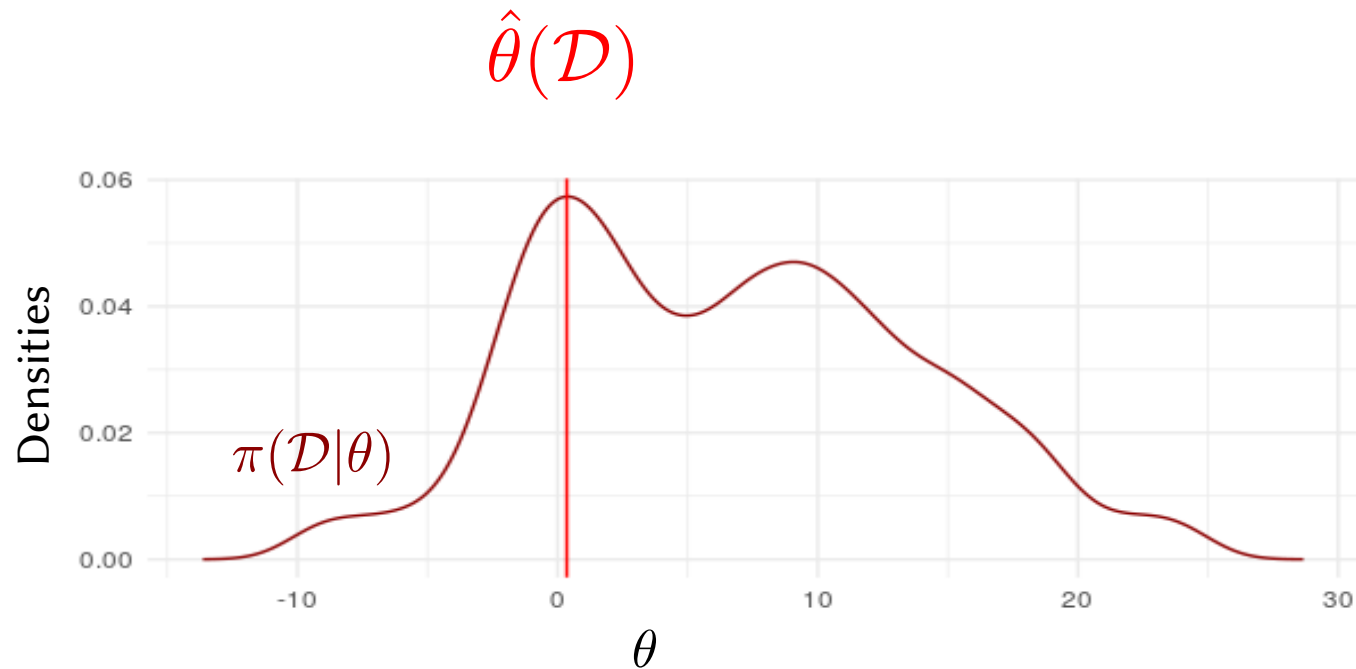
- experimental design
- observation (survivors)

**Risk identification**Exposure profile \mathcal{E}'

$$\text{Prediction } \mathcal{R}(\mathcal{E}' | \hat{\theta})$$

**Calibration**Likelihood $\pi(\mathcal{D} | \theta)$ 
 $\hat{\theta}(\mathcal{D})$ Point estimators of true parameters
**Mechanistic models**
 $\mathcal{M}(\theta), \theta$ parameters
**Environmental Quality Standards**Lethal Concentration $LC(\mathcal{E} | x, t)$ Multiplication Factor $MF(\mathcal{E}' | x, t)$ **Hazard characterisation****Risk characterisation**

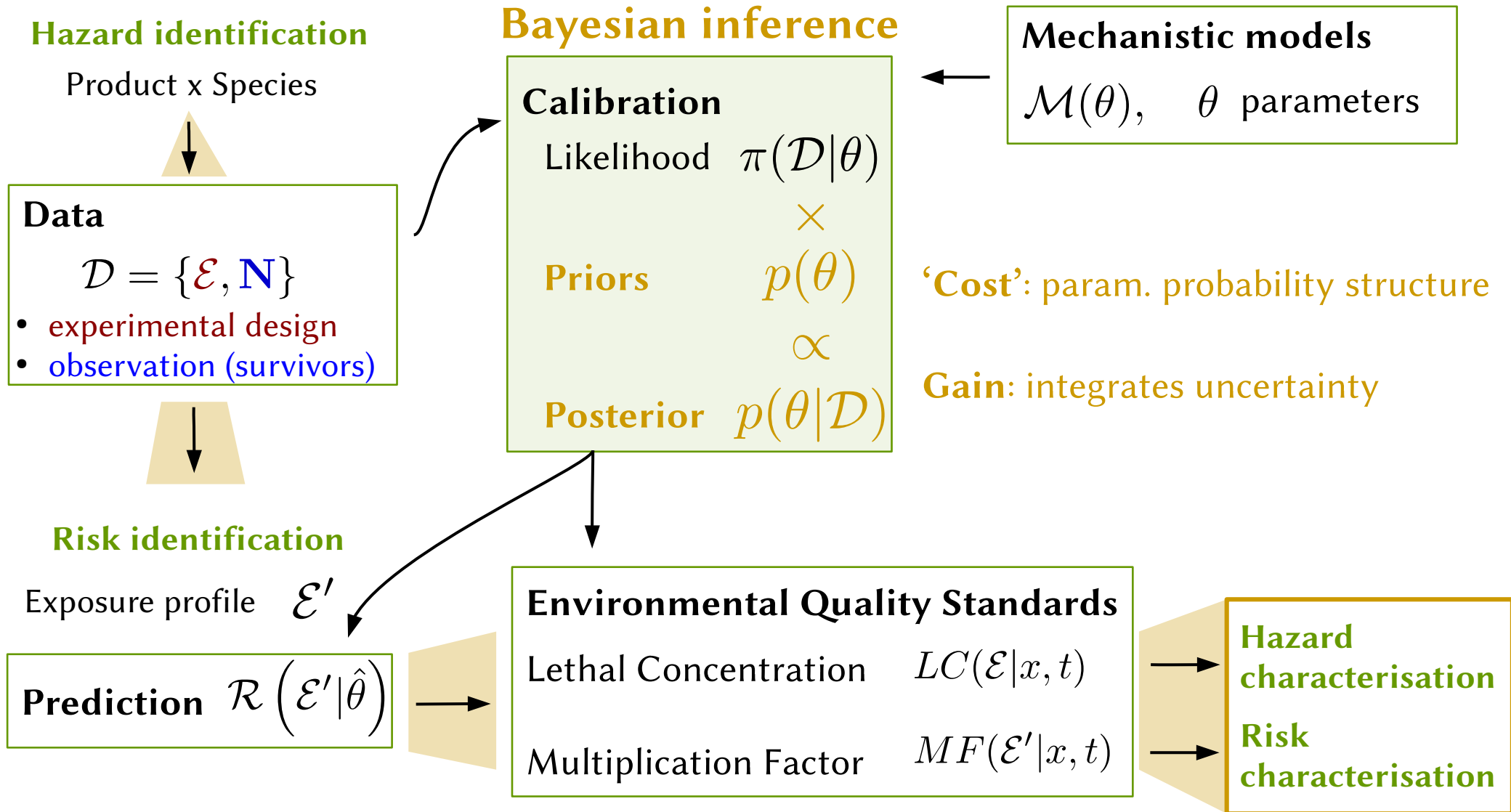


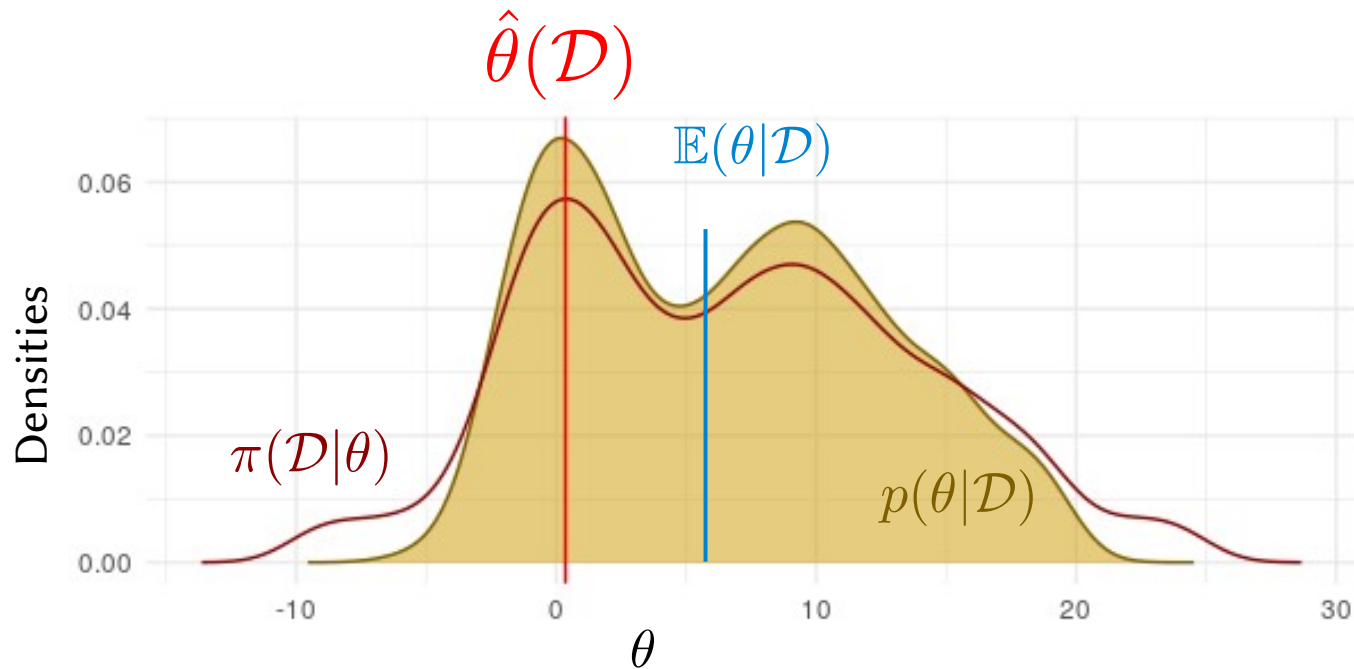


Frequentist

➡ max likelihood

$$\hat{\theta}(\mathcal{D}) = \operatorname{argmax}_{\theta} \pi(\mathcal{D}|\theta)$$





➔ probability structure on the parameter space

Frequentist

➔ max likelihood

$$\hat{\theta}(\mathcal{D}) = \operatorname{argmax}_{\theta} \pi(\mathcal{D}|\theta)$$

Bayesian

$$p(\theta|\mathcal{D}) \propto \pi(\mathcal{D}|\theta) \times p(\theta)$$

Toxicokinetic

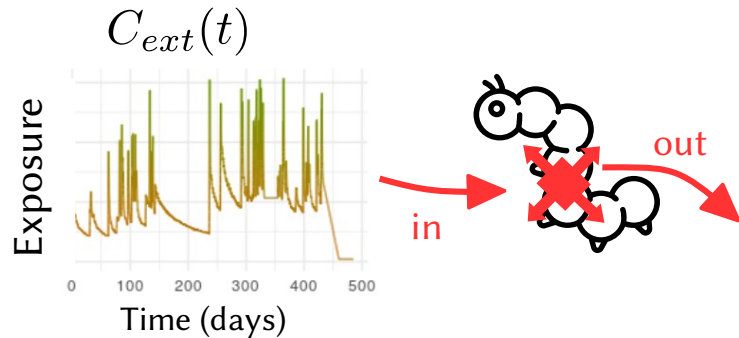
$$\frac{dD_{surv}(t)}{dt} = k_d (C_{ext}(t) - D_{surv}(t))$$

Toxicodynamic 

$$h(t) = h_+ \max_{0 \leq \tau \leq t} (D_{surv}(\tau) - z, 0) + h_b$$
$$S_{SD}(t) = \exp \left(- \int_0^t h(\tau) d\tau \right)$$

Toxicokinetic

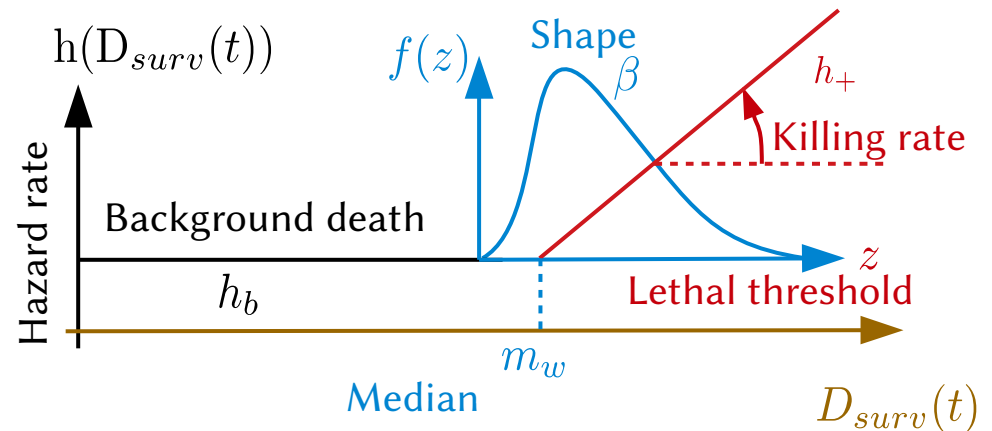
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Toxicokinetic

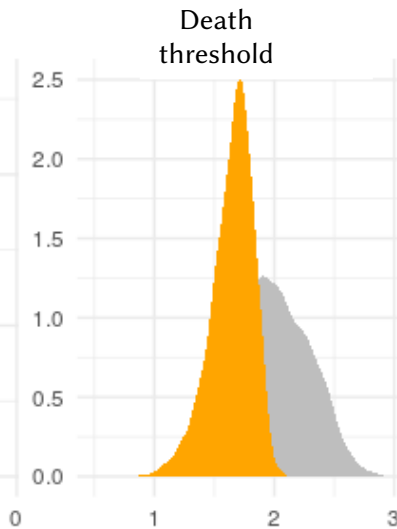
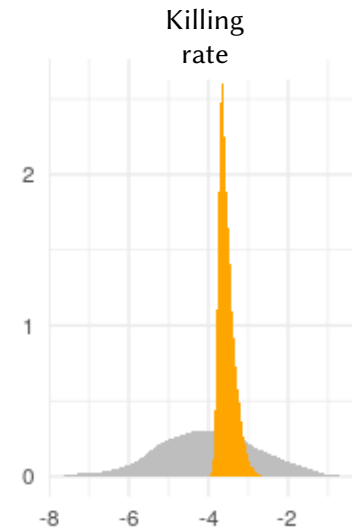
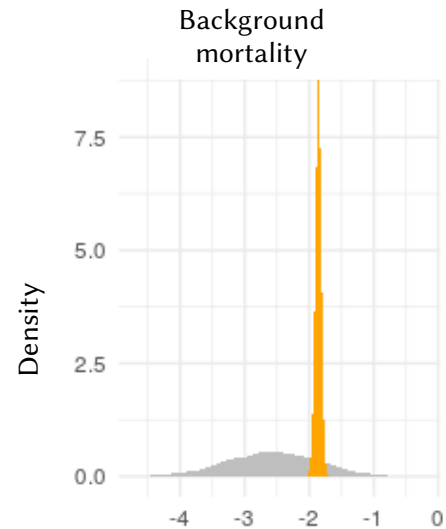
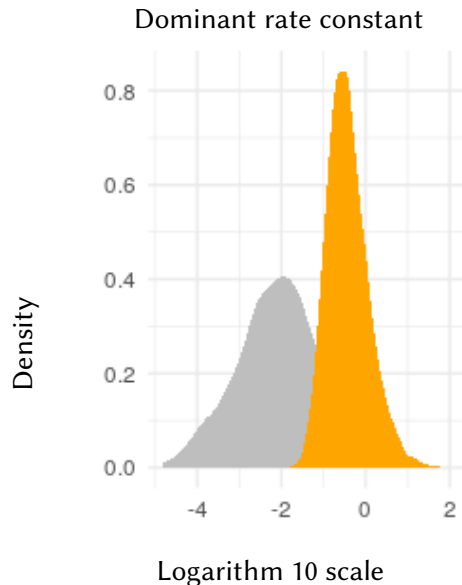
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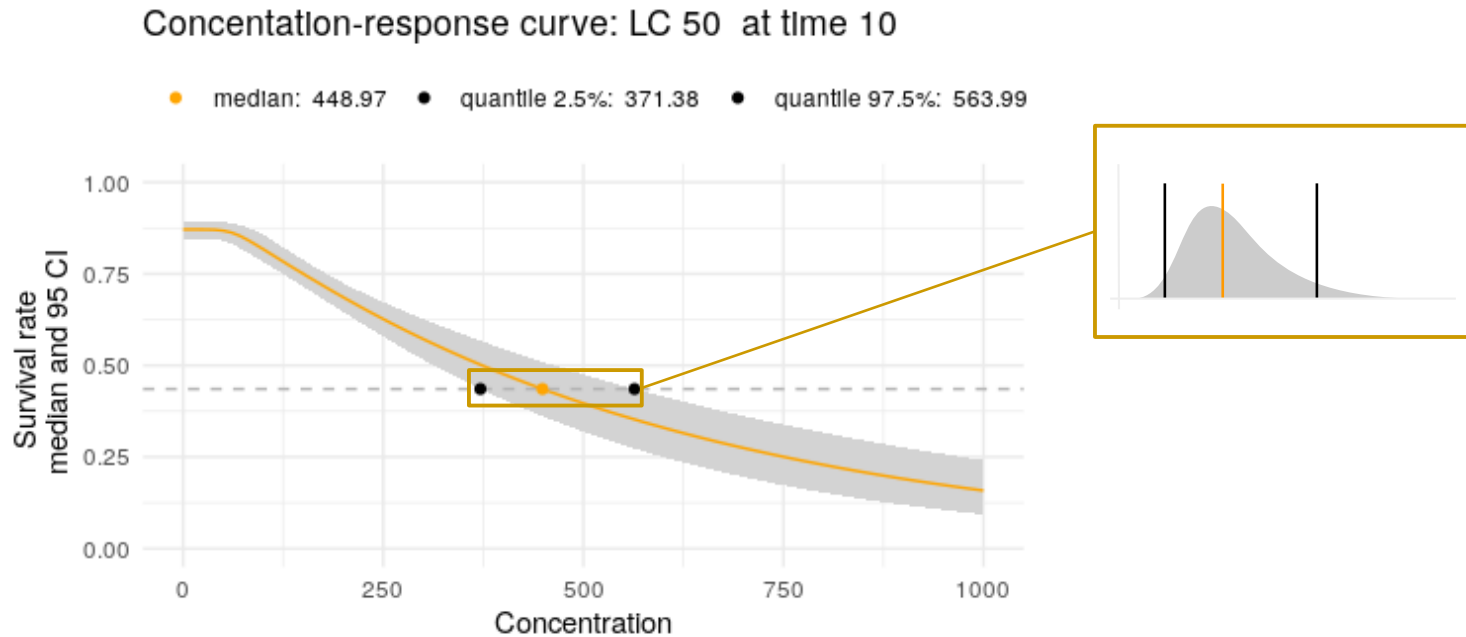
$$S_{SD}(t) = \exp \left(- \int_0^t h(\tau) d\tau \right)$$

Bayesian inference $\pi(\mathcal{D}|\theta) \times p(\theta) \propto p(\theta|\mathcal{D})$



➔ Uncertainties around Environmental Quality Standard

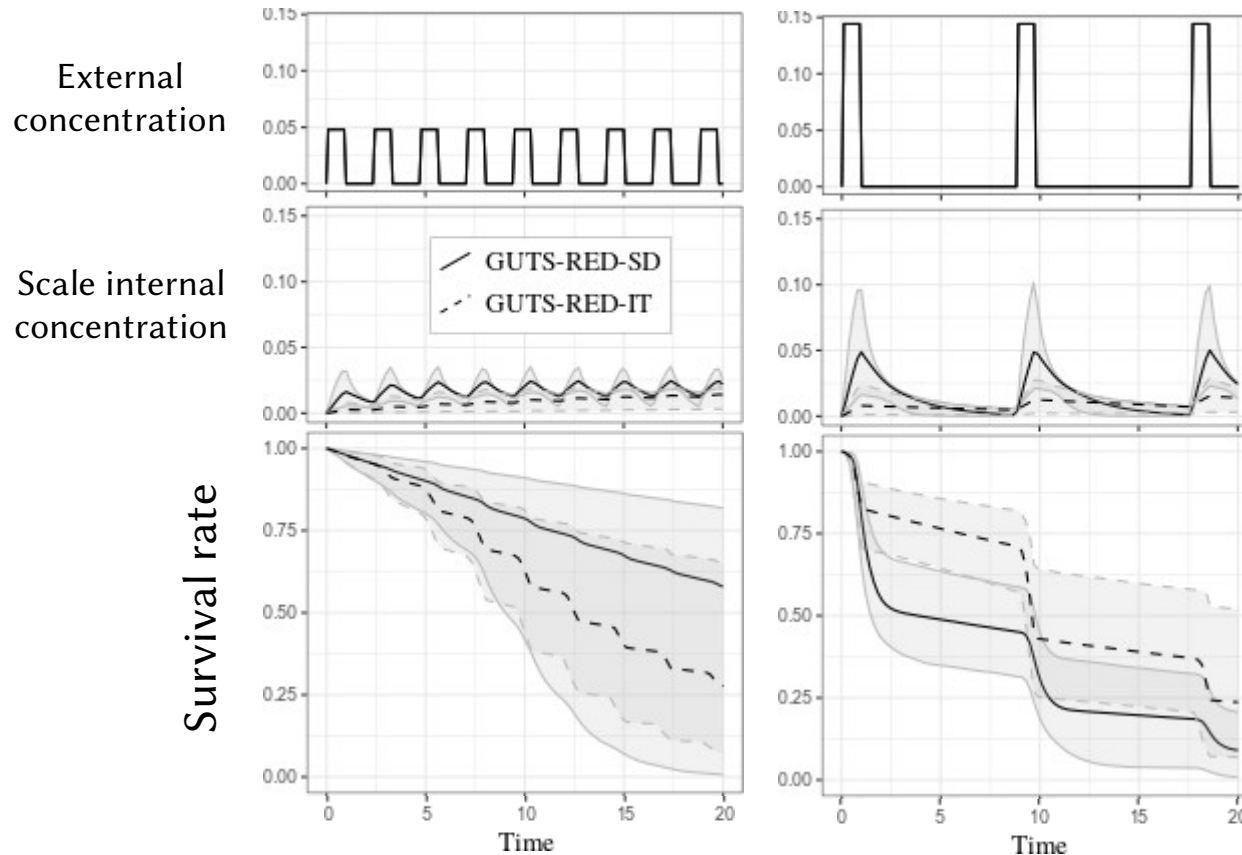
$$LC(\mathcal{E}|x, t)$$



Baudrot, V. ; Preux, S. ; Ducrot, V. ; Pavé, A. and Charles, S. (2018) *New insights to compare and choose TKTD models for survival based on an inter-laboratory study for Lymnaea stagnalis exposed to Cd.* **Env, Science & Tech.** 52(3) 1582-1590.

Baudrot, V. and Charles, S. (2019) *Recommendations to address uncertainties in environmental risk assessment using toxicokinetic-toxicodynamic models.* **PCI Ecology (2018)** => **Scientific Reports.** 9(11432)

➔ Uncertainties propagation over new exposure profiles

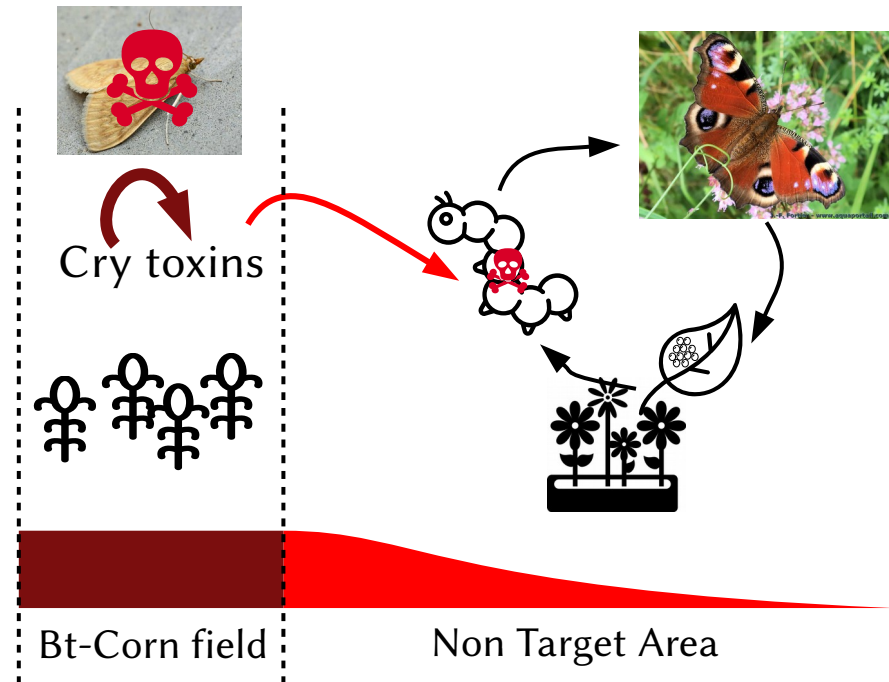


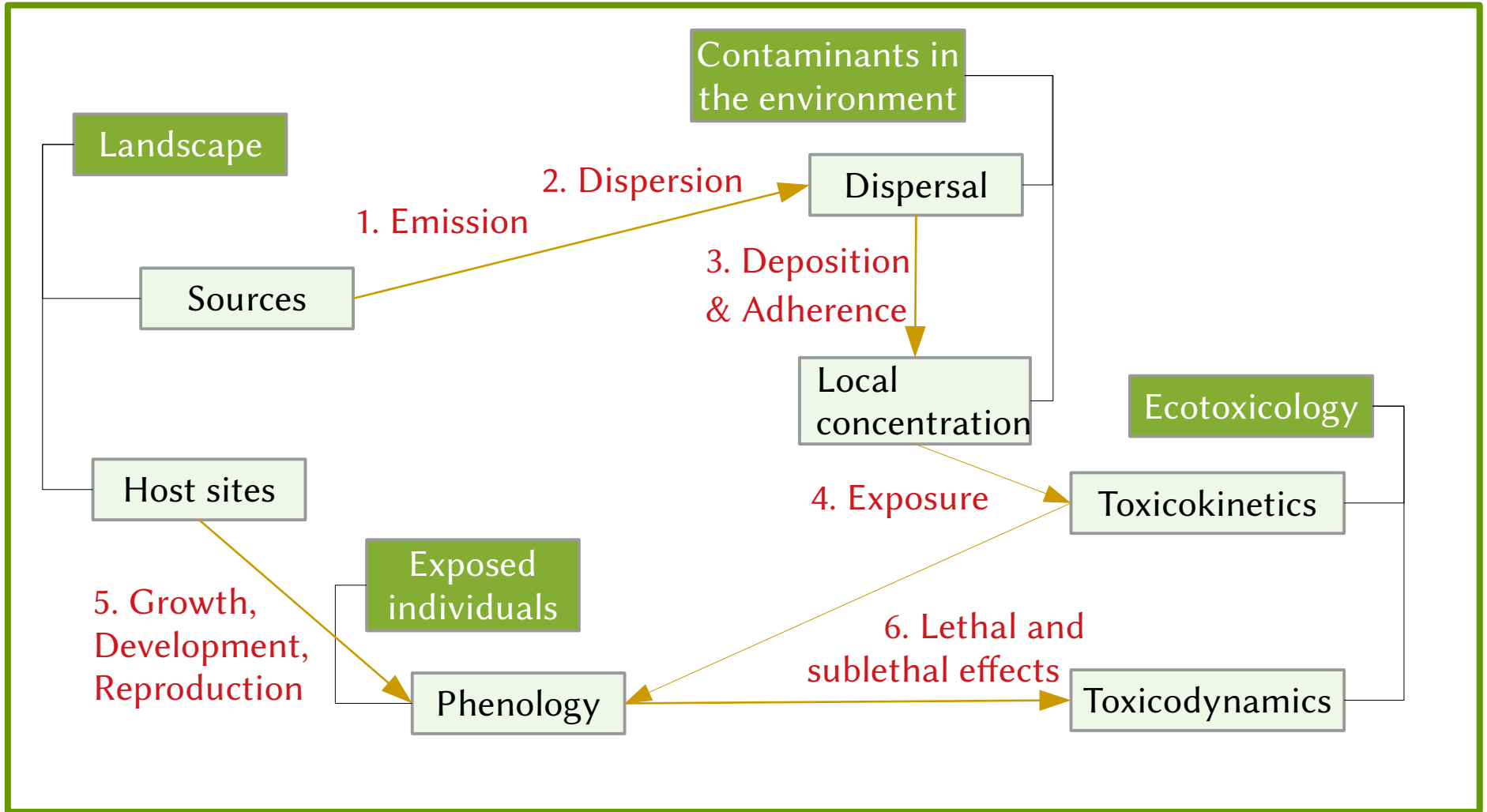
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BriskaR - A spatio-temporal exposure-hazard model for assessing environmental risk of Bt-maize on Non-Target Lepidoptera

Virgile BAUDROT
Samuel SOUBEYRAND
Antoine MESSÉAN
Andreas LANG
Stefanescu CONSTANTIN





Mechanistic models $\mathcal{M}(\theta)$
parameters θ

Data $\mathcal{D} = \{\mathcal{E}, \mathcal{O}\}$
experiment \mathcal{E} ; observations \mathcal{O}

1. Emission

Fields: C_n

Spatio-temporal emission:

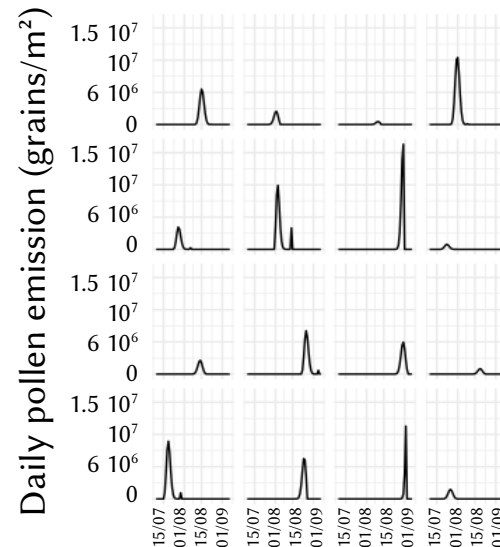
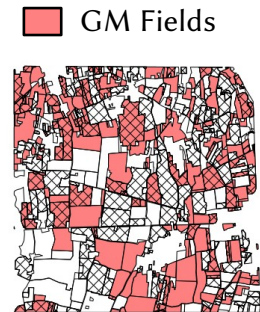
$$\tilde{E}(x, t) = \sum_{n \in N} \mathbf{1}(x \in C_n) E_n(t)$$

2. Dispersion

Dispersal kernel: $K(x, t)$

Contaminant intensity:

$$\lambda^{disp}(y, t) = \int_{\Omega} \tilde{E}(x, t) K(y - x) dx$$



Mechanistic models $\mathcal{M}(\theta)$
 parameters θ

Data $\mathcal{D} = \{\mathcal{E}, \mathcal{O}\}$
 experiment \mathcal{E} ; observations \mathcal{O}

Prediction $\mathcal{R}(\mathcal{E}'|\hat{\theta}(\mathcal{D}))$
 environment \mathcal{E}' ; inference params. $\hat{\theta}(\mathcal{D})$

1. Emission

Fields: C_n

Spatio-temporal emission:

$$\tilde{E}(x, t) = \sum_{n \in N} \mathbf{1}(x \in C_n) E_n(t)$$

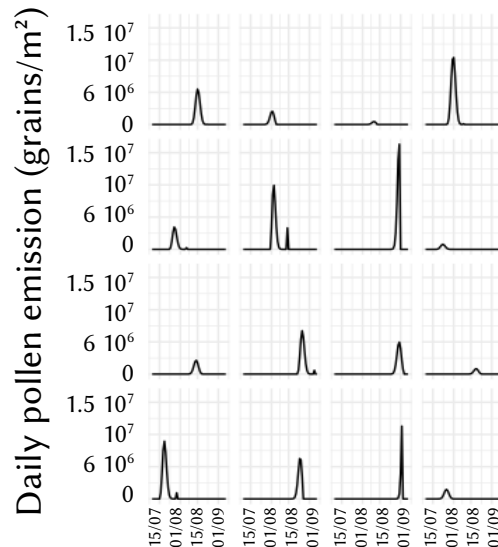
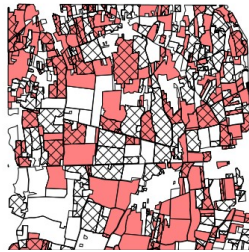
2. Dispersion

Dispersal kernel: $K(x, t)$

Contaminant intensity:

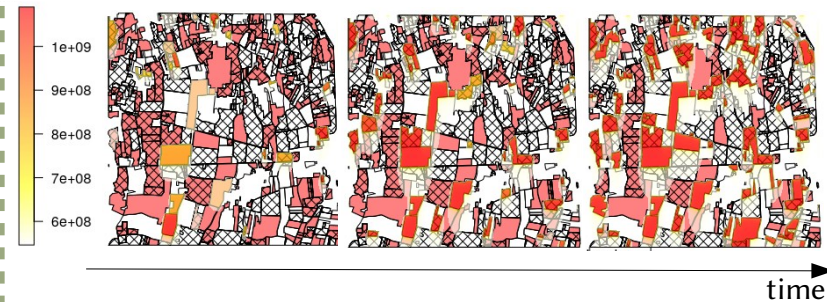
$$\lambda^{disp}(y, t) = \int_{\Omega} \tilde{E}(x, t) K(y - x) dx$$

GM Fields



Convolution computed with
 Fast Fourier Transform

$$\tilde{E} \otimes K(y, t) = \mathcal{F}^{-1} \left(\mathcal{F}(\tilde{E}) \mathcal{F}(K) \right)$$



Mechanistic models $\mathcal{M}(\theta)$
 parameters θ

3. Deposition & Adherence

$$\lambda_{local}(y, t) = (1 - \alpha(Z(t))) \lambda_{local}(y, t - 1) + \beta \lambda_{disp}(y, t)$$

4. Exposure

5. Development

$$\delta_0(T) = \exp(\rho T) - \exp\left(\rho T_{max} - \frac{T_{max} - T}{\Delta}\right) + \lambda$$

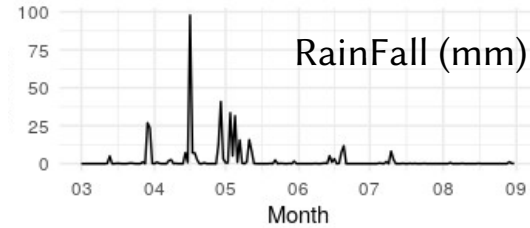
- $r(T)$: development rate
- T : temperature
- T_{max} : upper survival temperature
- ρ, Δ, λ : other parameters to fit

Mechanistic models $\mathcal{M}(\theta)$
parameters θ

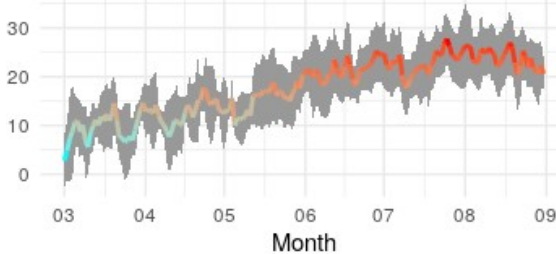
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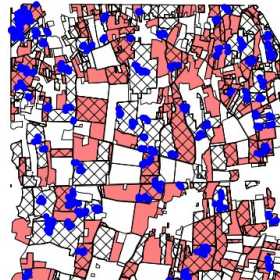
$$\lambda_{local}(y, t) = (1 - \alpha(Z(t))) \lambda_{local}(y, t - 1) + \beta \lambda_{disp}(y, t)$$



Temperature (mean, [min,max])



Larvae sites



5. Development

$$\delta_0(T) = \exp(\rho T) - \exp\left(\rho T_{max} - \frac{T_{max} - T}{\Delta}\right) + \lambda$$

- $r(T)$: development rate
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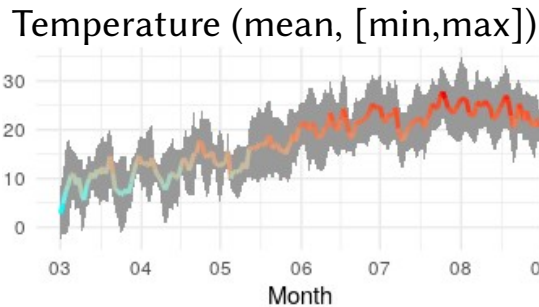
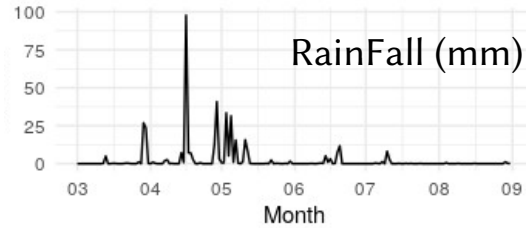
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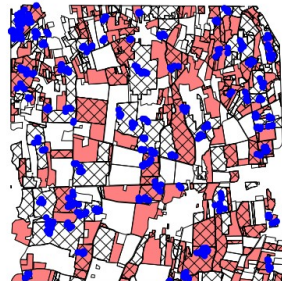
Prediction $\mathcal{R}(\mathcal{E}' | \hat{\theta}(\mathcal{D}))$
 environment \mathcal{E}' ; inference params. $\hat{\theta}(\mathcal{D})$

3. Deposition & Adherence

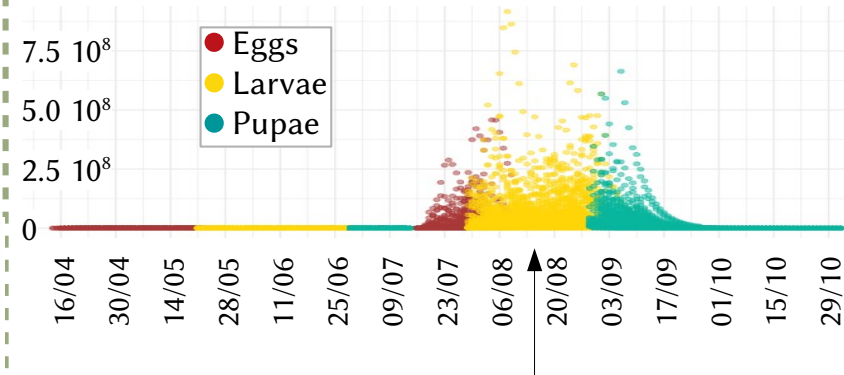
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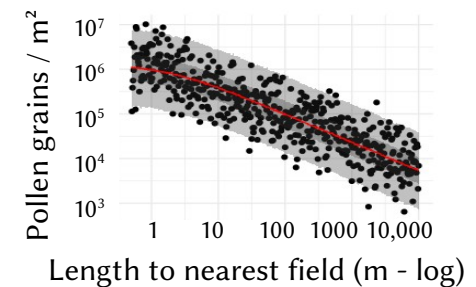
Larvae sites



Exposure nbr grains / m²



Exposure profile 15/08



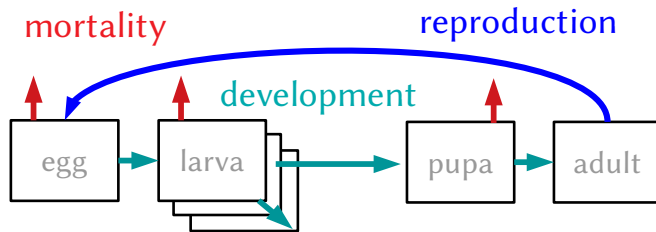
4. Exposure

5. Development

$$\delta_0(T) = \exp(\rho T) - \exp\left(\rho T_{max} - \frac{T_{max} - T}{\Delta}\right) + \lambda$$

- $r(T)$: development rate
- T : temperature
- T_{max} : upper survival temperature
- ρ, Δ, λ : other parameters to fit

Mechanistic models $\mathcal{M}(\theta)$
 parameters θ



6.1 Sublethal on Repro.

$$R(t) = R_0(t) \times \exp(-H_{repro}^+(t))$$

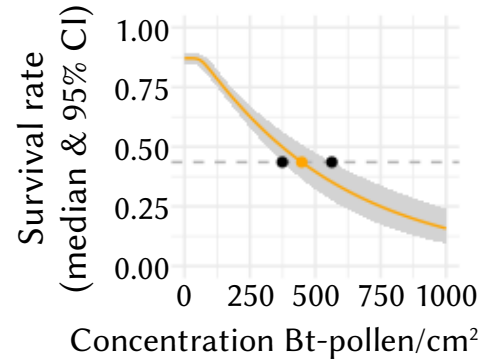
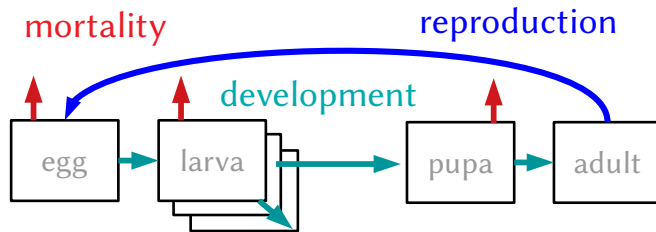
$$N_{G+1}(t) = R(t) \times \text{NID}_G(t)$$

6.2 Sublethal on Growth

$$\delta(t) = \delta_0(t) \times \exp(-H_{dev}^+(t))$$

Mechanistic models $\mathcal{M}(\theta)$
parameters θ

Data $\mathcal{D} = \{\mathcal{E}, \mathcal{O}\}$
experiment \mathcal{E} ; observations \mathcal{O}



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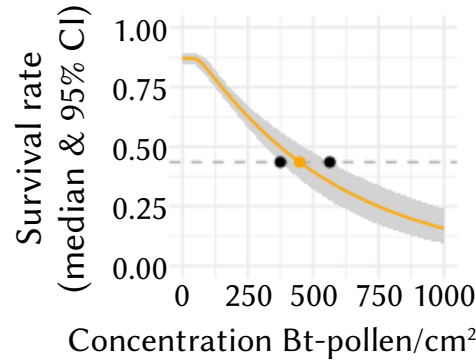
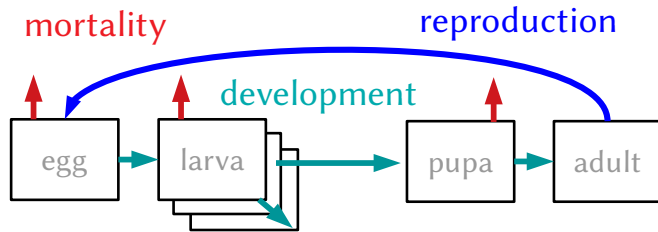
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Mechanistic models $\mathcal{M}(\theta)$
 parameters θ

Data $\mathcal{D} = \{\mathcal{E}, \mathcal{O}\}$
 experiment \mathcal{E} ; observations \mathcal{O}

Prediction $\mathcal{R}(\mathcal{E}' | \hat{\theta}(\mathcal{D}))$
 environment \mathcal{E}' ; inference params. $\hat{\theta}(\mathcal{D})$



**➔ In average,
 everything is fine...
 ... risk is in the quantiles**

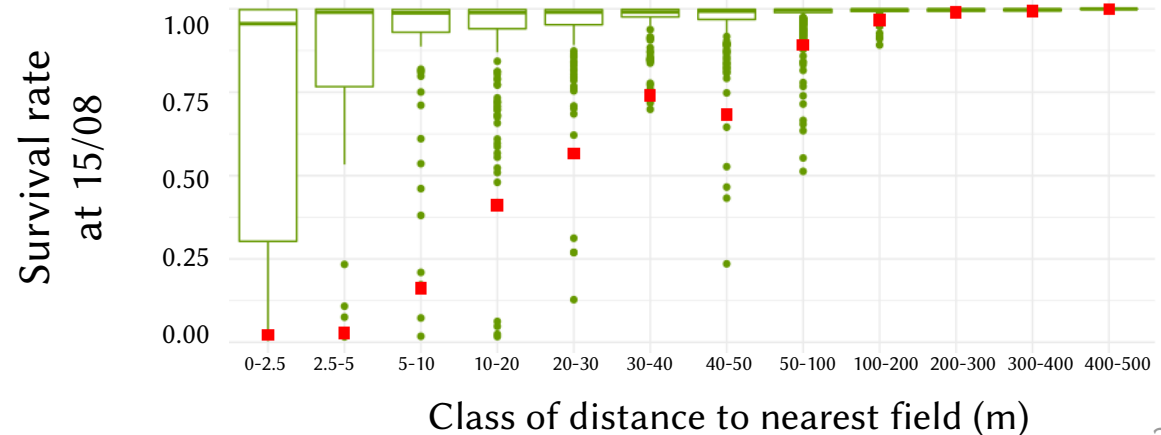
6.1 Sublethal on Repro.

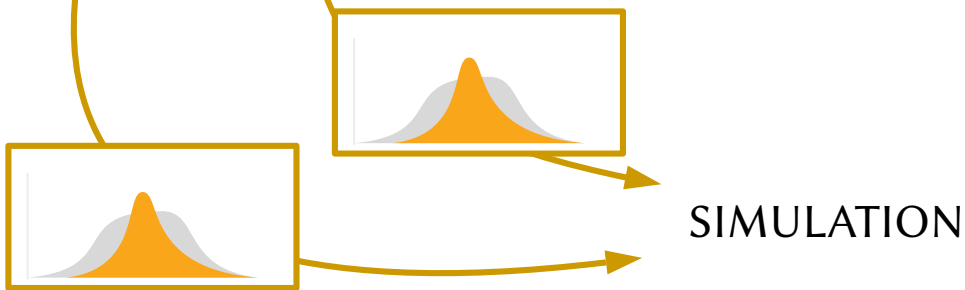
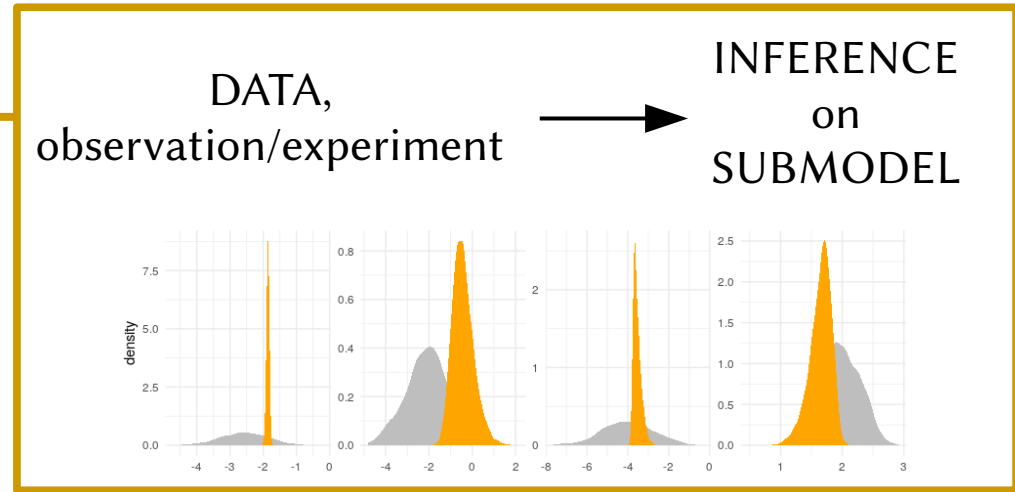
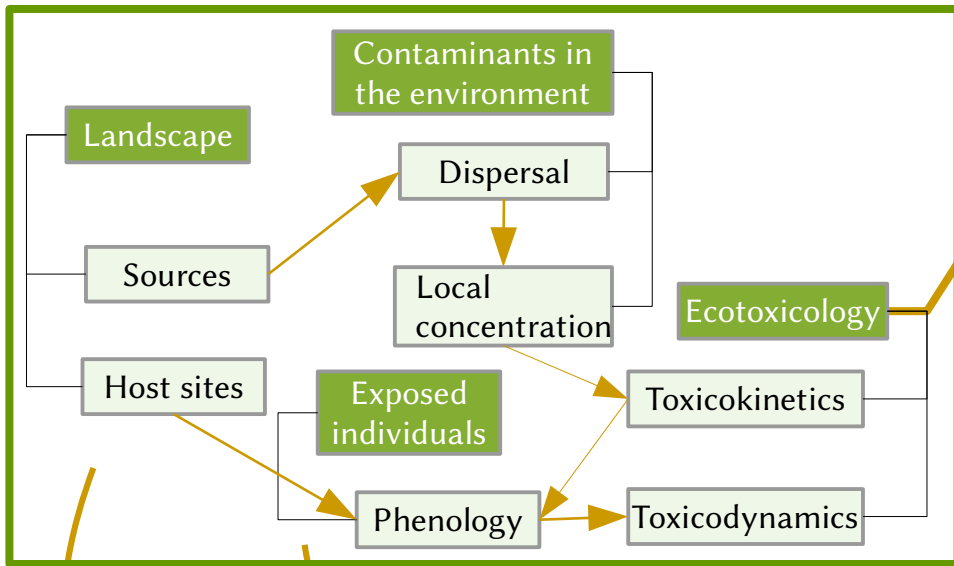
$$R(t) = R_0(t) \times \exp(-H_{repro}^+(t))$$

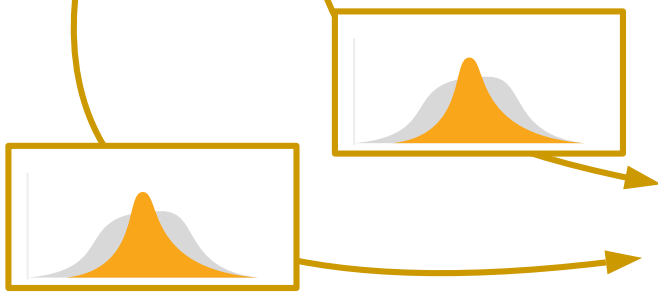
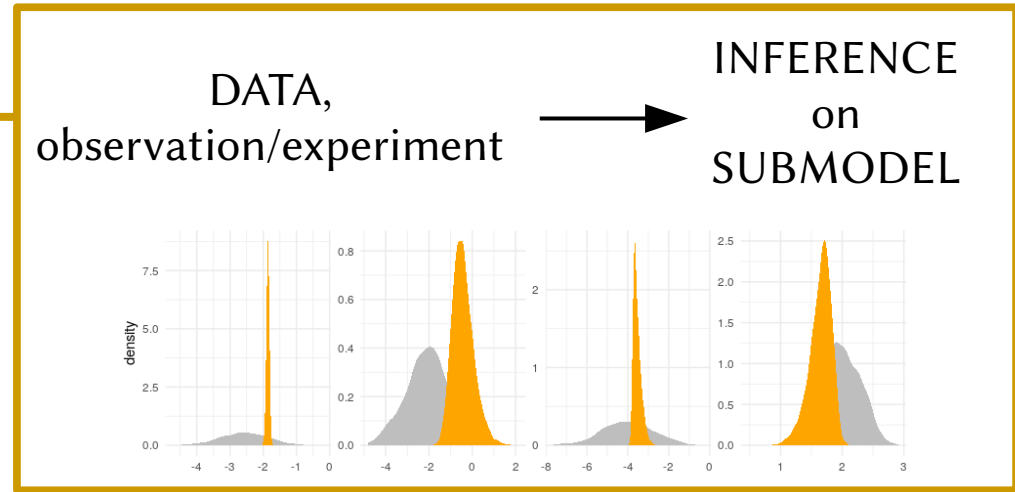
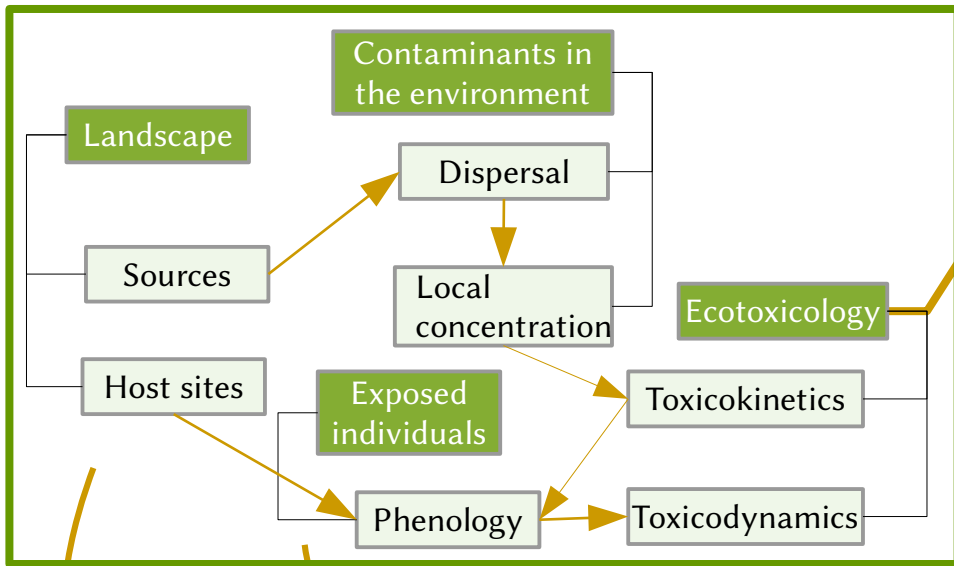
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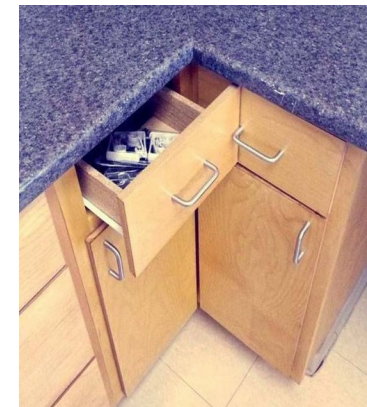






SIMULATION

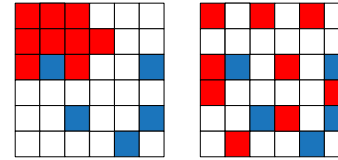
GLOBAL SENSITIVITY ANALYSIS



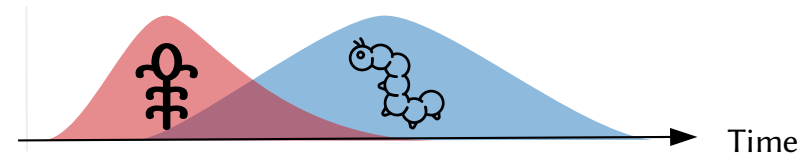
- 2 unitary tests
- 0 integration test

➔ 3 driving factors of sensitivity (need further investigation)

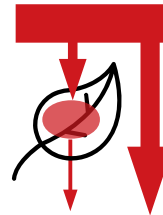
1. Aggregation of GM fields (SPATIAL)



2. Overlapping deposition ↔ sensitive stage

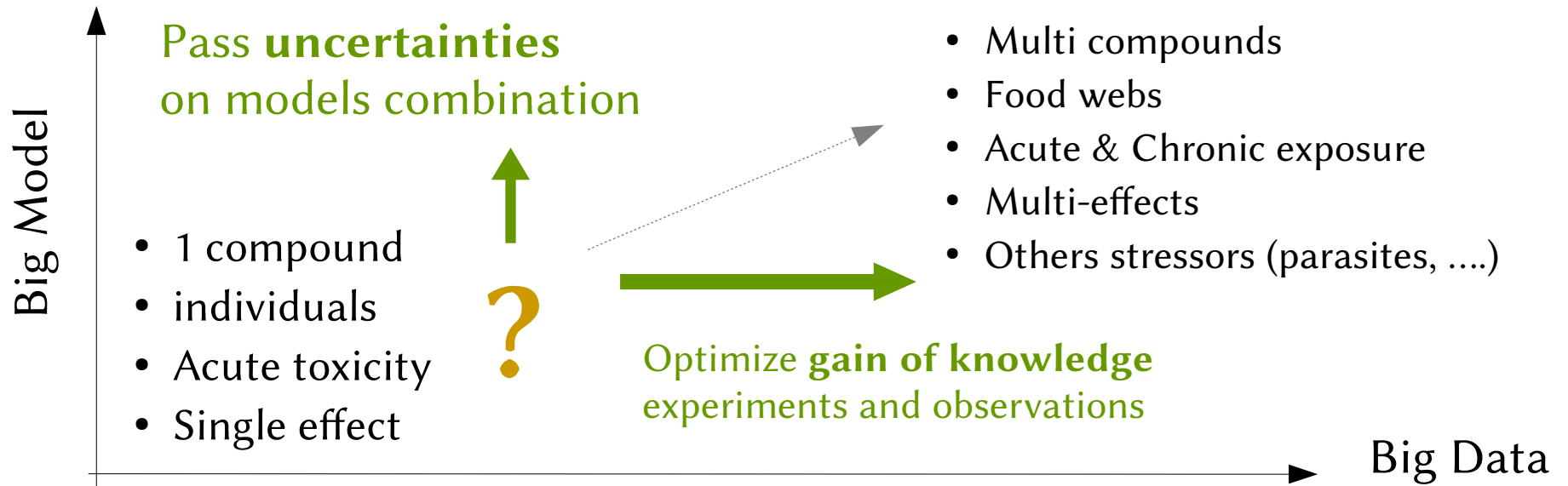


3. Loss and Adherence of pollen



1. Review/Build/Rebuild a set of model of pest-control strategies
→ Open Agent Based Model/Platform
2. Assessment of their environmental impact
→ Space, Time, Trophic Link, Evolution
3. Uncertainty analysis (Sensitivity, Bayesian inference)
→ lack of knowledge (inputs, output, latent variables)

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Thank you for your attention

$$\mathbb{P}(\text{Thanks}|\text{Attention}) = \frac{\mathbb{P}(\text{Attention}|\text{Thanks}) \times \mathbb{P}(\text{Thanks})}{\mathbb{P}(\text{Attention})}$$

Sciencehood

Goodness of fitting interesting question